Electricity & Magnetism
Lecture 12

Today's Concept:

Magnetic Force on Moving Charges

$$\vec{F} = q\vec{v} \times \vec{B}$$

Today's rants

I'm struggling a fair bit with this component of the course. Got me feeling like- https://www.youtube.com/watch?v=SIaFtAKnqBU and this https://youtu.be/PpccpglnNf0?t=1m39s

-

This lecture was okay, the major thing you really needed to know was the reet hend rull

It was good.

Please go over everything with examples. I was too traumatized to understand anything

Need a lot of help to understand the direction

magnetism is easier then current, please go over some of the rc circuit/kirchoff rules again please

these prelectures are not very good

can you explain how the velocity selector works again please?

I have no clue what's going on in this chapter. Please explain

so the B stands for magnetic field and its cross product with qv generates a force. so where does the electric field come into play

Can you please explain directions in more detail?

maybe explaining more the difference between magnetic field and force, and which ones to use in RHR, please.

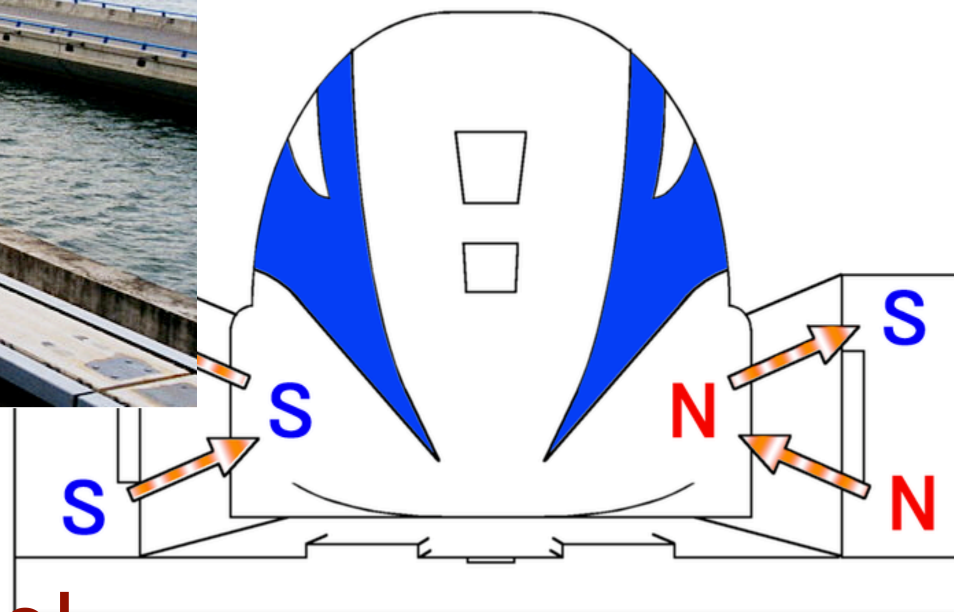
Please discuss more about the velocity selector.

What is this stuff

Can you please explain right hand rule again?

Comments

this stuff gets fun now :)

