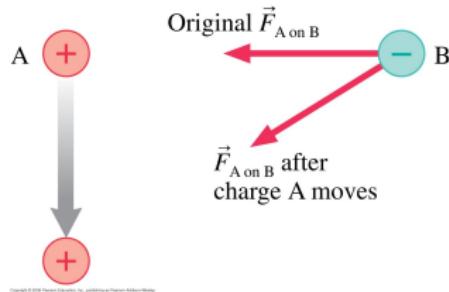


The Field Model (26.5)

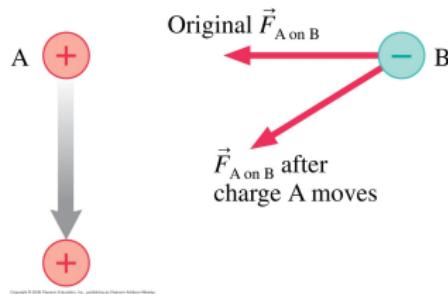
- How does the electric force get propagated from one particle to another?



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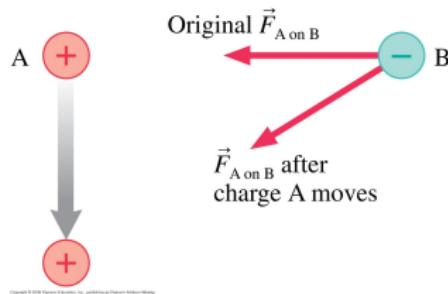
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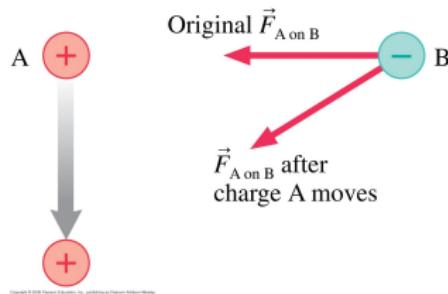
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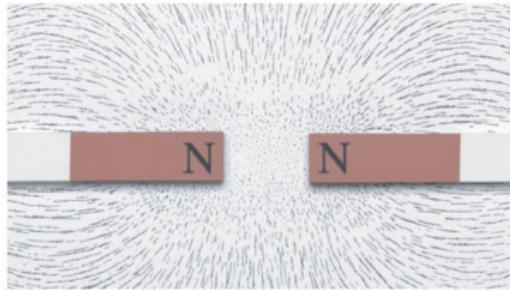
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- How does the electric force get propagated from one particle to another?
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- Instantaneous action at a distance is a bit hard to believe!
- What if the two particles below were 100 light-years apart??



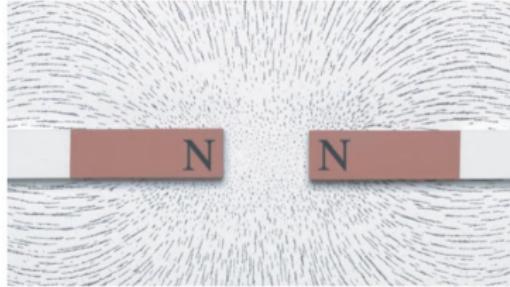
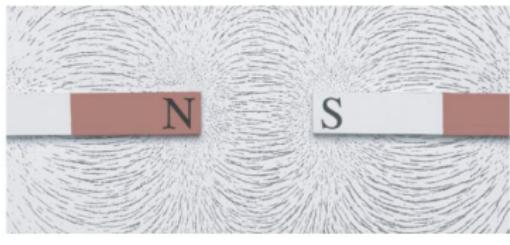
The Field Concept

- Faraday suggested that the space around a charged object was altered. Other charges then interacted with that altered space.



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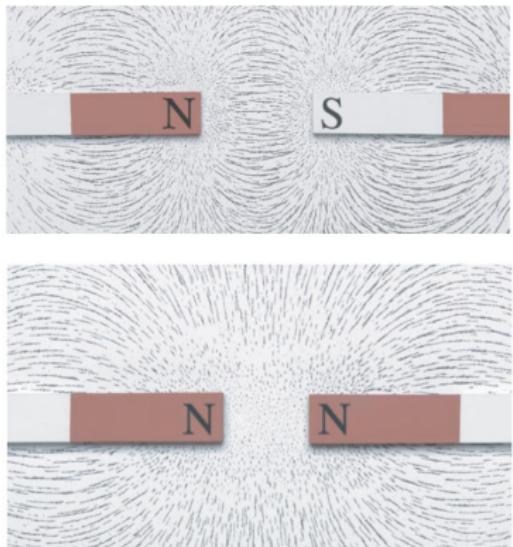
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- Faraday suggested that the space around a charged object was altered. Other charges then interacted with that altered space.
- The iron filings were reacting to the altered space close to the magnet...they were reacting to the magnetic field.

