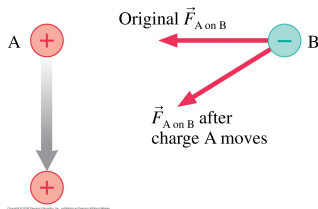


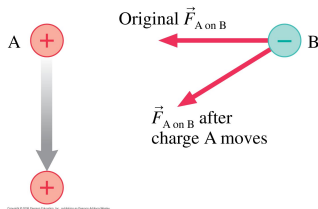
# The Field Model (26.5)

- How does the electric force get propagated from one particle to another?



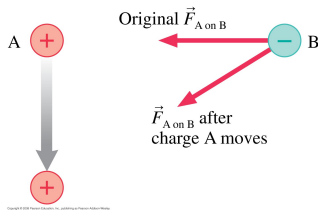
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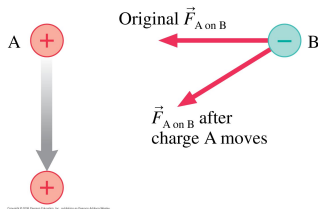
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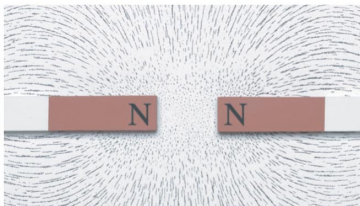
# The Field Model (26.5)

- How does the electric force get propagated from one particle to another?
- Newton's theories were not time-dependent - instantaneous action at a distance
- Instantaneous action at a distance is a bit hard to believe!
- What if the two particles below were 100 light-years apart??



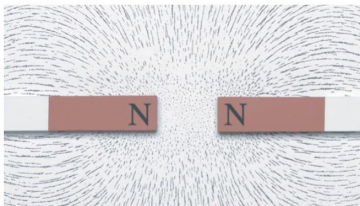
# The Field Concept

- Faraday suggested that the space around a charged object was altered. Other charges then interacted with that altered space.



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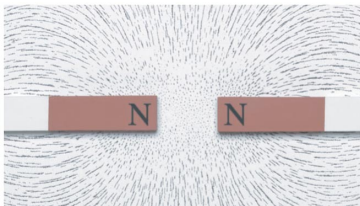
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- Faraday suggested that the space around a charged object was altered. Other charges then interacted with that altered space.
- The iron filings were reacting to the altered space close to the magnet...they were reacting to the magnetic field.

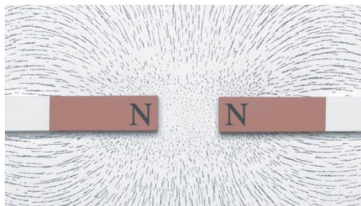
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- Faraday suggested that the space around a charged object was altered. Other charges then interacted with that altered space.
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- The iron filings were reacting to the altered space close to the magnet...they were reacting to the magnetic field.
- The field exists everywhere in space. Electric fields, magnetic fields, gravitational fields are some examples.
- We talked about light being a “self-sustaining oscillation of the EM field”



# The Electric Field: video

The video shown in today's class can be found at  
<http://www.learner.org/resources/series42.html>  
it is episode 29.

# The Electric Field

(a)

$\vec{F}_{\text{on } q}$

Charge  $q$  is being used as a probe charge. The force on  $q$  tells us that there's an electric field at point 1.

Point 1

$\vec{F}_{\text{on } q}$

Point 2

Now charge  $q$  is placed at point 2. There's also an electric field here that differs from the field at point 1.

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(b)

$\vec{E}_1$

1

This is the electric field vector at point 1.

2

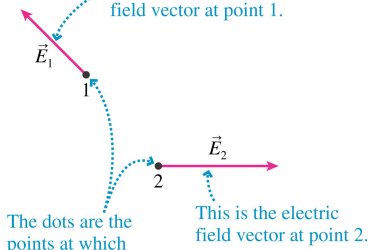
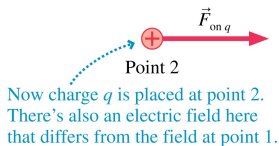
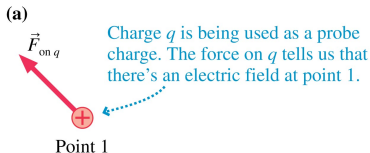
$\vec{E}_2$

The dots are the points at which

This is the electric field vector at point 2.

