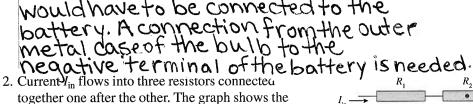
# 32 Fundamentals of Circuits

## 32.1 Circuit Elements and Diagrams

#### 32.2 Kirchhoff's Laws and the Basic Circuit

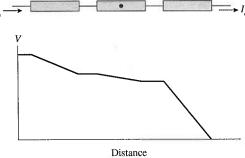
1. The tip of a flashlight bulb is touching the top of a 3 V battery. Does the bulb light? Why or why not?

No This is not a complete circuit. Both the side and the base of the bulb would have to be connected to the



value of the potential as a function of distance. a. Is  $I_{\text{out}}$  greater than, less than, or equal to  $I_{\text{in}}$ ? Explain.

Equal. This is due to the conservation of current



b. Rank in order, from largest to smallest, the three resistances  $R_1$ ,  $R_2$ , and  $R_3$ .

Order:  $R_3 > R_1 > R_2$ 

 $R = \Delta V$  and the current is the same through I each resistor:  $\Delta V_3 > \Delta V_1 > \Delta V_2$ 

c. Is there an electric field at the point inside  $R_2$  that is marked with a dot? If so, in which direction does it point? If not, why not?

Yes. The resistor is just a conductor with a larger resistance than the wires in the circuit. The electric field points to the right.

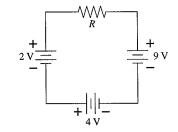
3 V

3. A flashlight bulb is connected to a battery and is glowing. Is current  $I_2$  greater than, less than, or equal to current  $I_1$ ? Explain.



I = I a due to conservation of current.

4. a. In which direction does current flow through resistor R?



Right to left.

b. Which end of *R* is more positive? Explain.

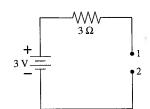
The right end. The current always enters the resistor on the high potential side of the resistor.

c. If this circuit were analyzed in a clockwise direction, what numerical value would you assign to  $\Delta V_R$ ? Why?

d. What value would  $\Delta V_{\rm R}$  have if the circuit were analyzed in a counterclockwise direction?

DVR=-3V

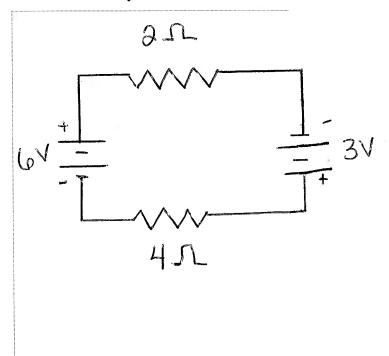
5. The wire is broken on the right side of this circuit. What is the potential difference  $\Delta V_{12}$  between points 1 and 2? Explain.



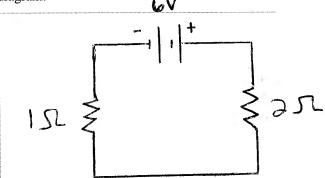
AV<sub>12</sub>=3V There is no current through the resistor so there is no potential difference across the resistor

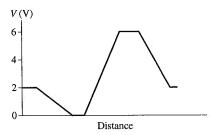
$$6V - I \cdot 2\Omega + 3V - I \cdot 4\Omega = 0$$

Assume that the analysis is done in a clockwise direction.



7. The current in a circuit is 2.0 A. The graph shows how the potential changes when going around the circuit in a clockwise direction, starting from the lower left corner. Draw the circuit diagram.



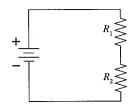


# 32.3 Energy and Power

8. This circuit has two resistors, with  $R_1 > R_2$ . Which of the two resistors dissipates the larger amount of power? Explain.

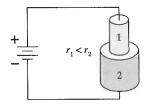
R, dissipates more power.

PR = I2 R The same current flows through each resistor.



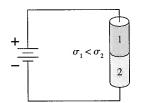
9. Two conductors of equal lengths are connected to a battery by ideal wires. The conductors are made of the same material but have different radii. Which of the two conductors dissipates the larger amount of power? Explain.