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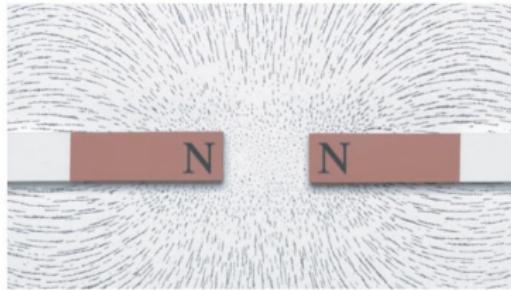
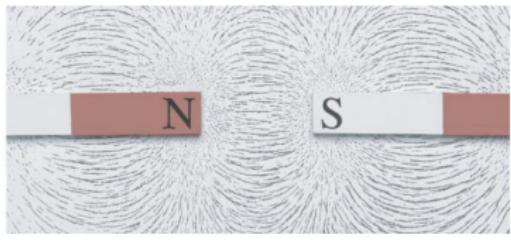
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- The iron filings were reacting to the altered space close to the magnet...they were reacting to the magnetic field.
- The field exists everywhere in space. Electric fields, magnetic fields, gravitational fields are some examples.
- We talked about light being a “self-sustaining oscillation of the EM field”

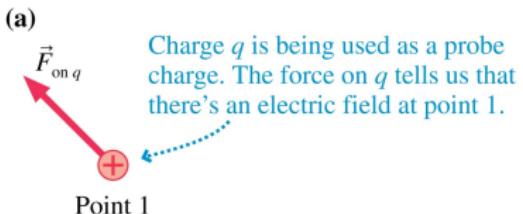
The Electric Field: video

The video shown in today's class can be found at

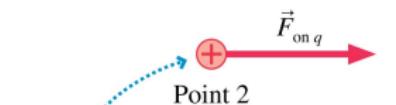
<http://www.learner.org/resources/series42.html>

it is episode 29.

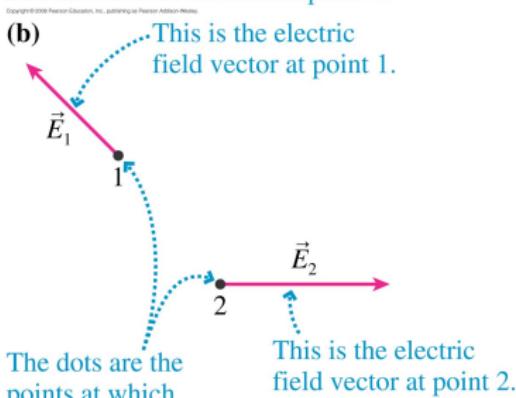
The Electric Field



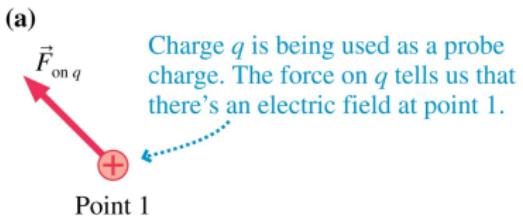
- We will describe a **field model** of electric interactions.



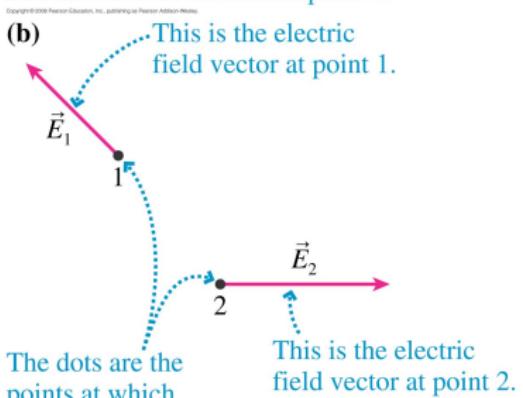
Now charge q is placed at point 2. There's also an electric field here that differs from the field at point 1.



