

# Exam #2 Answer Key

Economics 435: Quantitative Methods

Spring 2006

## 1 Ugly criminals

- a) Teenagers with high family income can spend more on clothes, makeup, gym memberships, etc., all with the intention of making themselves look better. So it is likely that  $cov(income, ugly) < 0$ . It is also likely that high family income reduces the relative benefits to a life of crime ( $\beta_2 < 0$ ).
- b) Since  $\text{plim } \hat{\beta}_1 = \beta_1 + \beta_2 \frac{cov(ugly, income)}{var(ugly)}$ , my guesses imply that  $\text{plim } (\hat{\beta}_1 - \beta_1) > 0$ .
- c) We are more likely to conclude that being unattractive increases the likelihood of committing crimes, as Mocan and Tekin conclude.
- d) This is just an example of measurement error, so our results on measurement error apply. An OLS regression of *crime* on (*ugly*, *x*) will not tend to lead researchers to conclude a positive effect of (true) unattractiveness on crime even if there is no effect. It will, however, lead them to systematically underestimate the effect of unattractiveness on crime.

## 2 Peer effects

- a) It will be negative.
- b) We only need one year of data to calculate  $\hat{\beta}_1^{OLS}$ , but need two years of data to calculate  $\hat{\beta}_1^{FE1}$  and three years of data to calculate  $\hat{\beta}_1^{FE2}$ .
- c)

$$\begin{aligned}\text{plim } \hat{\beta}_1^{OLS} &= \beta_1 + \frac{cov(\alpha_i, x_{it})}{var(x_{it})} \\ \text{plim } \hat{\beta}_1^{FE1} &= \beta_1 \\ \text{plim } \hat{\beta}_1^{FE2} &= \beta_1\end{aligned}$$

So  $\hat{\beta}_1^{FE1}$  and  $\hat{\beta}_1^{FE2}$  are consistent.

d)

$$\begin{aligned}\text{plim } \hat{\beta}_1^{OLS} &= \beta_1 + \frac{cov(\alpha_i + \delta_i t, x_{it})}{var(x_{it})} \\ \text{plim } \hat{\beta}_1^{FE1} &= \beta_1 + \frac{cov(\delta_i t, x_{it} - x_{i1})}{var(x_{it} - x_{i1})} \\ \text{plim } \hat{\beta}_1^{FE2} &= \beta_1\end{aligned}$$

So  $\hat{\beta}_1^{FE2}$  is consistent.