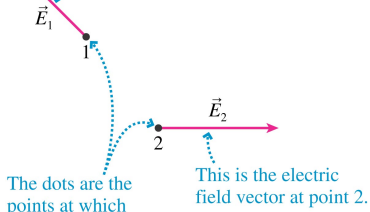
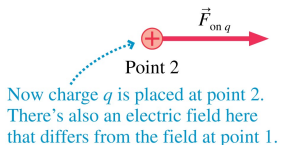
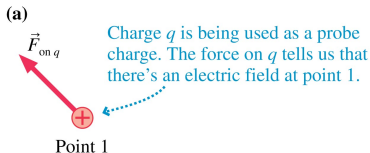
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# The Electric Field



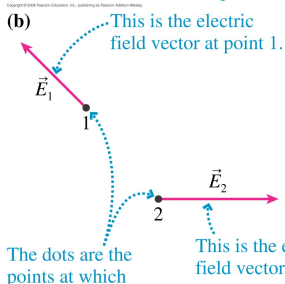
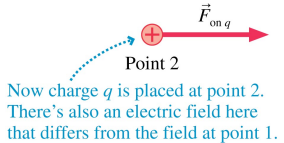
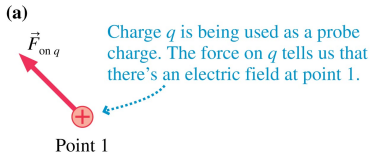
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- We will describe a **field model** of electric interactions.
- Source charges alter the space around them creating an electric field  $\vec{E}$
- A separate charge placed in the field experiences a force  $\vec{F}$  **exerted on it by the field**.
- The field is defined as

$$\vec{E}(x, y, z) \equiv \frac{\vec{F}_{on\ q\ at\ (x, y, z)}}{q}$$

The magnitude of the field is known as the **electric field strength**.

# The Electric Field

- We are using  $q$  as a test-charge or a probe of the field. You can make a field map by moving the charge around.

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- If  $q$  is positive, the electric field vector points in the same direction as the force on the charge.
- The electric field does not depend on the size of  $q$ . There is a  $q$  in both the numerator and denominator of

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which cancel out.

- Often we want to calculate the force on a test charge like

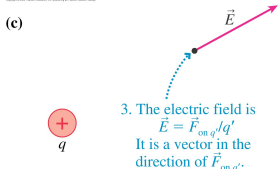
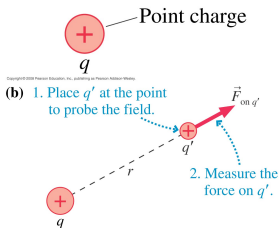
$$\vec{F}_{on\ q} = q\vec{E}$$

# The Electric Field of a Point Charge

(a) What is the electric field of  $q$  at this point?

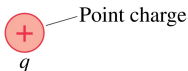
- Assuming both charges are positive,  $q'$  will be repelled from  $q$  according to Coulomb's Law

$$F_{\text{on } q'} = \frac{1}{4\pi\epsilon_0} \frac{qq'}{r^2}$$

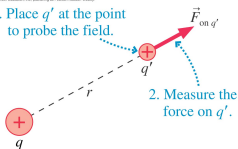


# The Electric Field of a Point Charge

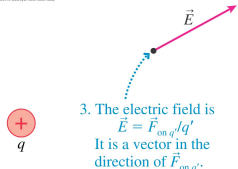
(a) What is the electric field of  $q$  at this point?



(b) 1. Place  $q'$  at the point to probe the field.