The Electric Field

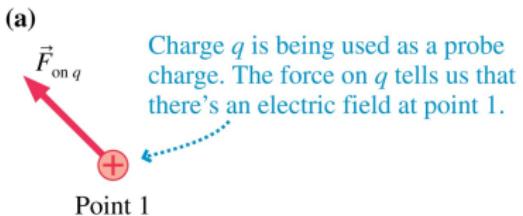


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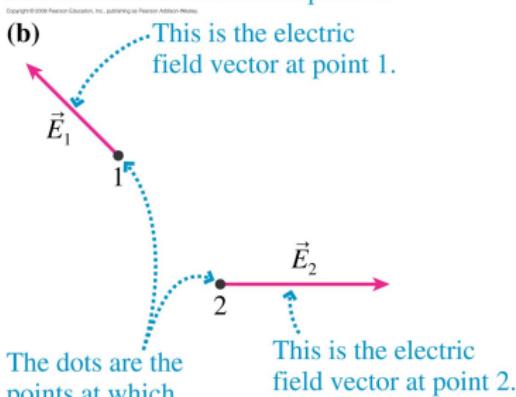


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- Source charges alter the space around them creating an electric field \vec{E}

The Electric Field

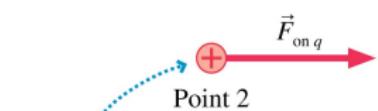
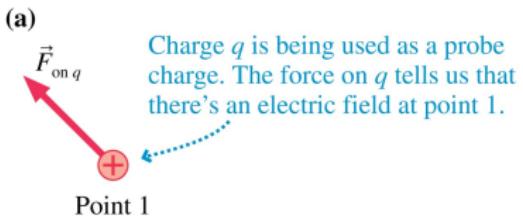


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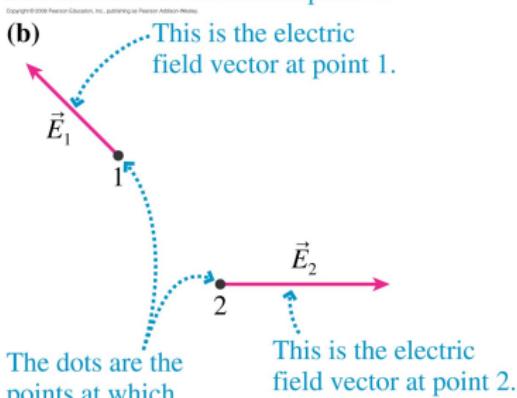


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- A separate charge placed in the field experiences a force \vec{F} **exerted on it by the field**.

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- We will describe a **field model** of electric interactions.
- Source charges alter the space around them creating an electric field \vec{E}
- A separate charge placed in the field experiences a force \vec{F} **exerted on it by the field**.
- The field is defined as

$$\vec{E}(x, y, z) \equiv \frac{\vec{F}_{\text{on } q \text{ at } (x, y, z)}}{q}$$

The magnitude of the field is known as the **electric field strength**.

The Electric Field

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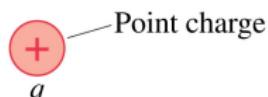
- Often we want to calculate the force on a test charge like

$$\vec{F}_{\text{on } q} = q \vec{E}$$

The Electric Field of a Point Charge

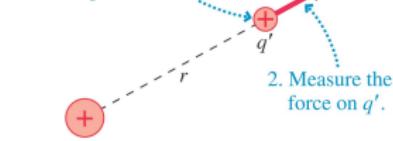
(a)

What is the electric field of q at this point?



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(b) 1. Place q' at the point to probe the field.



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(c)



3. The electric field is
 $\vec{E} = \vec{F}_{\text{on } q'}/q'$
It is a vector in the direction of $\vec{F}_{\text{on } q'}$.