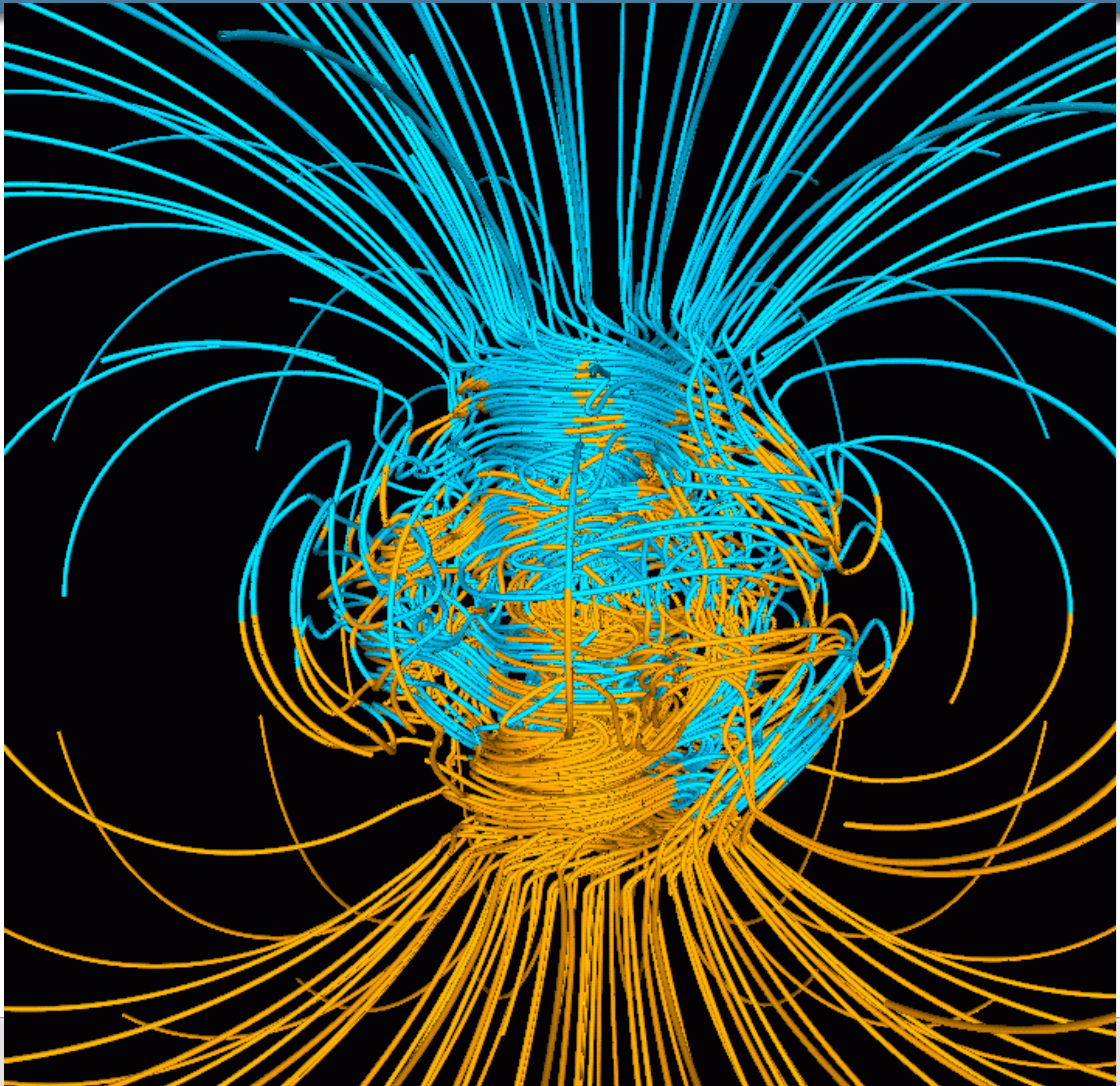


"see" on a flat screen,

etc., etc., ...

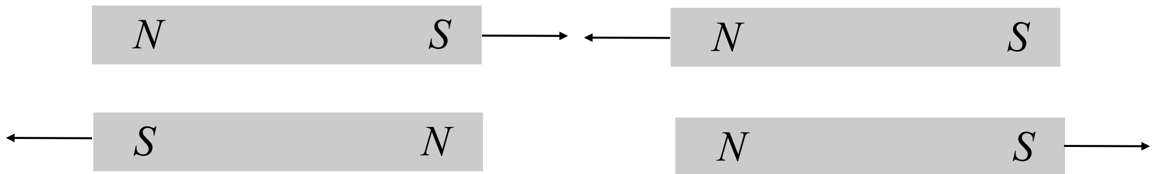
Will do!

Earth’s Magnetic Fleld



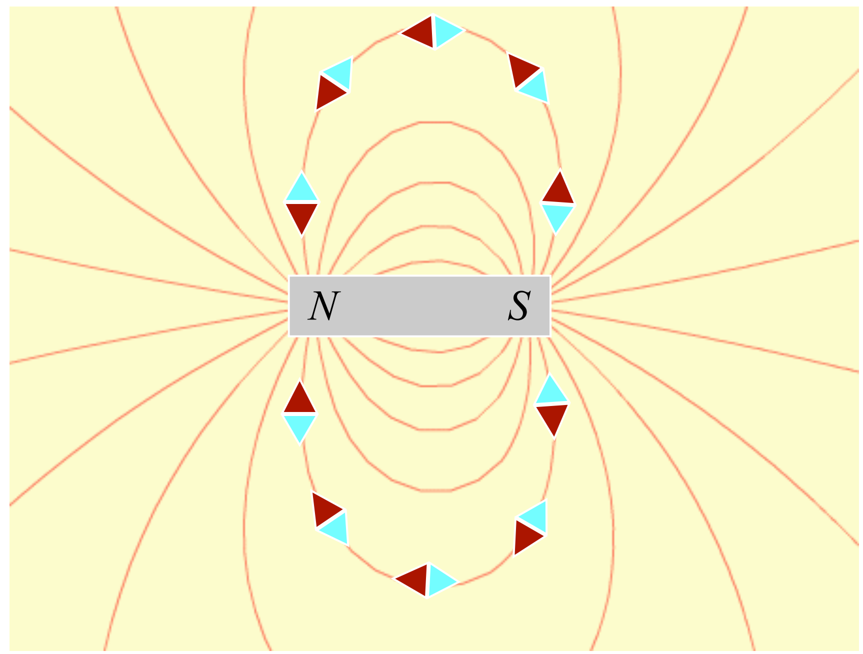
Magnetic Observations

Bar Magnets

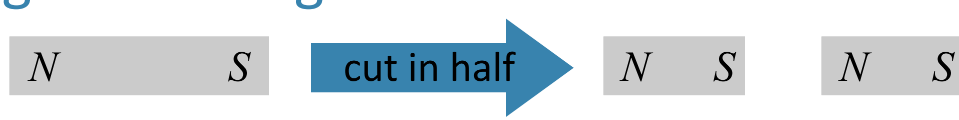


Compass Needles

These are "magnetic dipoles" and behave similarly to "electric dipoles"

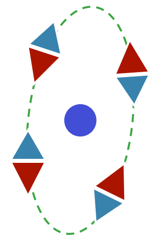


Magnetic Charge?