(c)



- Assuming both charges are positive,  $q'$  will be repelled from  $q$  according to Coulomb's Law

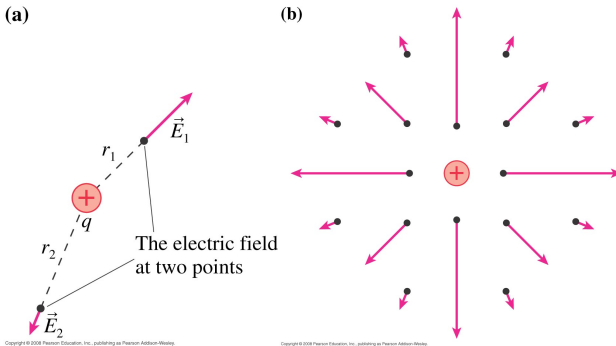
$$F_{on\ q'} = \frac{1}{4\pi\epsilon_0} \frac{qq'}{r^2}$$

- So, the electric field is pointing away from  $q$  as well and is:

$$E(x, y, z) = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

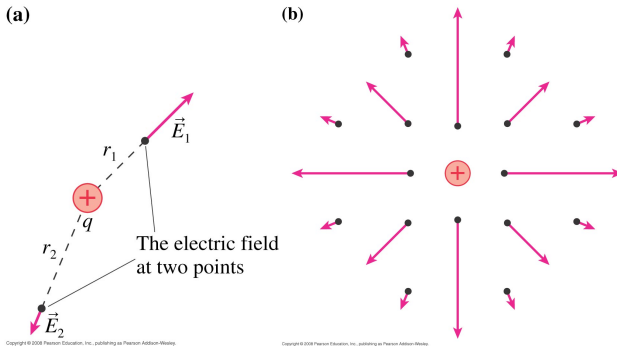
These equations represent the **magnitudes** of the electric force and electric field respectively.

# The Electric Field of a Point Charge



- The field strength goes like  $1/r^2$

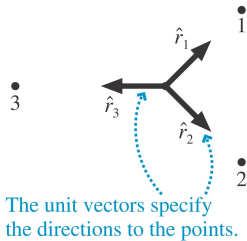
# The Electric Field of a Point Charge



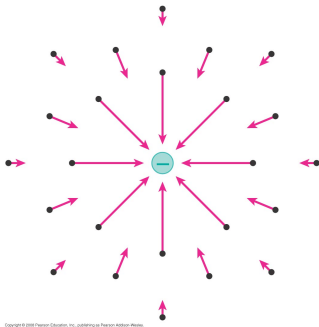
- The field strength goes like  $1/r^2$
- So, if we draw the  $\vec{E}$  at each point in space the lengths of the vectors will be very different from each other.

# Unit Vector Notation

(a)



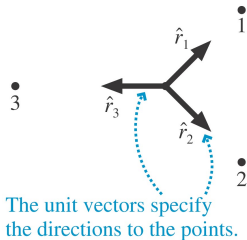
- We need a mathematical way to specify the direction of the field



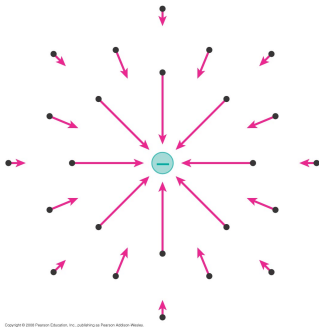


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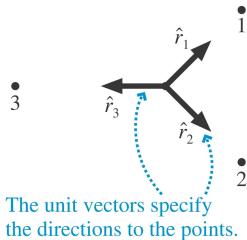


- We need a mathematical way to specify the direction of the field
- We will use a **unit vector** in the radial direction

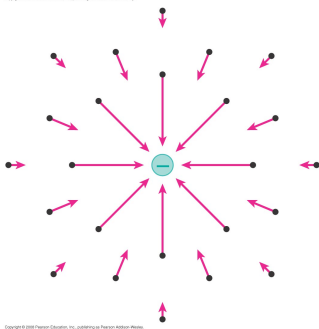


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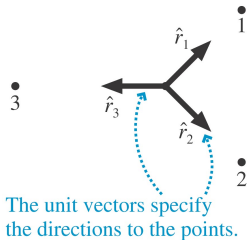


- We need a mathematical way to specify the direction of the field
- We will use a **unit vector** in the radial direction
- Define  $\hat{r}$  to be a vector of length 1 from the origin to the point of interest.