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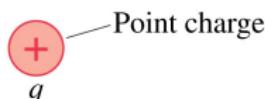
- Assuming both charges are positive, q' will be repelled from q according to Coulomb's Law

$$F_{\text{on } q'} = \frac{1}{4\pi\epsilon_0} \frac{qq'}{r^2}$$

The Electric Field of a Point Charge

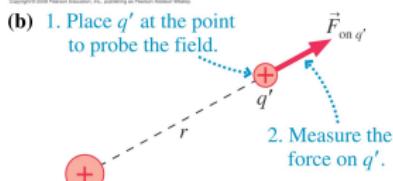
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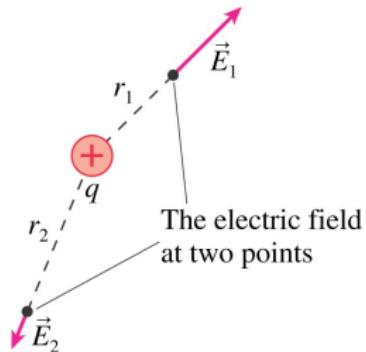
- So, the electric field is pointing away from q as well and is:

$$E(x, y, z) = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

These equations represent the **magnitudes** of the electric force and electric field respectively.

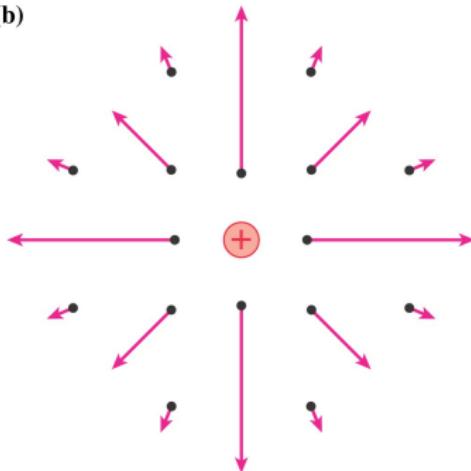
The Electric Field of a Point Charge

(a)



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(b)

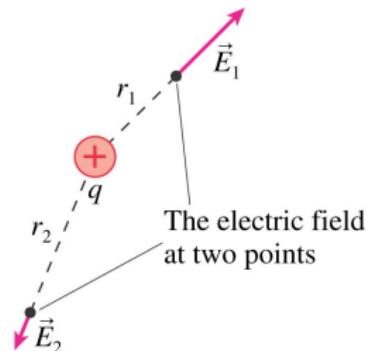


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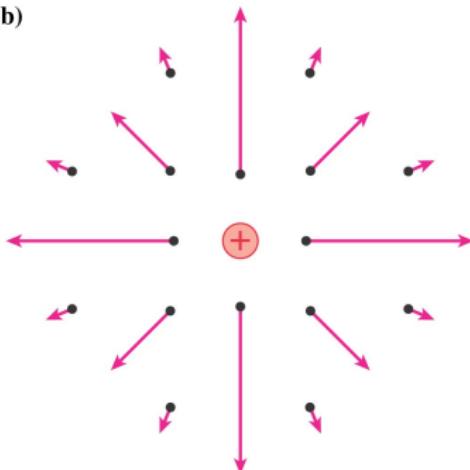
- The field strength goes like $1/r^2$

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(a)



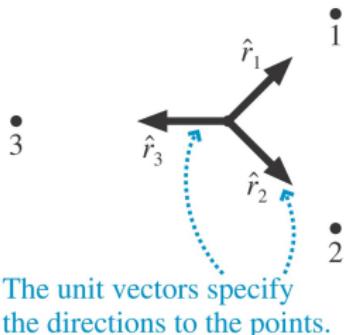
(b)



- The field strength goes like $1/r^2$
- So, if we draw the \vec{E} at each point in space the lengths of the vectors will be very different from each other.

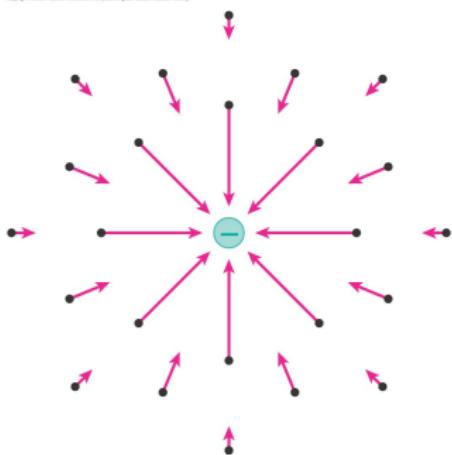
Unit Vector Notation

(a)



