

# ENSC 388 Quiz #2

Oct. 7, 2009

Name: ..... Student ID:.....

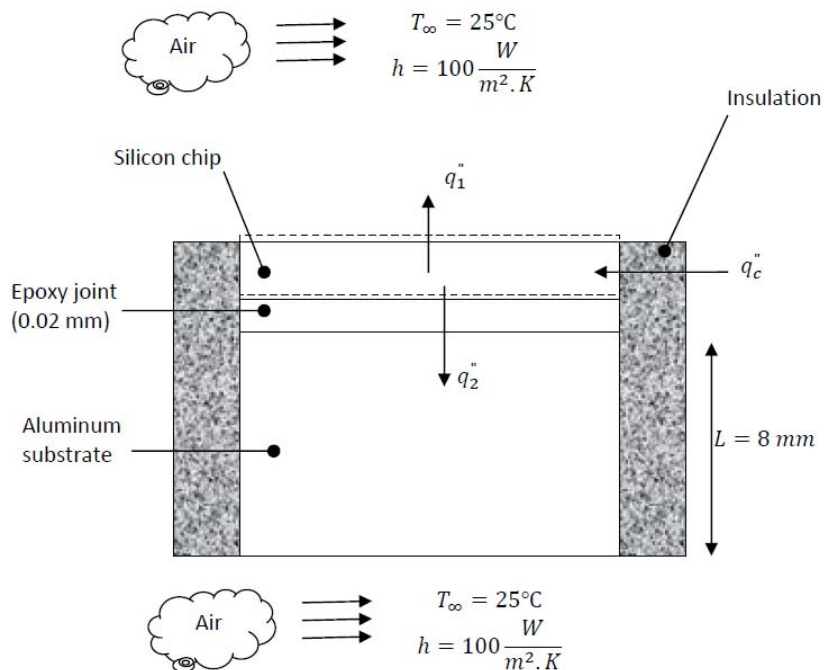
Time: 45 minutes or less. Develop answers on available place. The quiz has 5% (bonus) of the total mark. Closed books & closed notes.

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## Problem 1 (50%):

A thin silicon chip and an 8-mm-thick aluminum substrate are separated by a 0.02-mm thick epoxy joint. The chip and substrate are each 10 mm on a side, and their exposed surfaces are cooled by air, which is at a temperature of 25°C and provides a convection coefficient of 100 W/m<sup>2</sup>·K. If the chip dissipates 10<sup>4</sup> W/m<sup>2</sup> under normal conditions, will it operate below a maximum allowable temperature of 85°C?

Note: the thermal resistant at the interface between the silicon chip and the aluminum plate with 0.02-mm epoxy is:  $R_{t,c} = 0.9 \times 10^{-4} \text{ m}^2\text{K}/\text{W}$



Pure aluminum ( $T \sim 350 \text{ K}$ ):  $k = 239 \text{ W/m} \cdot \text{K}$

**Problem 2 (50%):**

Consider a 0.6m ×0.6m thin square plate in a room at 30°C. One side of the plate is maintained at a temperature of 90°C, while the other side is insulated. Determine the rate of heat transfer by natural convection from the plate if the plate is: a) vertical, b) horizontal with hot surface up, and c) horizontal with hot surface facing down.

Use the following properties for air at the film temperature:

$$k = 0.02808 \text{ W/mK}, \text{ Pr} = 0.7202, \text{ and } \nu = 1.896 \times 10^{-5} \text{ m}^2/\text{s}.$$

Also:

$$Ra_L = \frac{g\beta(T_s - T_\infty)L^3}{\nu^2} \text{ Pr}$$

**Problem 1:***Known:*

Dimensions, heat dissipation, and maximum allowable temperature of a silicon chip. Thickness of aluminum substrate and epoxy joint. Convection conditions at exposed chip and substrate surfaces.

*Find:*

- Whether maximum allowable temperature is exceeded.

**Assumptions:**

1. Steady-state conditions.
2. One-dimensional conduction (negligible heat transfer from sides of composite).
3. Negligible chip thermal resistance (an isothermal chip).
4. Constant properties.
5. Negligible radiation exchange with surroundings.

**Properties:**

Pure aluminum ( $T \sim 350$  K):  $k = 239$  W/m·K (Table A-24).

**Analysis:**

Heat dissipated in the chip is transferred to the air directly from the exposed surface and indirectly through the joint and substrate. Performing an energy balance on a control surface about the chip, it follows that, on the basis of a unit surface area,

$$q_c'' = q_1'' + q_2''$$

Or

$$q_c'' = \frac{T_c - T_\infty}{(1/h)} + \frac{T_c - T_\infty}{R_{t,c}'' + (L/k) + (1/h)}$$

To conservatively estimate  $T_c$ , the maximum possible value of  $R_{t,c}'' = 0.9 \times 10^{-4}$  m<sup>2</sup>·K/W is obtained from Table. Hence

$$T_c = T_\infty + q_c'' \left[ h + \frac{1}{R_{t,c}'' + (L/k) + (1/h)} \right]^{-1}$$

Or

$$T_c = 25^\circ\text{C} + \frac{10^4 \text{ W}}{\text{m}^2} \times \left[ 100 + \frac{1}{(0.9 + 0.34 + 100) \times 10^{-4}} \right]^{-1} \text{ m}^2 \cdot \text{K/W}$$

$$T_c = 25^\circ\text{C} + 50.3^\circ\text{C} = 75.3^\circ\text{C}$$

Hence the chip will operate below its maximum allowable temperature.

**Problem 2:**

See Example 14-2, page 623, Cengel book.