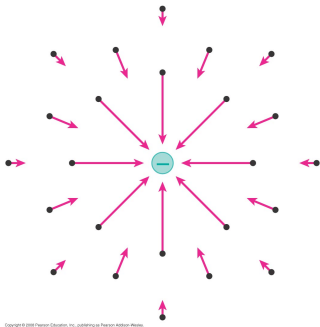
# Unit Vector Notation

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- We need a mathematical way to specify the direction of the field
- We will use a **unit vector** in the radial direction
- Define  $\hat{r}$  to be a vector of length 1 from the origin to the point of interest.
- The **vector** electric field can be written as

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$



# The Electric Field (Chapter 27)

- Electric fields are everywhere: natural and manipulated.

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# The Electric Field (Chapter 27)

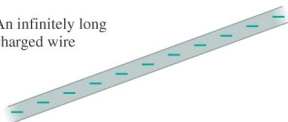
- Electric fields are everywhere: natural and manipulated.
- So far we have been drawing electric fields resulting from a single charge. What about complex objects?
- Chapter 27 is mainly about calculating electric fields from complex objects containing many charges.
- In other words, we will try to calculate realistic electric fields...with some simplifications of course ;-)

# Electric Field Models (27.1)

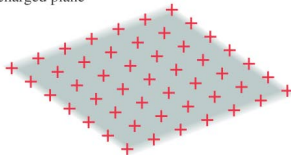
A point charge



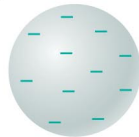
An infinitely long charged wire



An infinitely wide charged plane



A charged sphere



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- 1 A point charge
- 2 An infinitely long wire
- 3 An infinitely wide charged plane
- 4 A charged sphere

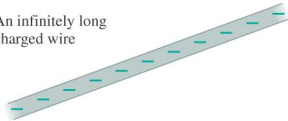


# Electric Field Models

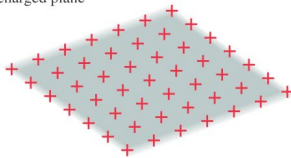
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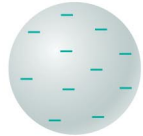
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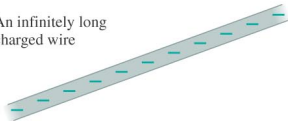
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# Electric Field Models

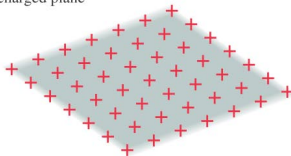
A point charge



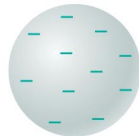
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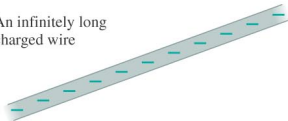
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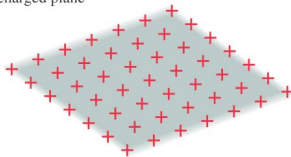
A point charge



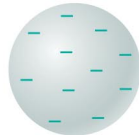
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- Small objects (or far-away objects) can often be modeled as points or spheres
- Wires or planes can be often modeled as infinite, even if they aren't.
- Everything starts from a point:

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$

# Point Charges and Superposition

- So, isn't any distribution of charges just a whole bunch of:

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?

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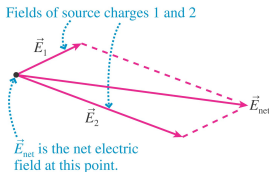
$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$

?