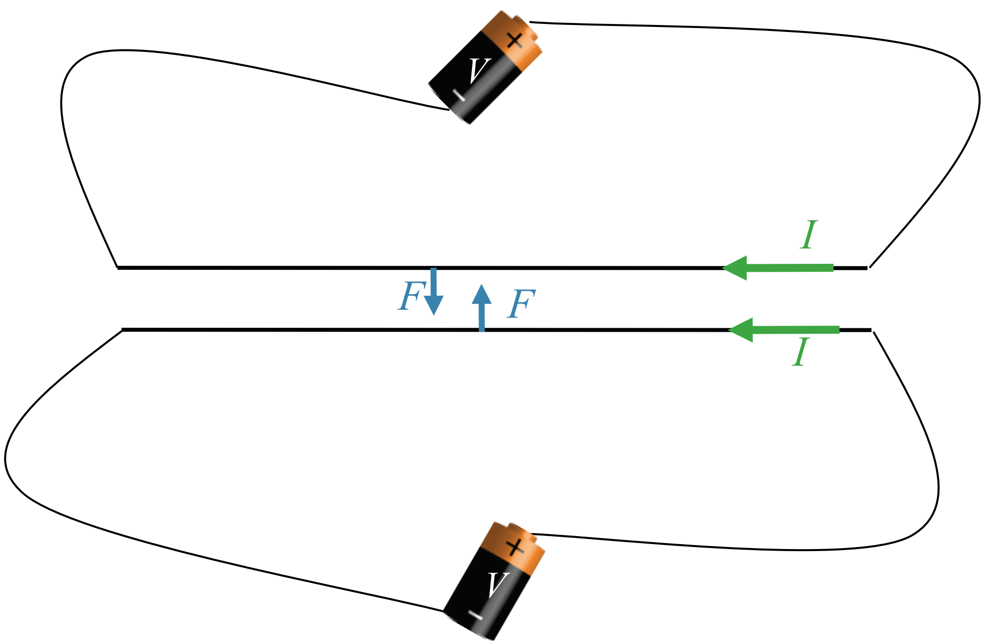
Magnetic Observations

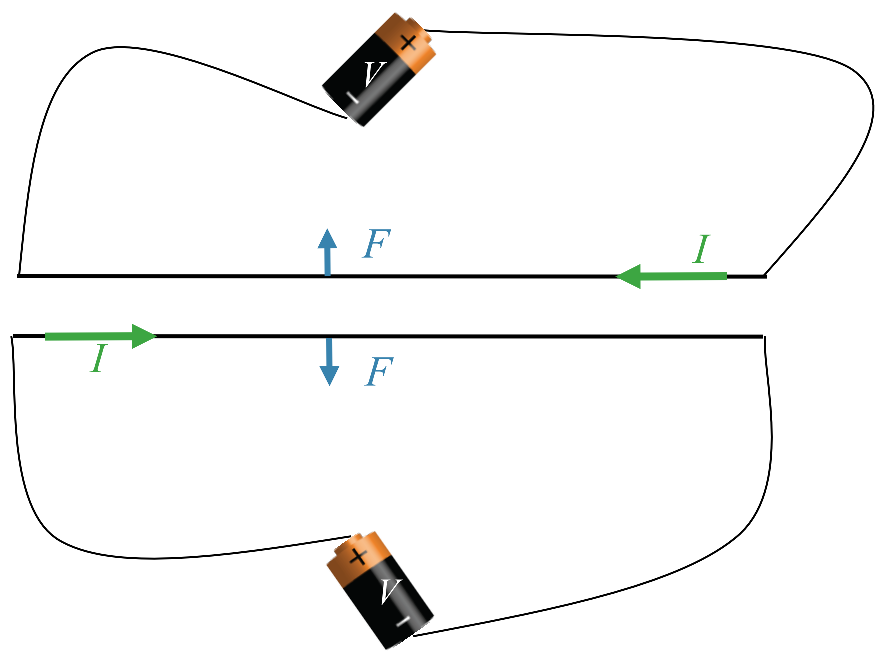
Compass needle deflected by electric current



Magnetic fields created by electric currents

Magnetic fields exert forces on electric currents (charges in motion)





Magnetism & Moving Charges

All observations are explained by two equations:

$$\vec{F} = q\vec{v} \times \vec{B}$$

Today

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{s} \times \hat{r}}{r^2}$$

Next Week

Cross Product Review

Cross Product different from Dot Product

$\mathbf{A} \cdot \mathbf{B}$ is a scalar; $\mathbf{A} \times \mathbf{B}$ is a vector

$\mathbf{A} \cdot \mathbf{B}$ proportional to the component of $\mathbf{B}$ parallel to $\mathbf{A}$

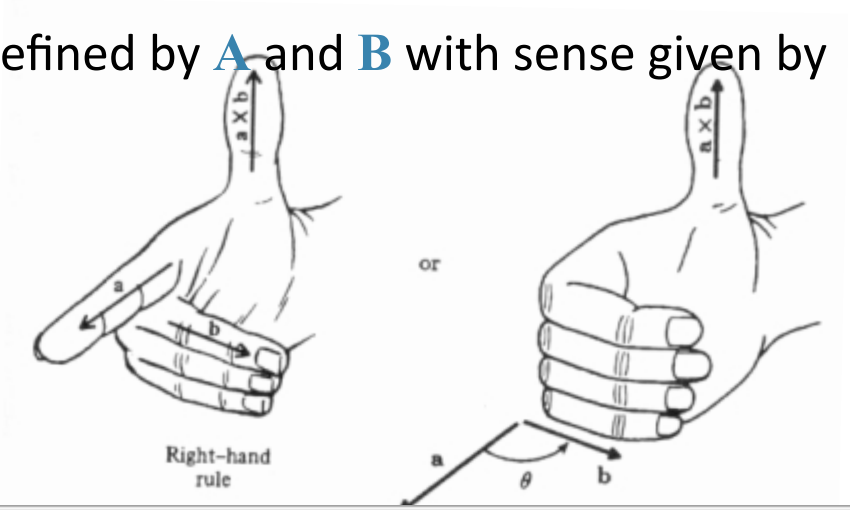
$\mathbf{A} \times \mathbf{B}$ proportional to the component of $\mathbf{B}$ perpendicular to $\mathbf{A}$

is a scalar; $\mathbf{A} \times \mathbf{B}$ is a vector

Definition of $\mathbf{A} \times \mathbf{B}$

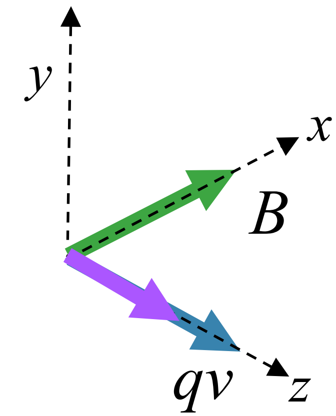
Magnitude: $|\mathbf{A}||\mathbf{B}| \sin \theta$

Direction: perpendicular to plane defined by $\mathbf{A}$ and $\mathbf{B}$ with sense given by right-hand-rule