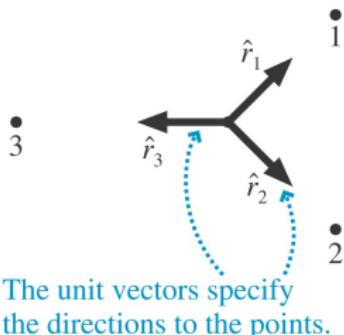
- We need a mathematical way to specify the direction of the field

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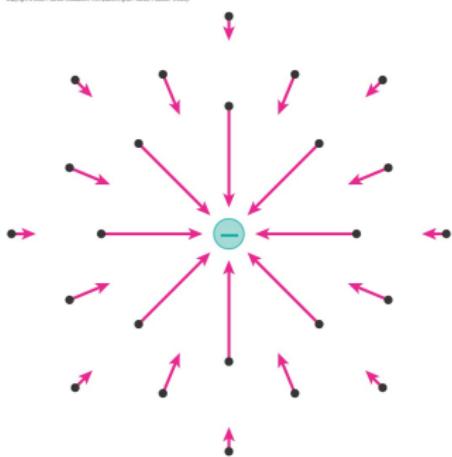
Unit Vector Notation

(a)



- We need a mathematical way to specify the direction of the field
- We will use a **unit vector** in the radial direction

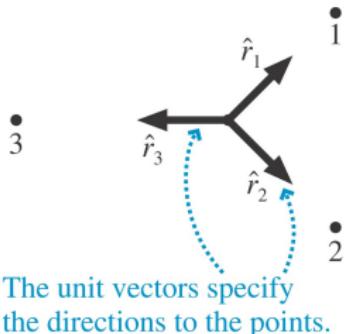
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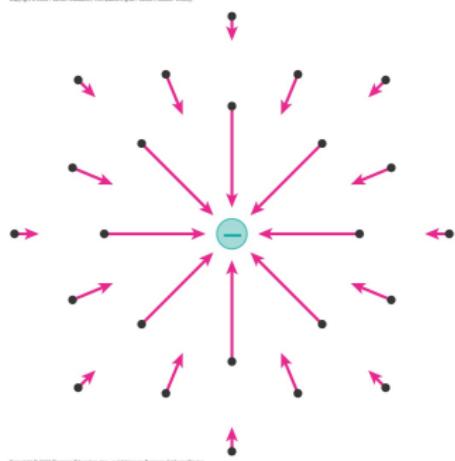
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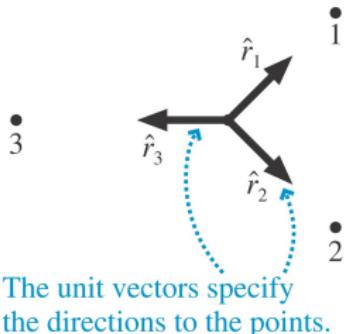
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- Define \hat{r} to be a vector of length 1 from the origin to the point of interest.



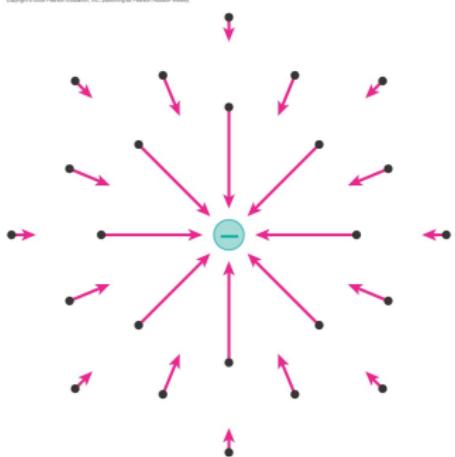
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Unit Vector Notation

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- We need a mathematical way to specify the direction of the field
- We will use a **unit vector** in the radial direction
- Define \hat{r} to be a vector of length 1 from the origin to the point of interest.
- The **vector** electric field can be written as

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$

The Electric Field (Chapter 27)

- Electric fields are everywhere: natural and manipulated.

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- So far we have been drawing electric fields resulting from a single charge. What about complex objects?

