5-46 R-134a contained in a spring-loaded piston-cylinder device is cooled until the temperature and volume drop to specified values. The heat transfer and the work done are to be determined.

Assumptions **1** The cylinder is stationary and thus the kinetic and potential energy changes are zero. **2** There are no work interactions involved other than the boundary work. **3** The thermal energy stored in the cylinder itself is negligible. **4** The compression or expansion process is quasi-equilibrium.

Analysis We take the contents of the cylinder as the system. This is a closed system since no mass enters or leaves. The energy balance for this stationary closed system can be expressed as

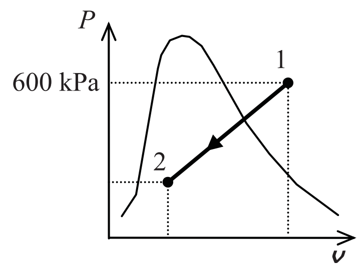
$$\underbrace{E_{\text{in}} - E_{\text{out}}}_{\substack{\text{Net energy transfer}\\ \text{by heat, work, and mass}}} = \underbrace{\Delta E_{\text{system}}}_{\substack{\text{Change in internal, kinetic,}\\ \text{potential, etc. energies}}}$$

$$W_{b,\text{in}} - Q_{\text{out}} = \Delta U = m(u_2 - u_1) \quad \text{(since KE = PE = 0)}$$

$$Q_{\text{out}} = W_{b,\text{in}} - m(u_2 - u_1)$$

The initial state properties are (Table A-13)

$$\left.\begin{array}{l} P_1 = 600 \text{ kPa} \\ T_1 = 15°\text{C} \end{array}\right\} \begin{array}{l} v_1 = 0.055522 \text{ m}^3/\text{kg} \\ u_1 = 357.96 \text{ kJ/kg} \end{array}$$



The mass of refrigerant is

$$m = \frac{V_1}{v_1} = \frac{0.3 \text{ m}^3}{0.055522 \text{ m}^3/\text{kg}} = 5.4033 \text{ kg}$$

The final specific volume is

$$v_2 = \frac{V_2}{m} = \frac{0.1 \text{ m}^3}{5.4033 \text{ kg}} = 0.018507 \text{ m}^3/\text{kg}$$

The final state at this specific volume and at -30°C is a saturated mixture. The properties at this state are (Table A-11)

$$x_2 = \frac{v_2 - v_f}{v_g - v_f} = \frac{0.018507 - 0.0007203}{0.22580 - 0.0007203} = 0.079024$$

$$u_2 = u_f + x_2 u_{fg} = 12.59 + (0.079024)(200.52) = 28.44 \text{ kJ/kg}$$

$$P_2 = 84.43 \text{ kPa}$$

Since this is a linear process, the work done is equal to the area under the process line 1-2:

$$W_{b,\text{in}} = \text{Area} = \frac{P_1 + P_2}{2}(V_1 - V_2) = \frac{(600 + 84.43)\text{kPa}}{2}(0.3 - 0.1)\text{m}^3 \left(\frac{1 \text{ kJ}}{1 \text{ kPa} \cdot \text{m}^3}\right) = \mathbf{68.44 \text{ kJ}}$$

Substituting into energy balance equation gives

$$Q_{\text{out}} = W_{b,\text{in}} - m(u_2 - u_1) = 68.44 \text{ kJ} - (5.4033 \text{ kg})(28.44 - 357.96) \text{ kJ/kg} = \mathbf{1849 \text{ kJ}}$$