

Solution: (a) Write the steady flow energy equation from top to bottom:

$$\frac{p_1}{\rho g} + \frac{\alpha_1 V_1^2}{2g} + (H + L) = \frac{p_2}{\rho g} + \frac{\alpha_2 V_2^2}{2g} + 0 + h_f, \quad \text{or:} \quad h_f = \frac{32\mu LV}{\rho g d^2} = H + L - \frac{\alpha_2 V_2^2}{2g}$$

Noting that, in a tube, $Q = V\pi d^2/4$, we may eliminate V in favor of Q and solve for the fluid viscosity:

$$\mu = \frac{\pi \rho g d^4}{128 L Q} (H + L) - \frac{\alpha_2 \rho Q}{16 \pi L} \quad \text{Ans. (a)}$$

(b) For the given data, converting $d = 0.041 \text{ in} = 0.00104 \text{ m}$, $L = 36.1 \text{ in} = 0.917 \text{ m}$, and $Q = 0.31 \text{ mL/s} = 3.1 \text{E-}7 \text{ m}^3/\text{s}$, we may substitute in the above formula (a) and calculate

$$\begin{aligned} \mu &= \frac{\pi(998.7)(9.81)(0.00104)^4}{128(0.917)(3.1\text{E-}7)}(0.153 + 0.917) - \frac{2.0(998.7)(3.1\text{E-}7)}{16\pi(0.917)} \\ &= 0.001063 - 0.000013 \approx \mathbf{0.00105} \frac{\text{kg}}{\text{m} \cdot \text{s}} \quad \text{Ans. (b)} \end{aligned}$$

(c) The accepted value (see Appendix Table A-1) for water at 16.5°C is $\mu \approx 1.11\text{E-}3 \text{ kg/m}\cdot\text{s}$, the error in the experiment is thus about -5.5% . *Ans. (c)*

(d) If we forgot the kinetic-energy correction factor $\alpha_2 = 2.0$ for laminar flow, the calculation in part (b) above would result in

$$\mu = 0.001063 - 0.000007 \approx \mathbf{0.001056} \text{ kg/m}\cdot\text{s} \text{ (negligible 0.6\% error)} \quad \text{Ans. (d)}$$

In this experiment, the dominant (first) term is the *elevation change* ($H + L$)—the momentum exiting the tube is negligible because of the low velocity (0.36 m/s).

3.139 The horizontal pump in Fig. P3.139 discharges 20°C water at $57 \text{ m}^3/\text{h}$. Neglecting losses, what power in kW is delivered to the water by the pump?

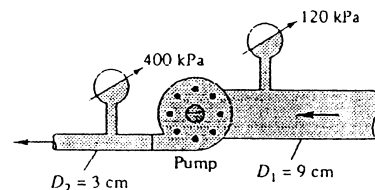


Fig. P3.139

Solution: First we need to compute the velocities at sections (1) and (2):

$$V_1 = \frac{Q}{A_1} = \frac{57/3600}{\pi(0.045)^2} = 2.49 \frac{\text{m}}{\text{s}}; \quad V_2 = \frac{Q}{A_2} = \frac{57/3600}{\pi(0.15)^2} = 22.4 \frac{\text{m}}{\text{s}}$$