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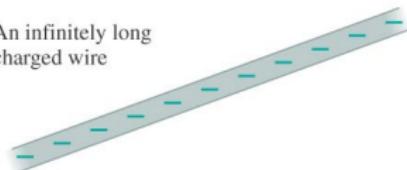
- Electric fields are everywhere: natural and manipulated.
- So far we have been drawing electric fields resulting from a single charge. What about complex objects?
- Chapter 27 is mainly about calculating electric fields from complex objects containing many charges.
- In other words, we will try to calculate realistic electric fields...with some simplifications of course ;-)

Electric Field Models (27.1)

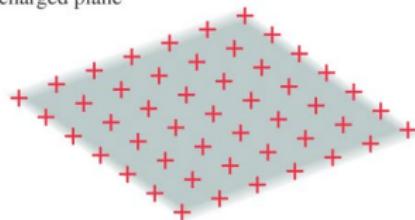
A point charge



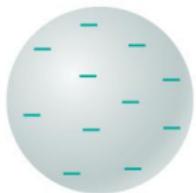
An infinitely long charged wire



An infinitely wide charged plane



A charged sphere



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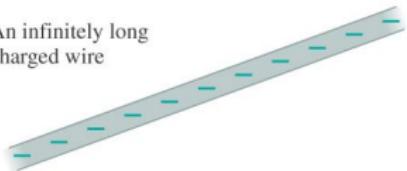
- 1 A point charge
- 2 An infinitely long wire
- 3 An infinitely wide charged plane
- 4 A charged sphere

Electric Field Models

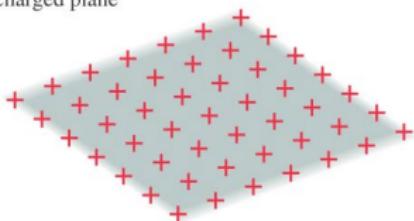
A point charge



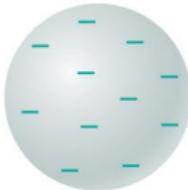
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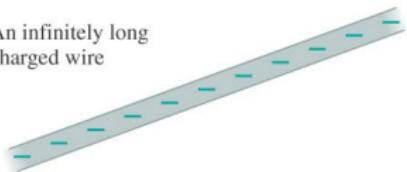
- Small objects (or far-away objects) can often be modeled as points or spheres

Electric Field Models

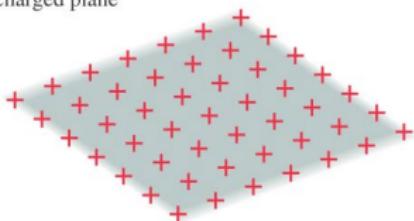
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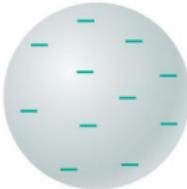
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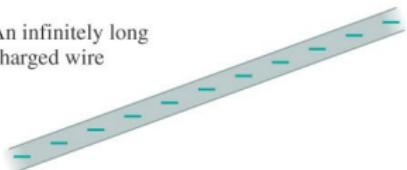
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Electric Field Models

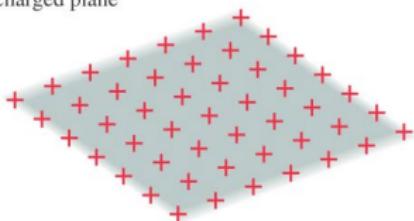
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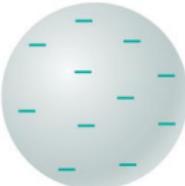
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- Small objects (or far-away objects) can often be modeled as points or spheres
- Wires or planes can be often modeled as infinite, even if they aren't.
- Everything starts from a point:

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$

Point Charges and Superposition

- So, isn't any distribution of charges just a whole bunch of:

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$

?

Point Charges and Superposition

- So, isn't any distribution of charges just a whole bunch of:

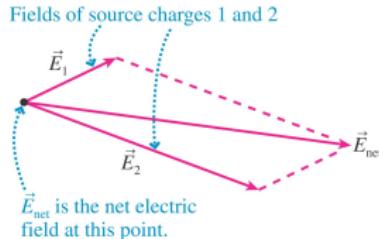
$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$

?