Remembering Directions: The Right Hand Rule

$$\vec{F} = q\vec{v} \times \vec{B}$$

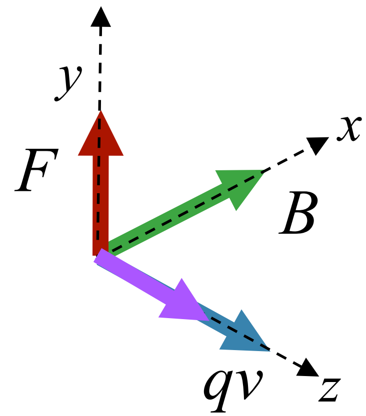


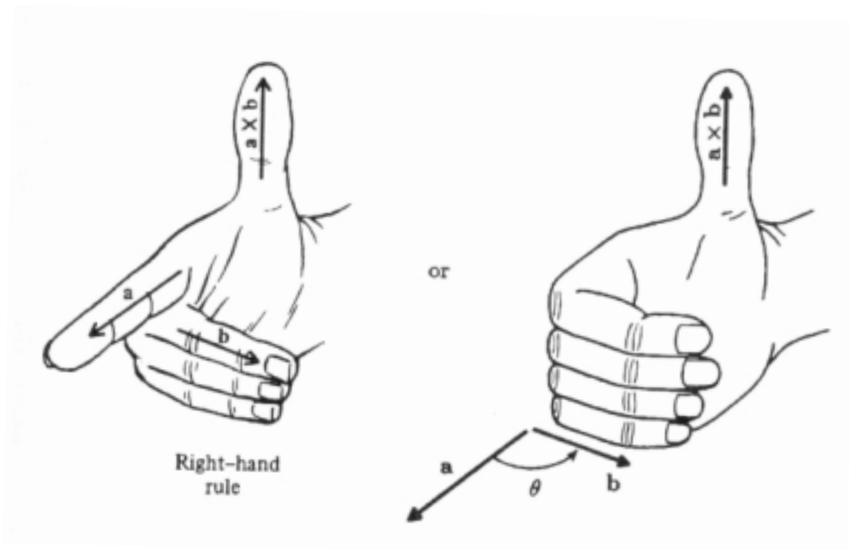
Which way does the force point?

A. x
B. –x
C. y
D. –y
E. z

Remembering Directions: The Right Hand Rule

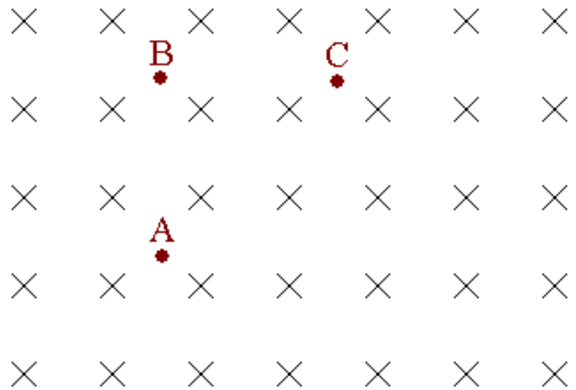
$$\vec{F} = q\vec{v} \times \vec{B}$$





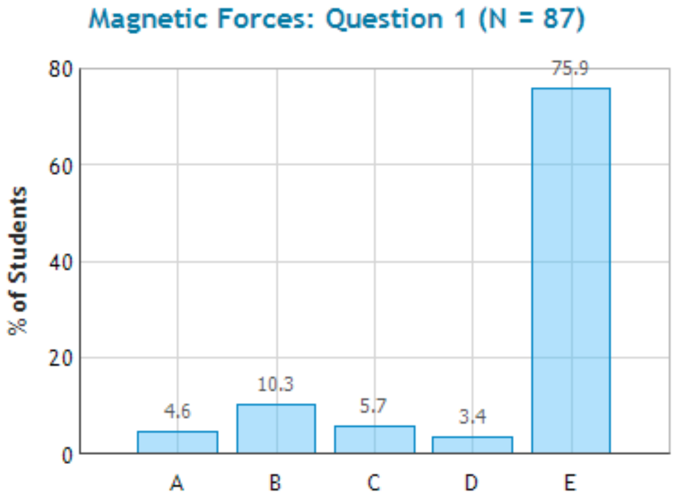
CheckPoint 2

Three points are arranged in a uniform magnetic field. The B field points into the screen.



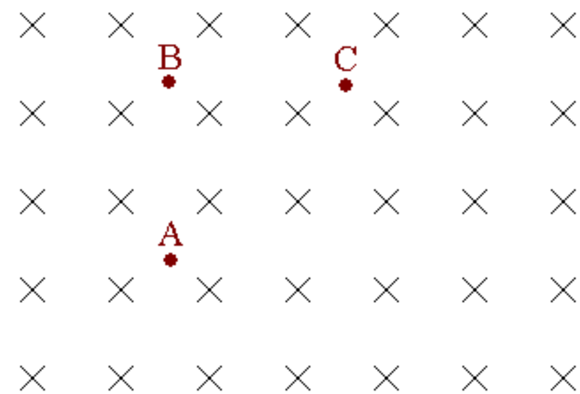
A positively charged particle is at point A and is stationary. The direction of the magnetic force on the particle is

A. right
B. left
C. into screen
D. out of screen
E. zero



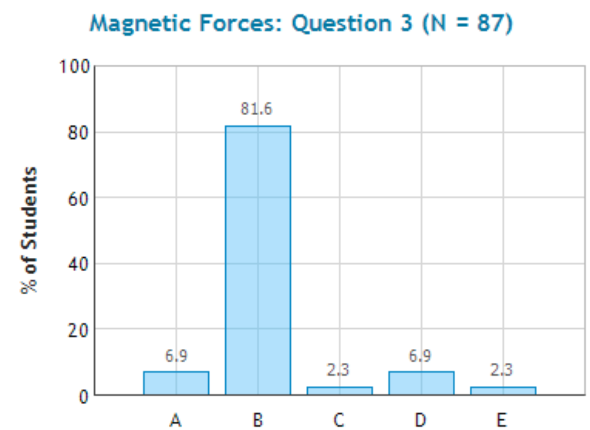
CheckPoint 4

Three points are arranged in a uniform magnetic field. The B field points into the screen.