Conductor 1. Since r<ra; then



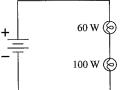
 $A_1 < A_2$  and  $R_1 > R_2$ . R = PL Both have the same p and the same  $L \cdot P_R = T^2 R$ 

10. Two conductors of equal lengths are connected to a battery by ideal wires. The conductors have the same radii but are made of different materials and have different conductivities  $\sigma$ . Which of the two conductors dissipates the larger amount of power? Explain.



Conductor 1. Resistivity is the reciprocal of conductivity  $P = \overline{\sigma}$ . So if  $\sigma_1 < \sigma_2$  then  $P_1 > P_2$  and  $P_1 > P_3$ . Therefore  $(P_R)_1 > (P_R)_2$  $P = P_1 = P_2$  and  $P_R = I^2R$ 

11. A 60 W lightbulb and a 100 W lightbulb are placed one after the other in a circuit. The battery's emf is large enough that both bulbs are glowing. Which one glows more brightly? Explain.



Here the currents are the same so

P=I > R and the 60W bulb has more
resistance. (The Wattage ratings are
determined by putting equal voltages
across the bulbs not equal currents.)

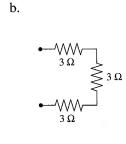
Therefore, the 60W bulb glows more brightly.

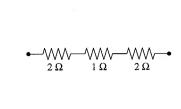
c.

#### 32.4 Series Resistors

#### 32.5 Real Batteries

12. What is the equivalent resistance of each group of resistors?





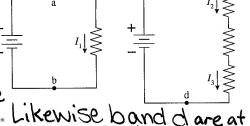
$$R_{\rm eq} = 115$$

$$R_{\rm eq} = 9 \Omega$$

$$R_{\rm eq} = 50$$

- 13. The figure shows two circuits. The two batteries are identical and the four resistors all have exactly the same resistance.
  - a. Is  $\Delta V_{ab}$  larger than, smaller than, or equal to  $\Delta V_{cd}$ ?

are at the same potential as the positive electrode of the battery. Likewise band d are at the same potential as the negative electrode, or Rank in order, from largest to smallest, the currents I1, I2, and I3.



Order: 
$$I_1 > I_2 = I_3$$

Explanation:

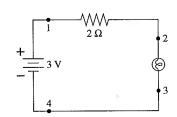
I, and I, are equal due to conservation of current.

- 14. The lightbulb in this circuit has a resistance of  $1\Omega$ .
  - a. What are the values of:

$$\Delta V_{12} - \partial V$$

$$\Delta V_{23} - |V|$$

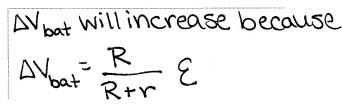
$$\Delta V_{34} = 0 V$$

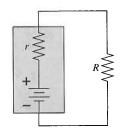


b. Suppose the bulb is now removed from its socket. Then what are the values of:

$$\begin{array}{c} \Delta V_{12} & \text{OV} \\ \Delta V_{23} & \text{-} \text{3V} \\ \Delta V_{34} & \text{OV} \end{array}$$

15. If the value of R is increased, does  $\Delta V_{\rm bat}$  increase, decrease, or stay the same? Explain.

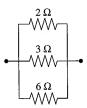




## 32.6 Parallel Resistors

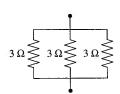
16. What is the equivalent resistance of each group of resistors?

a.



- 10





 $R_{\rm eq} = 15$ 

 $R_{\rm eq} = 0.5 \Omega$ 

17. a. What fraction of current I goes through the  $3\Omega$  resistor?

34

- $I \longrightarrow \begin{bmatrix} {}^{3}\Omega \\ {}^{\vee} \\ {}^{\vee} \\ {}^{9}\Omega \end{bmatrix}$
- b. If the  $9\Omega$  resistor is replaced with a larger resistor, will the fraction of current going through the  $3\Omega$  resistor increase, decrease, or stay the same?

Increase.

18. The figure shows five combinations of identical resistors. Rank in order, from largest to smallest, the equivalent resistances  $(R_{eq})_1$  to  $(R_{eq})_5$ .