- Actually, yes. As we noted earlier, the electric force obeys the **principle of superposition**

$$\vec{E}_{\text{net}} = \frac{\vec{F}_{\text{on } q}}{q} = \frac{\vec{F}_1 \text{ on } q}{q} + \frac{\vec{F}_2 \text{ on } q}{q} + \dots = \sum_i \vec{E}_i$$

The net electric field is the vector sum of the electric fields due to each charge



Limiting Cases and Typical Field Strength

- Your text emphasizes using limiting cases to get an understanding of the effects of a given charge distribution. A very common thing to do in physics!

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Limiting Cases and Typical Field Strength

- Your text emphasizes using limiting cases to get an understanding of the effects of a given charge distribution. A very common thing to do in physics!
- Limiting cases often allow for a simpler treatment (eg. some terms in equations just disappear) and/or allow the physical picture to be seen more clearly.
- An example: a charge distribution should look like a point charge when viewed from a great distance. If this is not the case, you probably have the wrong description!

The Electric Field of Multiple Point Charges (27.2)

- We already noted that the electric field is a vector field, and superposition is a vector sum.

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$$(E_{net})_x = (E_1)_x + (E_2)_x + \dots = \sum (E_i)_x$$

$$(E_{net})_y = (E_1)_y + (E_2)_y + \dots = \sum (E_i)_y$$

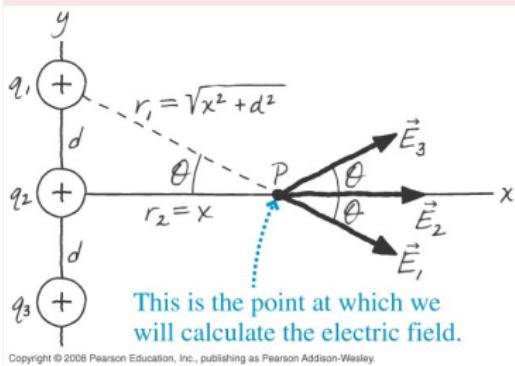
$$(E_{net})_z = (E_1)_z + (E_2)_z + \dots = \sum (E_i)_z$$

- Sometimes it is useful to write this as

$$\vec{E}_{net} = (E_{net})_x \hat{i} + (E_{net})_y \hat{j} + (E_{net})_z \hat{k}$$

Example 27.1: The Electric Field of 3 Equal Point Charges

Example 27.1

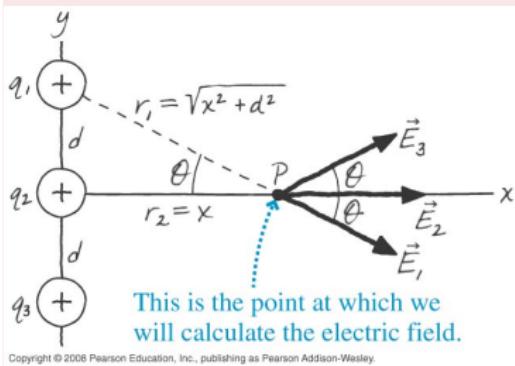


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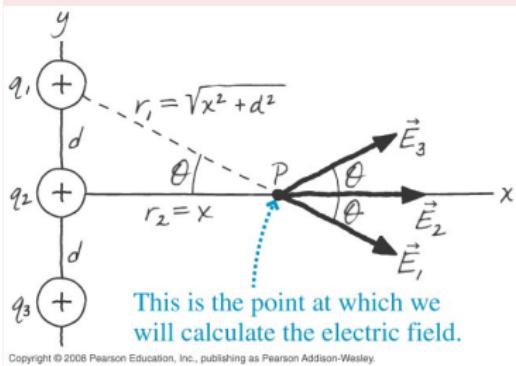


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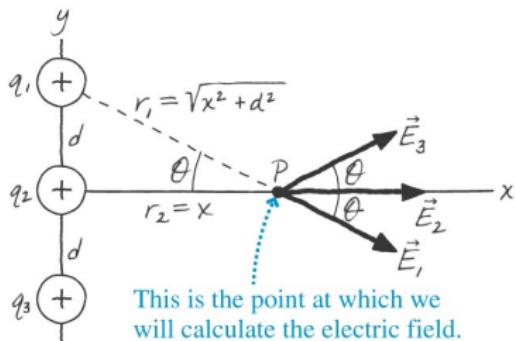