The positive charge moves from A to B. The direction of the magnetic force on it is

A. right
B. left
C. into screen
D. out of screen
E. zero



Cross Product Practice

Protons (positive charge) coming out of screen

Magnetic field pointing down

What is direction of force on POSITIVE charge?

$$\vec{F} = q\vec{v} \times \vec{B}$$

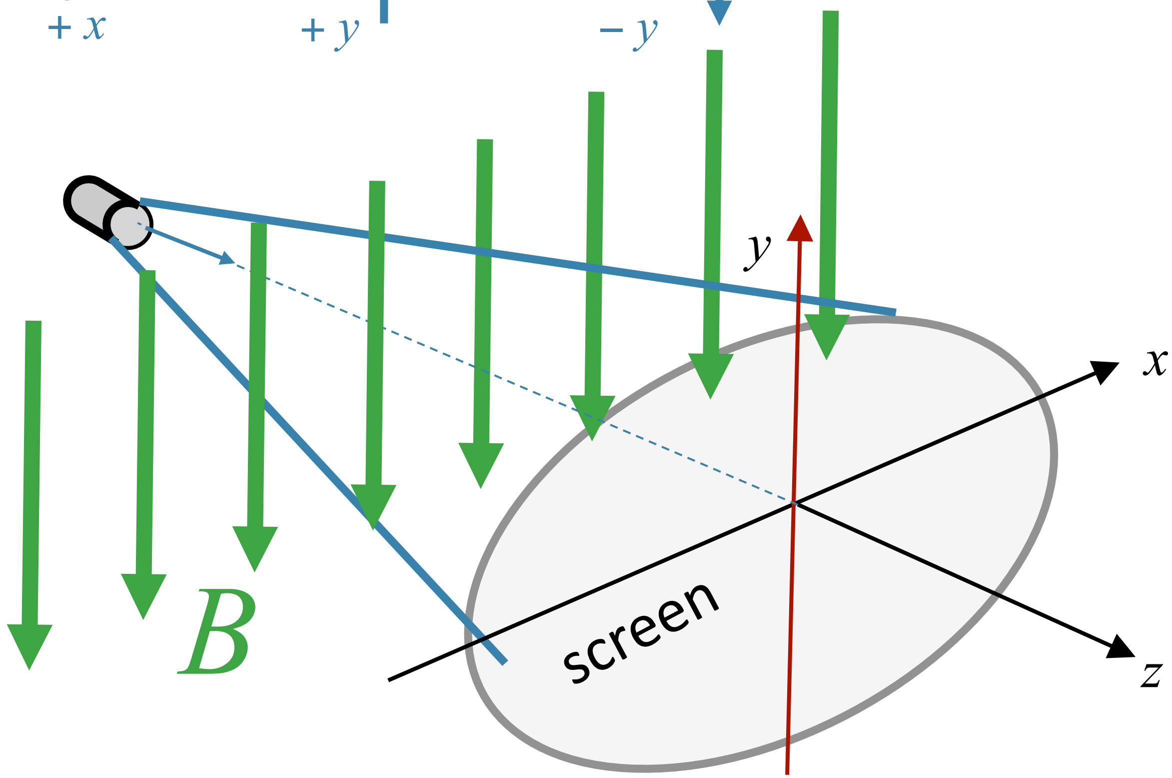
A) Left $-x$

B) Right $+x$

C) UP $+y$

D) Down $-y$

E) Zero



Motion of Charge q in Uniform B Field

Force is perpendicular to **v**

Speed does not change

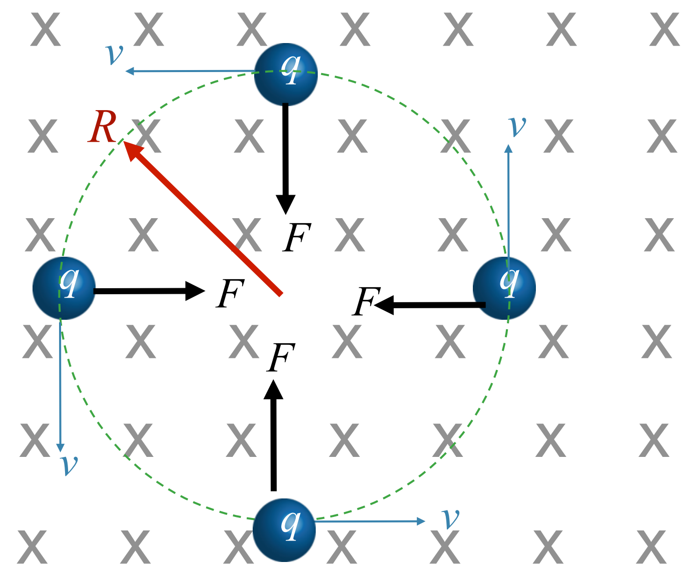
Uniform Circular Motion

Solve for R:

