6.5 In flow past a body or wall, early transition to turbulence can be induced by placing a trip wire on the wall across the flow, as in Fig. P6.5. If the trip wire in Fig. P6.5 is placed where the local velocity is $U$, it will trigger turbulence if $U d / \nu=850$, where $d$ is the wire diameter [Ref. 3 of Ch. 6]. If the sphere diameter is 20 cm and transition is observed at $\operatorname{Re} D=90,000$, what is the


Fig. P6.5 diameter of the trip wire in mm ?

Solution: For the same U and $v$,

$$
\begin{aligned}
& \operatorname{Re}_{d}=\frac{U d}{v}=850 ; \quad \operatorname{Re}_{D}=\frac{U D}{v}=90000 \\
& \text { or } \quad d=D \frac{\operatorname{Re}_{d}}{\operatorname{Re}_{D}}=(200 \mathrm{~mm})\left(\frac{850}{90000}\right) \approx \mathbf{1 . 9} \mathbf{~ m m}
\end{aligned}
$$

P6.6 For flow of a uniform stream parallel to a sharp flat plate, transition to a turbulent boundary layer on the plate may occur at $\mathrm{Re}_{x}=\rho U x / \mu \approx 1 \mathrm{E} 6$, where $U$ is the approach velocity and $x$ is distance along the plate. If $U=2.5 \mathrm{~m} / \mathrm{s}$, determine the distance $x$ for the following fluids at $20^{\circ} \mathrm{C}$ and 1 atm : (a) hydrogen; (b) air; (c) gasoline; (d) water; (e) mercury; and $(f)$ glycerin.

Solution: We are to calculate $x=\left(\operatorname{Re}_{x}\right)(\mu) /(\rho U)=(1 \mathrm{E} 6)(\mu) /[\rho(2.5 \mathrm{~m} / \mathrm{s})]$. Make a table:

| FLUID | $\rho-\mathrm{kg} / \mathrm{m}^{3}$ | $\mu-\mathrm{kg} / \mathrm{m}-\mathrm{s}$ | $x-$ meters |
| :---: | :---: | :---: | :---: |
| Hydrogen | 0.00839 | $9.05 \mathrm{E}-5$ | 43. |
| Air | 1.205 | $1.80 \mathrm{E}-5$ | 6.0 |
| Gasoline | 680 | $2.92 \mathrm{E}-4$ | 0.17 |
| Water | 998 | 0.0010 | 0.40 |


| Mercury | 13,550 | $1.56 \mathrm{E}-3$ | 0.046 |
| :---: | :---: | :---: | :---: |
| Glycerin | 1260 | 1.49 | 470. |

Clearly there are vast differences between fluid properties and their effects on flows.
6.7 Cola, approximated as pure water at $20^{\circ} \mathrm{C}$, is to fill an $8-\mathrm{oz}$ container (1 U.S. gal $=$ 128 fl oz ) through a $5-\mathrm{mm}$-diameter tube. Estimate the minimum filling time if the tube flow is to remain laminar. For what cola (water) temperature would this minimum time be 1 min ?

Solution: For cola "water", take $\rho=998 \mathrm{~kg} / \mathrm{m}^{3}$ and $\mu=0.001 \mathrm{~kg} / \mathrm{m} \cdot \mathrm{s}$. Convert 8 fluid ounces $=(8 / 128)\left(231 \mathrm{in}^{3}\right) \approx 2.37 \mathrm{E}-4 \mathrm{~m}^{3}$. Then, if we assume transition at $\mathrm{Re}=2300$,

$$
\operatorname{Re}_{\text {crit }}=2300=\frac{\rho \mathrm{VD}}{\mu}=\frac{4 \rho \mathrm{Q}}{\pi \mu \mathrm{D}}, \quad \text { or: } \quad \mathrm{Q}_{\text {crit }}=\frac{2300 \pi(0.001)(0.005)}{4(998)} \approx 9.05 \mathrm{E}-6 \frac{\mathrm{~m}^{3}}{\mathrm{~s}}
$$

Then $\Delta \mathrm{t}$ fill $=v / \mathrm{Q}=2.37 \mathrm{E}-4 / 9.05 \mathrm{E}-6 \approx \mathbf{2 6} \mathbf{s}$ Ans. (a)
(b) We fill in exactly one minute if $\mathrm{Q}_{\text {crit }}=2.37 \mathrm{E}-4 / 60=3.94 \mathrm{E}-6 \mathrm{~m}^{3} / \mathrm{s}$. Then

$$
\mathrm{Q}_{\text {crit }}=3.94 \mathrm{E}-6 \frac{\mathrm{~m}^{3}}{\mathrm{~s}}=\frac{2300 \pi \nu \mathrm{D}}{4} \text { if } v_{\text {water }} \approx 4.36 \mathrm{E}-7 \mathrm{~m}^{2} / \mathrm{s}
$$

From Table A-1, this kinematic viscosity occurs at $\mathbf{T} \approx \mathbf{6 6}^{\circ} \mathbf{C}$ Ans. (b)
6.8 When water at $20^{\circ} \mathrm{C}\left(\rho=998 \mathrm{~kg} / \mathrm{m}^{3}, \mu=0.001 \mathrm{~kg} / \mathrm{m} \cdot \mathrm{s}\right)$ flows through an $8-\mathrm{cm}$ diameter pipe, the wall shear stress is 72 Pa . What is the axial pressure gradient ( $\partial \mathrm{p} / \partial \mathrm{x})$ if the pipe is (a) horizontal; and (b) vertical with the flow $u$ ?
Solution: Equation (6.9b) applies in both cases, noting that $\tau_{\mathrm{w}}$ is negative:
(a) Horizontal: $\frac{d p}{d x}=\frac{2 \tau_{w}}{R}=\frac{2(-72 \mathrm{~Pa})}{0.04 \mathrm{~m}}=-\mathbf{3 6 0 0} \frac{\mathbf{P a}}{\mathbf{m}} \quad$ Ans. (a)
(b) Vertical, up: $\frac{d p}{d x}=\frac{2 \tau_{w}}{R}-\rho g \frac{d z \tau^{1}}{d x}=-3600-998(9.81)=-\mathbf{1 3}, \mathbf{4 0 0} \frac{\mathbf{P a}}{\mathbf{m}} \quad$ Ans. (b)