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- There are some clear simplifications - we do not care about the z direction at all. The y components cancel out.
- The x components add like

$$(E_{net})_x = (E_1)_x + (E_2)_x + (E_3)_x = 2(E_1)_x + (E_2)_x$$

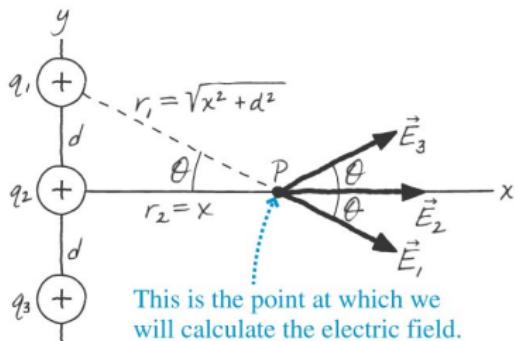
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$$(E_2)_x = E_2 = \frac{1}{4\pi\epsilon_0} \frac{q_2}{x^2}$$

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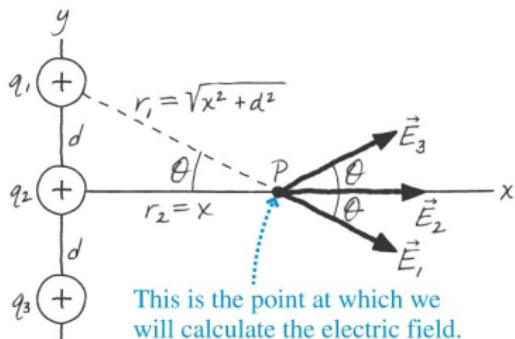
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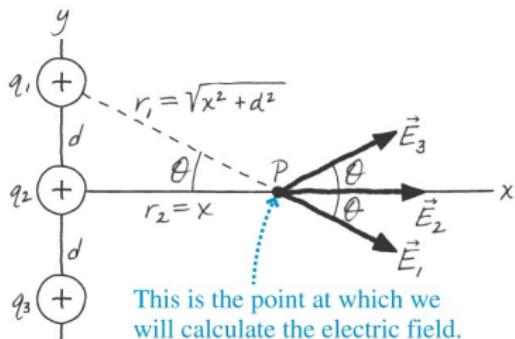
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- But r_1 and θ vary with x . We should express E_1 in terms of x

$$\cos \theta = \frac{x}{r_1} = \frac{x}{(x^2 + d^2)^{1/2}}$$

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This is the point at which we will calculate the electric field.

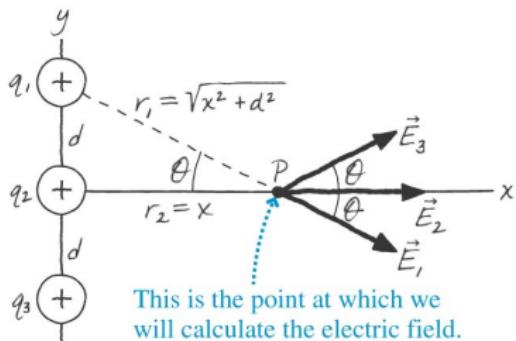
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$$(E_1)_x = \frac{1}{4\pi\epsilon_0} \frac{q}{x^2 + d^2} \frac{x}{(x^2 + d^2)^{1/2}} = \frac{1}{4\pi\epsilon_0} \frac{xq}{(x^2 + d^2)^{3/2}}$$

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Combining the expressions gives

$$(E_{net})_x = 2(E_1)_x + (E_2)_x = \frac{q}{4\pi\epsilon_0} \left[\frac{1}{x^2} + \frac{2x}{(x^2 + d^2)^{3/2}} \right]$$

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$$\vec{E}_{net} = \frac{q}{4\pi\epsilon_0} \left[\frac{1}{x^2} + \frac{2x}{(x^2 + d^2)^{3/2}} \right] \hat{i}$$

- Notice as $x \rightarrow 0$ the second term vanishes

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- Notice as $x \rightarrow 0$ the second term vanishes

$$\vec{E}_{net} = \frac{1}{4\pi\epsilon_0} \frac{q}{x^2} \hat{i}$$

- As x gets very large, d becomes insignificant compared to x .

$$\vec{E}_{net} = \frac{1}{4\pi\epsilon_0} \frac{(3q)}{x^2} \hat{i}$$