

14-72 The absorber plate and the glass cover of a flat-plate solar collector are maintained at specified temperatures. The rate of heat loss from the absorber plate by natural convection is to be determined.

Assumptions 1 Steady operating conditions exist. 2 Air is an ideal gas with constant properties. 3 Heat loss by radiation is negligible. 4 The air pressure in the enclosure is 1 atm.

Properties The properties of air at 1 atm and the average temperature of $(T_1 + T_2)/2 = (80 + 40)/2 = 60^\circ\text{C}$ are (Table A-22)

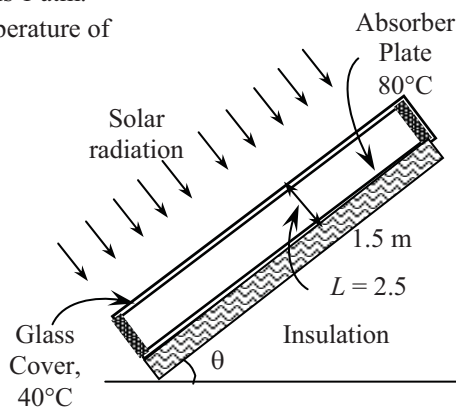
$$k = 0.02808 \text{ W/m}\cdot^\circ\text{C}$$

$$\nu = 1.896 \times 10^{-5} \text{ m}^2/\text{s}$$

$$\text{Pr} = 0.7202$$

$$\beta = \frac{1}{T_f} = \frac{1}{(60 + 273)\text{K}} = 0.003003 \text{ K}^{-1}$$

Analysis For $\theta = 0^\circ$, we have horizontal rectangular enclosure. The characteristic length in this case is the distance between the two glasses $L_c = L = 0.025 \text{ m}$. Then,



$$\text{Ra} = \frac{g\beta(T_1 - T_2)L^3}{\nu^2} \text{Pr} = \frac{(9.81 \text{ m/s}^2)(0.003003 \text{ K}^{-1})(80 - 40 \text{ K})(0.025 \text{ m})^3}{(1.896 \times 10^{-5} \text{ m}^2/\text{s})^2} (0.7202) = 3.689 \times 10^4$$

$$\begin{aligned} \text{Nu} &= 1 + 1.44 \left[1 - \frac{1708}{\text{Ra}} \right]^+ + \left[\frac{\text{Ra}^{1/3}}{18} - 1 \right]^+ \\ &= 1 + 1.44 \left[1 - \frac{1708}{3.689 \times 10^4} \right]^+ + \left[\frac{(3.689 \times 10^4)^{1/3}}{18} - 1 \right]^+ = 3.223 \end{aligned}$$

Then

$$A_s = H \times W = (1.5 \text{ m})(3 \text{ m}) = 4.5 \text{ m}^2$$

$$\dot{Q} = k\text{Nu}A_s \frac{T_1 - T_2}{L} = (0.02808 \text{ W/m}\cdot^\circ\text{C})(3.223)(4.5 \text{ m}^2) \frac{(80 - 40)^\circ\text{C}}{0.025 \text{ m}} = \mathbf{652 \text{ W}}$$

For $\theta = 30^\circ$, we obtain

$$\begin{aligned} \text{Nu} &= 1 + 1.44 \left[1 - \frac{1708}{\text{Ra} \cos \theta} \right]^+ + \left[\frac{1708(\sin 1.8\theta)^{1.6}}{\text{Ra} \cos \theta} \right]^+ + \left[\frac{(\text{Ra} \cos \theta)^{1/3}}{18} - 1 \right]^+ \\ &= 1 + 1.44 \left[1 - \frac{1708}{(3.689 \times 10^4) \cos(30)} \right]^+ + \left[\frac{1708[\sin(1.8 \times 30)]^{1.6}}{(3.689 \times 10^4) \cos(30)} \right]^+ + \left[\frac{[(3.689 \times 10^4) \cos(30)]^{1/3}}{18} - 1 \right]^+ \\ &= 3.074 \end{aligned}$$

$$\dot{Q} = k\text{Nu}A_s \frac{T_1 - T_2}{L} = (0.02808 \text{ W/m}\cdot^\circ\text{C})(3.074)(4.5 \text{ m}^2) \frac{(80 - 40)^\circ\text{C}}{0.025 \text{ m}} = \mathbf{621 \text{ W}}$$

For $\theta = 90^\circ$, we have vertical rectangular enclosure. The Nusselt number for this geometry and orientation can be determined from $(\text{Ra} = 3.689 \times 10^4)$ - same as that for horizontal case)

$$\text{Nu} = 0.42\text{Ra}^{1/4} \text{Pr}^{0.012} \left(\frac{H}{L} \right)^{-0.3} = 0.42(3.689 \times 10^4)^{1/4} (0.7202)^{0.012} \left(\frac{2 \text{ m}}{0.025 \text{ m}} \right)^{-0.3} = 1.557$$

$$\dot{Q} = k\text{Nu}A_s \frac{T_1 - T_2}{L} = (0.02808 \text{ W/m}\cdot^\circ\text{C})(1.557)(4.5 \text{ m}^2) \frac{(80 - 40)^\circ\text{C}}{0.025 \text{ m}} = \mathbf{315 \text{ W}}$$

Discussion Caution is advised for the vertical case since the condition $H/L < 40$ is not satisfied.