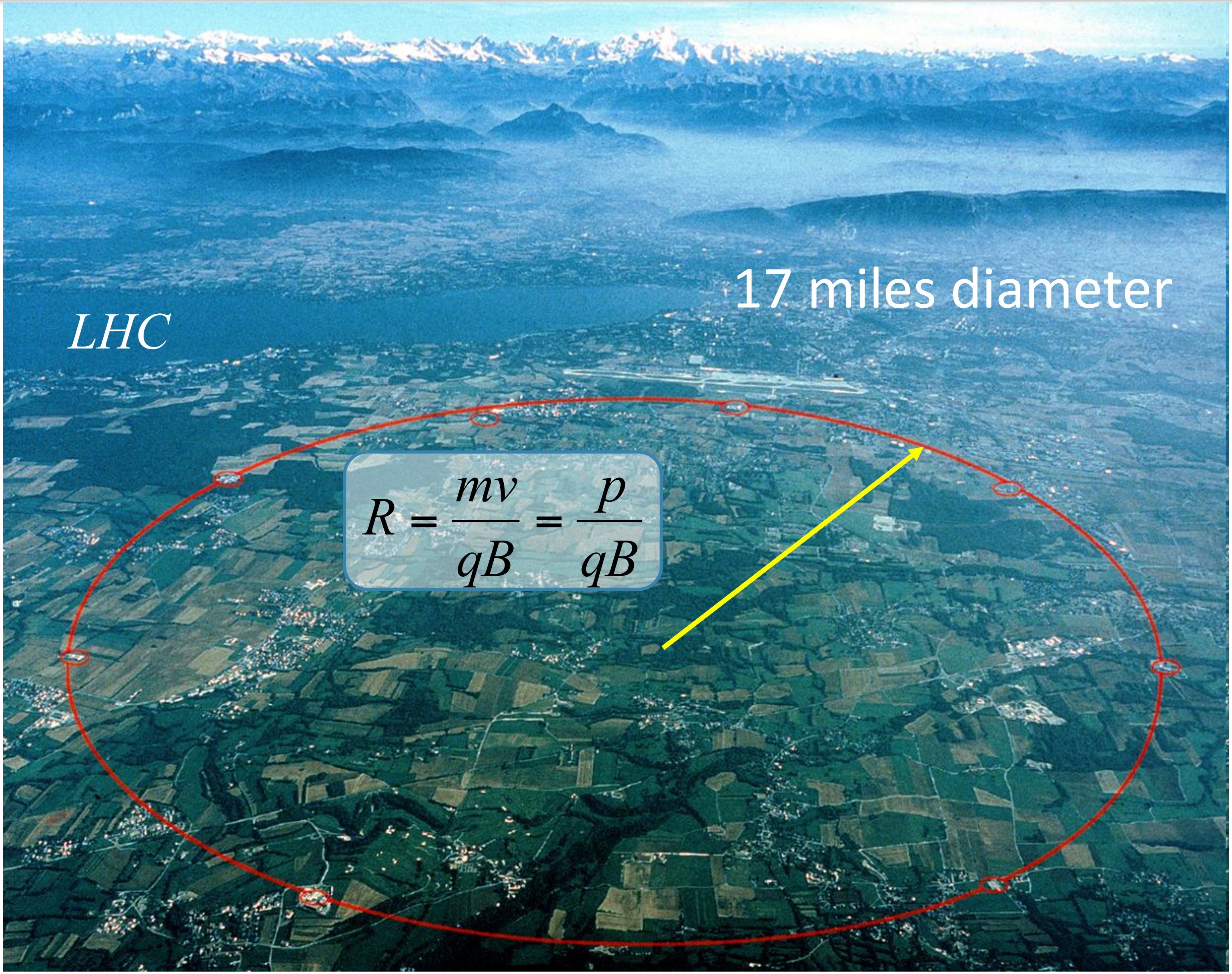
$$\vec{F} = q\vec{v} \times \vec{B} \Rightarrow F = qvB$$

$$a = \frac{v^2}{R}$$

$$qvB = m\frac{v^2}{R} \quad \longrightarrow \quad R = \frac{mv}{qB}$$



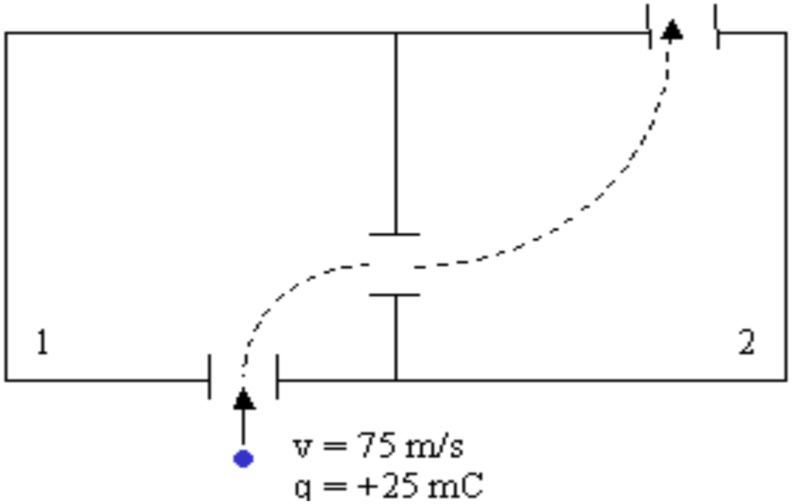
Uniform **B** into page



$$R = \frac{mv}{qB} = \frac{p}{qB}$$

CheckPoint 6

The drawing shows the top view of two interconnected chambers. Each chamber has a unique magnetic field. A positively charged particle is fired into chamber 1, and observed to follow the dashed path shown in the figure.



What is the direction of the magnetic field in chamber 1?

