

**5-67** A student living in a room turns her 150-W fan on in the morning. The temperature in the room when she comes back 10 h later is to be determined.

**Assumptions 1** Air is an ideal gas since it is at a high temperature and low pressure relative to its critical point values of  $-141^{\circ}\text{C}$  and  $3.77\text{ MPa}$ . **2** The kinetic and potential energy changes are negligible,  $\Delta ke \cong \Delta pe \cong 0$ . **3** Constant specific heats at room temperature can be used for air. This assumption results in negligible error in heating and air-conditioning applications. **4** All the doors and windows are tightly closed, and heat transfer through the walls and the windows is disregarded.

**Properties** The gas constant of air is  $R = 0.287\text{ kPa}\cdot\text{m}^3/\text{kg}\cdot\text{K}$  (Table A-1). Also,  $c_v = 0.718\text{ kJ}/\text{kg}\cdot\text{K}$  for air at room temperature (Table A-2).

**Analysis** We take the room as the system. This is a *closed system* since the doors and the windows are said to be tightly closed, and thus no mass crosses the system boundary during the process. The energy balance for this system can be expressed as

$$\underbrace{E_{in} - E_{out}}_{\substack{\text{Net energy transfer} \\ \text{by heat, work, and mass}}} = \underbrace{\Delta E_{\text{system}}}_{\substack{\text{Change in internal, kinetic,} \\ \text{potential, etc. energies}}}$$

$$W_{e,in} = \Delta U$$

$$W_{e,in} = m(u_2 - u_1) \cong mc_v(T_2 - T_1)$$

The mass of air is

$$\mathcal{V} = 4 \times 6 \times 6 = 144\text{ m}^3$$

$$m = \frac{P_1 \mathcal{V}}{RT_1} = \frac{(100\text{ kPa})(144\text{ m}^3)}{(0.287\text{ kPa}\cdot\text{m}^3/\text{kg}\cdot\text{K})(288\text{ K})} = 174.2\text{ kg}$$

The electrical work done by the fan is

$$W_e = \dot{W}_e \Delta t = (0.15\text{ kJ/s})(10 \times 3600\text{ s}) = 5400\text{ kJ}$$

Substituting and using the  $c_v$  value at room temperature,

$$5400\text{ kJ} = (174.2\text{ kg})(0.718\text{ kJ}/\text{kg}\cdot^{\circ}\text{C})(T_2 - 15)^{\circ}\text{C}$$

$$T_2 = \mathbf{58.2^{\circ}\text{C}}$$

**Discussion** Note that a fan actually causes the internal temperature of a confined space to rise. In fact, a 100-W fan supplies a room with as much energy as a 100-W resistance heater.