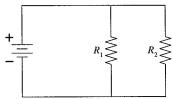
Order: (Req) 2 > (Req) 4 > (Req), > (Req) 5 > (Req)

Explanation: 
$$(Req)_1 = R (Req)_3 = \frac{R}{3} (Req)_4 = \frac{3R}{3}$$

## 32.7 Resistor Circuits

# 32.8 Getting Grounded

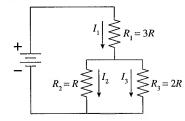
19. The circuit shown has a battery and two resistors, with  $R_1 > R_2$ . Which of the two resistors dissipates the larger amount of power? Explain your reasoning.



Radissipates more power

 $\rho = (\Delta V)^2$  and both resistors have the Same potential drop because they are connected in parallel.

20. Rank in order, from largest to smallest, the three currents  $I_1$  to  $I_3$ .

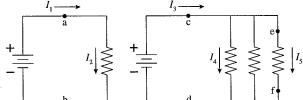


Order:  $I_1 > I_2 > I_3$ 

Explanation: By Kirchhoff's Junction Rule  $I_1 = I_2 + I_3$ . Also  $I_3$  is less than  $I_2$ 

because R3>R2 and they have the Same potential difference because they are in parallel. I= DY

21. The two batteries are identical and the four resistors all have exactly the same resistance.



a. Compare  $\Delta V_{\rm ab}$ ,  $\Delta V_{\rm cd}$ , and  $\Delta V_{\rm ef}$ . Are they all the same? If not, rank them in decreasing order. Explain your reasoning.

They are all the same.

Points a, c, and e are all at the same potential as the positive electrode on the battery. Points b, d, and f are all at the same potential as the negative electrode.

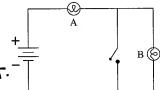
b. Rank in order, from largest to smallest, the five currents  $I_1$  to  $I_5$ .

Order:  $T_3 > T_1 = T_2 = T_4 = T_5$ Explanation:

By conservation of current  $T_1 = T_2$ .

Also  $T_1 = \frac{W_{bat}}{R} = \frac{1}{3} = \frac{W_{bat}}{R/3} = \frac{3T_1}{R/3}$   $T_4 = \frac{W_{bat}}{R} = T_5$  Exercises 22–28: Assume that all wires are ideal (zero resistance) and that all batteries are ideal (constant potential difference).

22. Initially bulbs A and B are glowing. Then the switch is closed. What happens to each bulb? Does it get brighter, stay the same, get dimmer, or go out? Explain your reasoning.

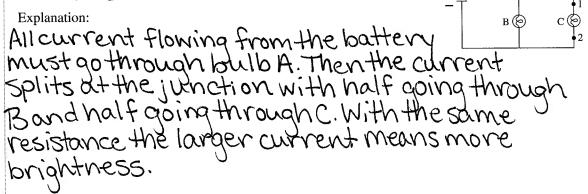


A (🕞

Bub Agets brighter and bulb B goes out. - I when the switch is closed all the current travels along this zero resistance poth rather than through bulb B. With less resistance in the circuit the current is larger so bulb A burns brighter.

23. a. Bulbs A, B, and C are identical. Rank in order, from most to least, the brightnesses of the three bulbs.

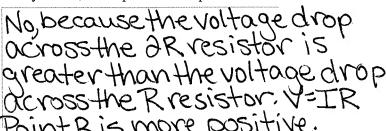
Order: A>B=C

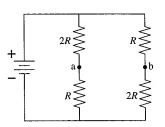


b. Suppose a wire is connected between points 1 and 2. What happens to each bulb? Does it get brighter, stay the same, get dimmer, or go out? Explain.

Bulbs Band C go out because now there is a zero resistance wire along which all the current will flow. Now the total resistance in the circuit is less, the current is more, and bulb A will burn brighter.

24. a. Consider the points a and b. Is the potential difference  $\Delta V_{ab} = 0$ ? If so, why? If not, which point is more positive?





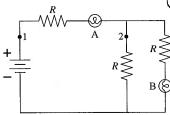
connected between points a and b, does a current flow through it? If so, in which direction to the right or to the left? Explain.

To the left. A wire connecting points a and b forces the same potentia ough each Rres the junction In ar registor. that current flows to the right

25. Bulbs A and B are identical. Initially both are glowing.

a. Bulb A is removed from its socket. What happens to bulb B? Does it get brighter, stay the same, get dimmer, or go out? Explain.