A. up

B. down

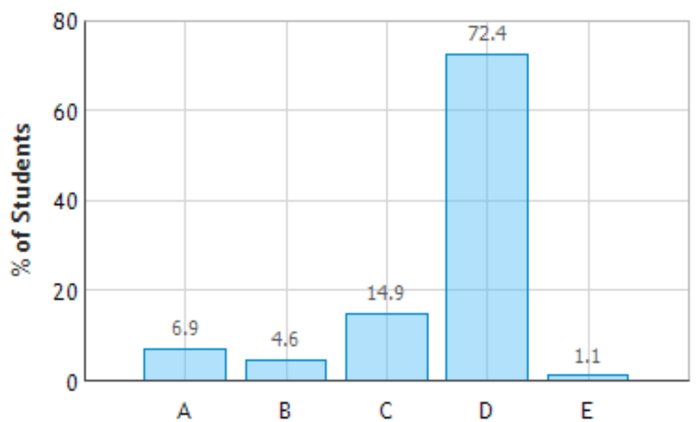
C. into page

D. out of page

E. Zero

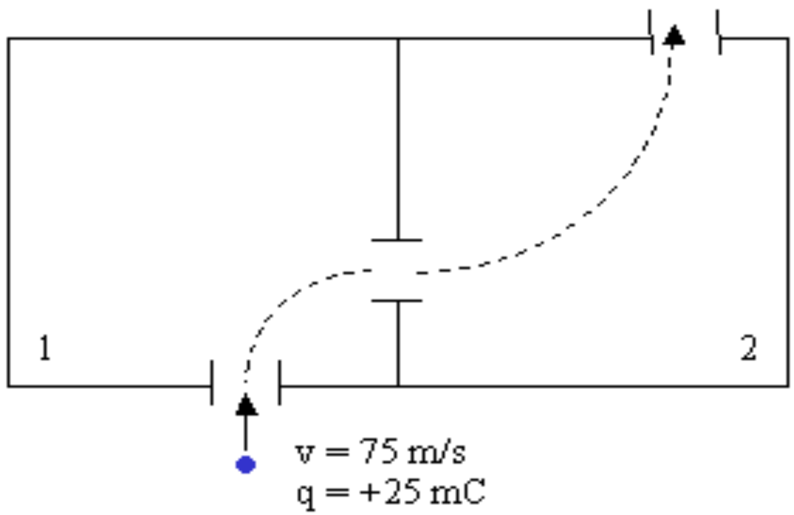
Confusion?

Motion in a Magnetic Field: Question 1 (N = 87)



CheckPoint 8

The drawing shows the top view of two interconnected chambers. Each chamber has a unique magnetic field. A positively charged particle is fired into chamber 1, and observed to follow the dashed path shown in the figure.

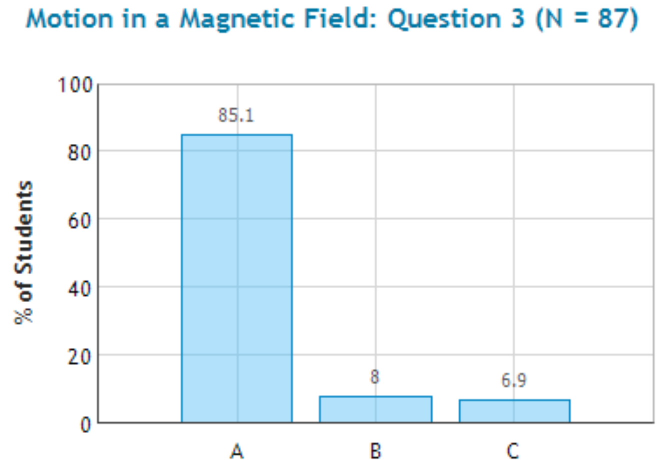


Compare the magnitude of the magnetic field in chamber 1 to the magnitude of the magnetic field in chamber 2.

A. $|B_1| > |B_2|$

B. $|B_1| = |B_2|$

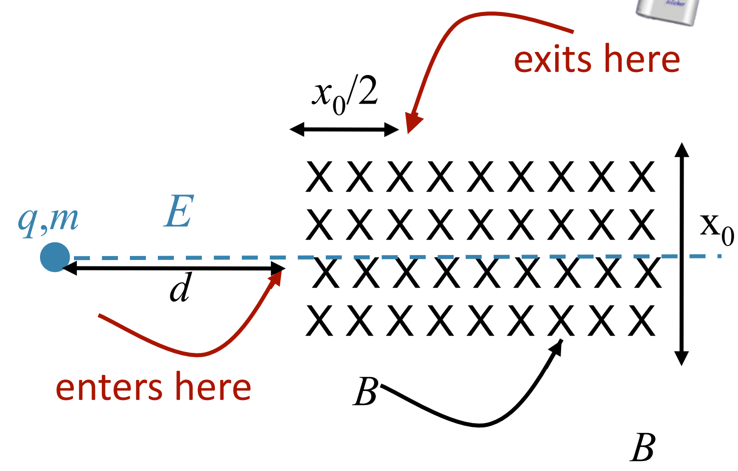
C. $|B_1| < |B_2|$



Calculation

A particle of charge q and mass m is accelerated from rest by an electric field E through a distance d and enters and exits a region containing a constant magnetic field B at the points shown. Assume q,m,E,d, and x_0 are known.

What is B?



Conceptual Analysis

What do we need to know to solve this problem?

A) Lorentz Force Law

B) E field definition

C) V definition

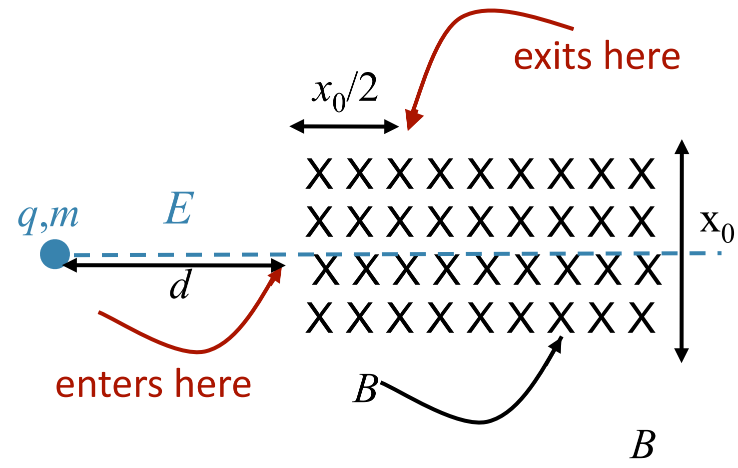
D) Conservation of Energy/Newton's Laws

E) All of the above

Calculation

A particle of charge q and mass m is accelerated from rest by an electric field E through a distance d and enters and exits a region containing a constant magnetic field B at the points shown. Assume q,m,E,d, and x_0 are known.