- Actually, yes. As we noted earlier, the electric force obeys the **principle of superposition**

$$\vec{E}_{net} = \frac{\vec{F}_{on\ q}}{q} = \frac{\vec{F}_1\ on\ q}{q} + \frac{\vec{F}_2\ on\ q}{q} + \dots = \sum_i \vec{E}_i$$

**The net electric field is the vector sum of the electric fields due to each charge**



# Limiting Cases and Typical Field Strength

- Your text emphasizes using limiting cases to get an understanding of the effects of a given charge distribution. A very common thing to do in physics!

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# Limiting Cases and Typical Field Strength

- Your text emphasizes using limiting cases to get an understanding of the effects of a given charge distribution. A very common thing to do in physics!
- Limiting cases often allow for a simpler treatment (eg. some terms in equations just disappear) and/or allow the physical picture to be seen more clearly.
- An example: a charge distribution should look like a point charge when viewed from a great distance. If this is not the case, you probably have the wrong description!



# The Electric Field of Multiple Point Charges (27.2)

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$$(E_{net})_x = (E_1)_x + (E_2)_x + \cdots = \sum (E_i)_x$$

$$(E_{net})_y = (E_1)_y + (E_2)_y + \cdots = \sum (E_i)_y$$

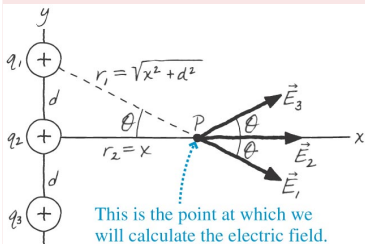
$$(E_{net})_z = (E_1)_z + (E_2)_z + \cdots = \sum (E_i)_z$$

- Sometimes it is useful to write this as

$$\vec{E}_{net} = (E_{net})_x \hat{i} + (E_{net})_y \hat{j} + (E_{net})_z \hat{k}$$

# Example 27.1: The Electric Field of 3 Equal Point Charges

## Example 27.1

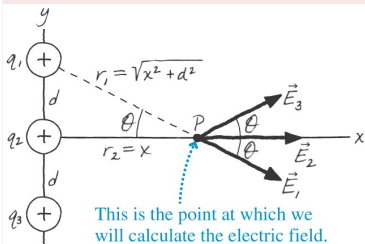


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Three equal point charges  $q$  are located on the  $y$ -axis at  $y = 0$  and  $y = \pm d$ . What is the electric field at a point on the  $x$ -axis?

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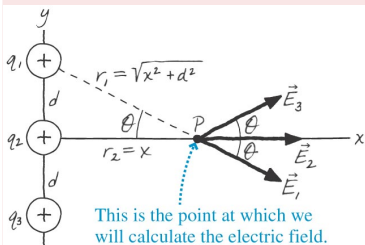


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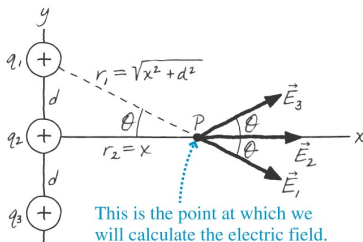
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Three equal point charges  $q$  are located on the  $y$ -axis at  $y = 0$  and  $y = \pm d$ . What is the electric field at a point on the  $x$ -axis?

- There are some clear simplifications - we do not care about the  $z$  direction at all. The  $y$  components cancel out.
- The  $x$  components add like

$$(E_{net})_x = (E_1)_x + (E_2)_x + (E_3)_x = 2(E_1)_x + (E_2)_x$$

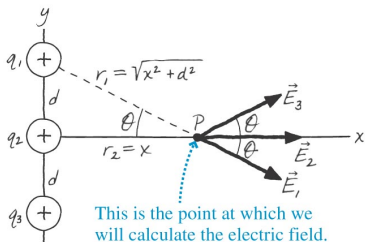
# Example 27.1: The Electric Field of 3 Equal Point Charges



$$(E_2)_x = E_2 = \frac{1}{4\pi\epsilon_0} \frac{q_2}{x^2}$$

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# Example 27.1: The Electric Field of 3 Equal Point Charges