It goes out. With bulb A out of its uit is not complete. there is no closed both from the



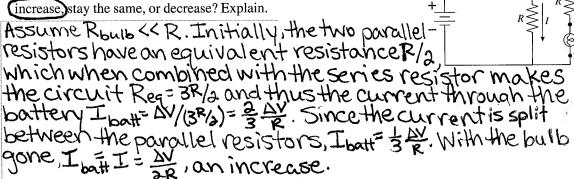
b. Bulb A is replaced. Bulb B is then removed from its socket. What happens to bulb A? Does it get brighter, stay the same, get dimmer, or go out? Explain.

immer. The current ecreases because resistance of the

c. The circuit is restored to its initial condition. A wire is then connected between points 1 and 2. What happens to the brightness of each bulb?

because # is more.

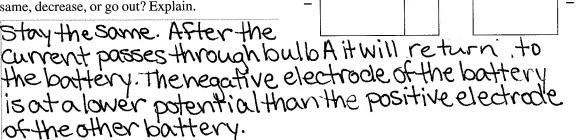
- 26. Initially the lightbulb is glowing. It is then removed from its socket.
  - a. What happens to the current *I* when the bulb is removed? Does it



b. What happens to the potential difference  $\Delta V_{12}$  between points 1 and 2? Does it increase, stay the same, decrease, or become zero? Explain.

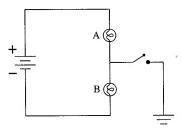
Increases. Now there is no potential difference across the resistor that is in series with the bulb because there is no current through the resistor. So the potential difference between land a is now the potential difference of the parallel group.

27. Bulbs A and B are identical and initially both are glowing. Then the switch is closed. What happens to each bulb? Does its brightness increase, stay the same, decrease, or go out? Explain.



28. Bulbs A and B are identical and initially both are glowing. Then the switch is closed. What happens to each bulb? Does its brightness increase, stay the same, decrease, or go out? Explain.

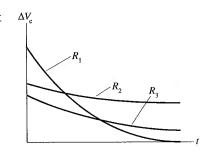
Staysthesame. The ground wire is not part of a complete circuit so no current will flow down it. The current through the bulbs remains the same.



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## 32.9 RC Circuits

29. The graph shows the voltage as a function of time on a capacitor as it is discharged (separately) through three different resistors. Rank in order, from largest to smallest, the values of the resistances  $R_1$  to  $R_3$ .

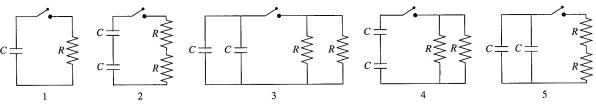


Order:  $\mathbb{R}_{2} > \mathbb{R}_{3} > \mathbb{R}_{1}$ 

**Explanation:** 

T=RC The decay time is longest for the R2 curve and Shortest for the R, curve.

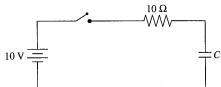
30. The capacitors in each circuit are discharged when the switch closes at t = 0 s. Rank in order, from largest to smallest, the time constants  $\tau_1$  to  $\tau_5$  with which each circuit will discharge.



Order:  $T_5 > T_1 = T_2 = T_3 > T_4$ 

**Explanation:** 

- 31. The charge on the capacitor is zero when the switch closes at t = 0 s.
  - a. What will be the current in the circuit after the switch has been closed for a long time? Explain.



After the switch has been closed along time the capacitor will be fully charged and the current will decrease to zero.

(Actually I=0 at t>0.)

b. Immediately after the switch closes, before the capacitor has had time to charge, the potential difference across the capacitor is zero. What must be the potential difference across the resistor in order to satisfy Kirchhoff's loop law? Explain.

10V. With a zero potential difference across the capacitor DVc+DVR = DVbatt 50 DVR = DVbatt - DVc
DVR = 10V - 0V = 10V

c. Based on your answer to part b, what is the current in the circuit immediately after the switch closes?

I = WR = 10V = 1A

d. Sketch a graph of current versus time, starting from just before t = 0 s and continuing until the switch has been closed a long time. There are no numerical values for the horizontal axis, so you should think about the *shape* of the graph.

