

6.75 You wish to water your garden with 100 ft of $\frac{5}{8}$ -in-diameter hose whose roughness is 0.011 in. What will be the delivery, in ft^3/s , if the gage pressure at the faucet is 60 lb/in^2 ? If there is no nozzle (just an open hose exit), what is the maximum horizontal distance the exit jet will carry?

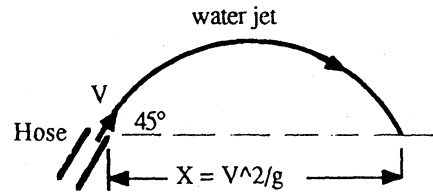


Fig. P6.75

Solution: For water, take $\rho = 1.94 \text{ slug}/\text{ft}^3$ and $\mu = 2.09\text{E-}5 \text{ slug}/\text{ft}\cdot\text{s}$. We are given $\epsilon/d = 0.011/(5/8) \approx 0.0176$. For constant area hose, $V_1 = V_2$ and energy yields

$$\frac{P_{\text{faucet}}}{\rho g} = h_f, \quad \text{or:} \quad \frac{60 \times 144 \text{ psf}}{1.94(32.2)} = 138 \text{ ft} = f \frac{L}{d} \frac{V^2}{2g} = f \frac{100}{(5/8)/12} \frac{V^2}{2(32.2)},$$

$$\text{or } fV^2 \approx 4.64. \quad \text{Guess } f \approx f_{\text{fully rough}} = 0.0463, \quad V \approx 10.0 \frac{\text{ft}}{\text{s}}, \quad \text{Re} \approx 48400$$

$$\text{then } f_{\text{better}} \approx 0.0472, \quad V_{\text{final}} \approx \mathbf{9.91 \text{ ft/s}} \text{ (converged)}$$

$$\text{The hose delivery then is } Q = (\pi/4)(5/8/12)^2(9.91) = \mathbf{0.0211 \text{ ft}^3/\text{s}}. \quad \text{Ans. (a)}$$

From elementary particle-trajectory theory, the maximum horizontal distance X travelled by the jet occurs at $\theta = 45^\circ$ (see figure) and is $X = V^2/g = (9.91)^2/(32.2) \approx \mathbf{3.05 \text{ ft}}$ Ans. (b), which is pitiful. You need a *nozzle* on the hose to increase the exit velocity.

6.76 The small turbine in Fig. P6.76 extracts 400 W of power from the water flow. Both pipes are wrought iron. Compute the flow rate $Q \text{ m}^3/\text{h}$. Sketch the EGL and HGL accurately.

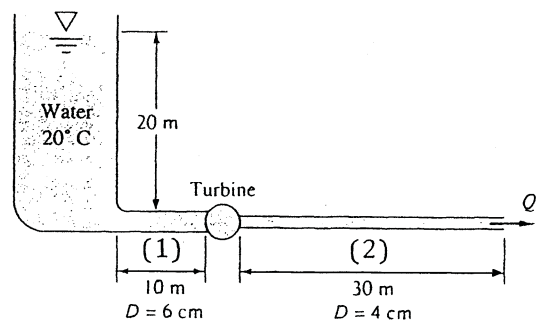


Fig. P6.76

Solution: For water, take $\rho = 998 \text{ kg}/\text{m}^3$ and $\mu = 0.001 \text{ kg}/\text{m}\cdot\text{s}$. For wrought iron, take $\epsilon \approx 0.046 \text{ mm}$, hence $\epsilon/d_1 = 0.046/60 \approx 0.000767$ and $\epsilon/d_2 = 0.046/40 \approx 0.00115$. The energy equation, with $V_1 \approx 0$ and $p_1 = p_2$, gives

$$z_1 - z_2 = 20 \text{ m} = \frac{V_2^2}{2g} + h_{f2} + h_{f1} + h_{\text{turbine}}, \quad h_{f1} = f_1 \frac{L_1}{d_1} \frac{V_1^2}{2g} \quad \text{and} \quad h_{f2} = f_2 \frac{L_2}{d_2} \frac{V_2^2}{2g}$$

$$\text{Also, } h_{\text{turbine}} = \frac{P}{\rho g Q} = \frac{400 \text{ W}}{998(9.81)Q} \quad \text{and} \quad Q = \frac{\pi}{4} d_1^2 V_1 = \frac{\pi}{4} d_2^2 V_2$$