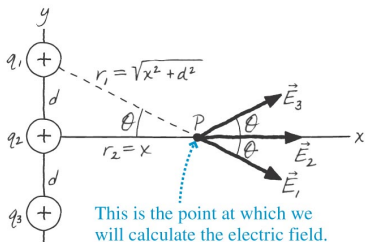
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$$(E_2)_x = E_2 = \frac{1}{4\pi\epsilon_0} \frac{q_2}{x^2}$$

$$(E_1)_x = E_1 \cos \theta = \frac{1}{4\pi\epsilon_0} \frac{q_1}{r_1^2} \cos \theta$$



# Example 27.1: The Electric Field of 3 Equal Point Charges



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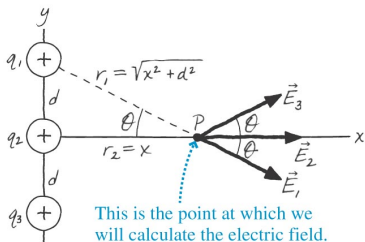
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- But  $r_1$  and  $\theta$  vary with  $x$ . We should express  $E_1$  in terms of  $x$

$$\cos \theta = \frac{x}{r_1} = \frac{x}{(x^2 + d^2)^{1/2}}$$

# Example 27.1: The Electric Field of 3 Equal Point Charges



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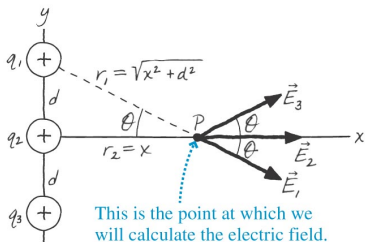
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$$\cos \theta = \frac{x}{r_1} = \frac{x}{(x^2 + d^2)^{1/2}}$$

$$(E_1)_x = \frac{1}{4\pi\epsilon_0} \frac{q}{x^2 + d^2} \frac{x}{(x^2 + d^2)^{1/2}} = \frac{1}{4\pi\epsilon_0} \frac{xq}{(x^2 + d^2)^{3/2}}$$

## Example 27.1: The Electric Field of 3 Equal Point Charges

Combining the expressions gives

$$(E_{net})_x = 2(E_1)_x + (E_2)_x = \frac{q}{4\pi\epsilon_0} \left[ \frac{1}{x^2} + \frac{2x}{(x^2 + d^2)^{3/2}} \right]$$

## Example 27.1: The Electric Field of 3 Equal Point Charges

Combining the expressions gives

$$(E_{net})_x = 2(E_1)_x + (E_2)_x = \frac{q}{4\pi\epsilon_0} \left[ \frac{1}{x^2} + \frac{2x}{(x^2 + d^2)^{3/2}} \right]$$
$$\vec{E}_{net} = \frac{q}{4\pi\epsilon_0} \left[ \frac{1}{x^2} + \frac{2x}{(x^2 + d^2)^{3/2}} \right] \hat{i}$$

- Notice as  $x \rightarrow 0$  the second term vanishes

$$\vec{E}_{net} = \frac{1}{4\pi\epsilon_0} \frac{q}{x^2} \hat{i}$$

## Example 27.1: The Electric Field of 3 Equal Point Charges

Combining the expressions gives

$$(E_{net})_x = 2(E_1)_x + (E_2)_x = \frac{q}{4\pi\epsilon_0} \left[ \frac{1}{x^2} + \frac{2x}{(x^2 + d^2)^{3/2}} \right]$$
$$\vec{E}_{net} = \frac{q}{4\pi\epsilon_0} \left[ \frac{1}{x^2} + \frac{2x}{(x^2 + d^2)^{3/2}} \right] \hat{i}$$

- Notice as  $x \rightarrow 0$  the second term vanishes

$$\vec{E}_{net} = \frac{1}{4\pi\epsilon_0} \frac{q}{x^2} \hat{i}$$

- As  $x$  gets very large,  $d$  becomes insignificant compared to  $x$ .

$$\vec{E}_{net} = \frac{1}{4\pi\epsilon_0} \frac{(3q)}{x^2} \hat{i}$$