

For seawater, take $\rho = 1.99 \text{ slug/ft}^3$, $\mu = 2.23\text{E-}5 \text{ slug/ft}\cdot\text{s}$. With $L_p = 150 \text{ ft}$ and $V_p = 15 \text{ knots} = 25.3 \text{ ft/s}$, evaluate

$$\text{Re}_{\text{proto}} = \frac{\rho_p V_p L_p}{\mu_p} = \frac{1.99(25.3)(150)}{2.23\text{E-}5} \approx 3.39\text{E}8; \quad \text{Fr}_p = \frac{25.3}{[32.2(150)]^{1/2}} \approx 0.364$$

For $\text{Fr} \approx 0.364$, interpolate to $C_{F,\text{wave}} \approx 0.0027$

Thus we can immediately estimate $F_{\text{wave}} \approx 0.0027(1.99)(25.3)^2(150)^2 \approx 77000 \text{ lbf}$. However, as mentioned in Fig. 5.8 of the text, Re_p is far outside the range of the friction force data, therefore we must *extrapolate* as best we can. A power-law curve-fit is

$$C_{F,\text{friction}} \approx \frac{0.0178}{\text{Re}^{0.144}}, \quad \text{hence } C_{F,\text{proto}} \approx \frac{0.0178}{(3.39\text{E}8)^{0.144}} \approx 0.00105$$

Thus $F_{\text{friction}} \approx 0.00105(1.99)(25.3)^2(150)^2 \approx 30000 \text{ lbf}$. **Ftotal $\approx 107000 \text{ lbf}$.** *Ans.*

5.77 A dam spillway is to be tested by using Froude scaling with a one-thirtieth-scale model. The model flow has an average velocity of 0.6 m/s and a volume flow of $0.05 \text{ m}^3/\text{s}$. What will the velocity and flow of the prototype be? If the measured force on a certain part of the model is 1.5 N , what will the corresponding force on the prototype be?

Solution: Given $\alpha = L_m/L_p = 1/30$, Froude scaling requires that

$$V_p = \frac{V_m}{\sqrt{\alpha}} = \frac{0.6}{(1/30)^{1/2}} \approx 3.3 \frac{\text{m}}{\text{s}}; \quad Q_p = \frac{Q_m}{\alpha^{5/2}} = \frac{0.05}{(1/30)^{5/2}} \approx 246 \frac{\text{m}^3}{\text{s}} \quad \text{Ans. (a)}$$

The force scales in similar manner, assuming that the density remains constant (water):

$$F_p = F_m \left(\frac{\rho_p}{\rho_m} \right) \left(\frac{V_p}{V_m} \right)^2 \left(\frac{L_p}{L_m} \right)^2 = F_m (1) \left(\frac{1}{\sqrt{\alpha}} \right)^2 \left(\frac{1}{\alpha} \right)^2 = (1.5)(30)^3 \approx 40500 \text{ N} \quad \text{Ans. (b)}$$

5.78 A prototype spillway has a characteristic velocity of 3 m/s and a characteristic length of 10 m . A small model is constructed by using Froude scaling. What is the minimum scale ratio of the model which will ensure that its minimum Weber number is 100 ? Both flows use water at 20°C .

Solution: For water at 20°C , $\rho = 998 \text{ kg/m}^3$ and $Y = 0.073 \text{ N/m}$, for both model and prototype. Evaluate the Weber number of the prototype:

$$\text{We}_p = \frac{\rho_p V_p^2 L_p}{Y_p} = \frac{998(3.0)^2(10.0)}{0.073} \approx 1.23\text{E}6; \quad \text{for Froude scaling,}$$