What is B?



Strategic Analysis

Calculate v, the velocity of the particle as it enters the magnetic field

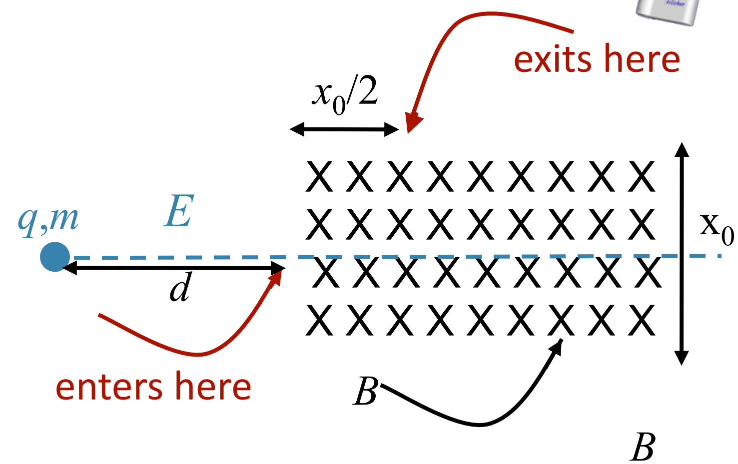
Use Lorentz Force equation to determine the path in the field as a function of B

Apply the entrance-exit information to determine B

Calculation

A particle of charge q and mass m is accelerated from rest by an electric field E through a distance d and enters and exits a region containing a constant magnetic field B at the points shown. Assume q,m,E,d, and x_0 are known.

What is B?



What is v_0, the speed of the particle as it enters the magnetic field ?

A: $v_o = \sqrt{\dfrac{2E}{m}}$

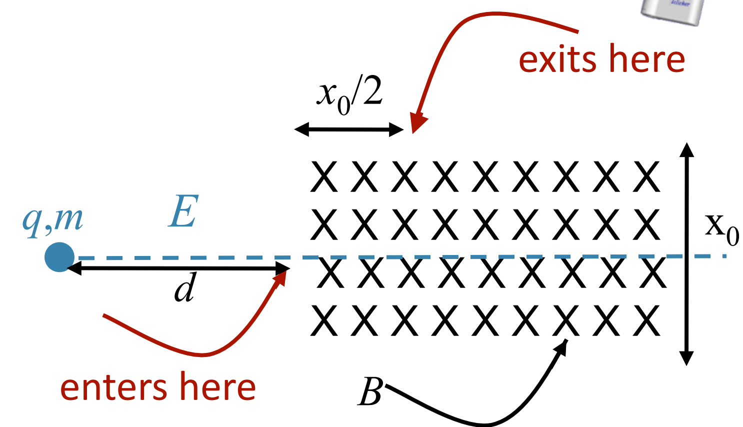
B: $v_o = \sqrt{\dfrac{2qEd}{m}}$

C: $v_o = \sqrt{2ad}$

D: $v_o = \sqrt{\dfrac{2qE}{md}}$

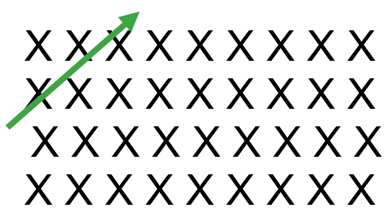
E: $v_o = \sqrt{\dfrac{qEd}{m}}$

A particle of charge q and mass m is accelerated from rest by an electric field E through a distance d and enters and exits a region containing a constant magnetic field B at the points shown. Assume q,m,E,d, and x_0 are known.

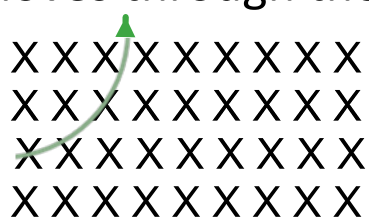


What is B? $v_o = \sqrt{\frac{2qEd}{m}}$

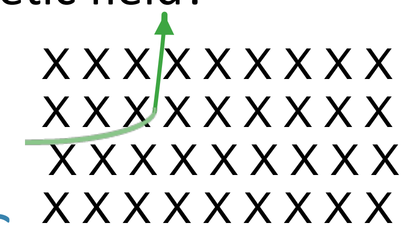
What is the path of the particle as it moves through the magnetic field? B



A



B

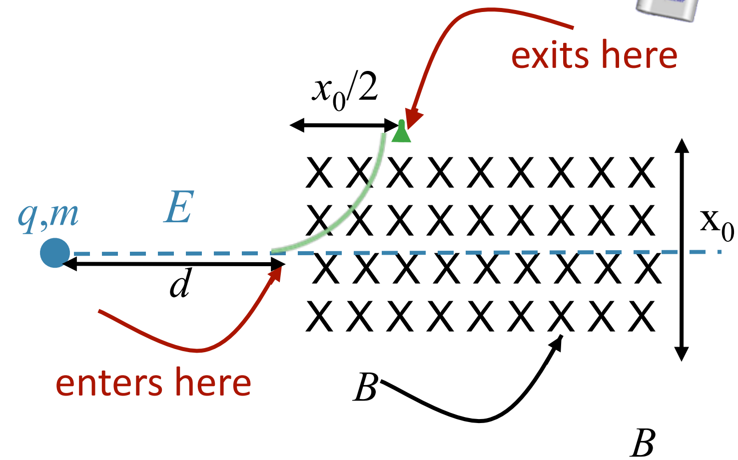


C

Calculation

A particle of charge q and mass m is accelerated from rest by an electric field E through a distance d and enters and exits a region containing a constant magnetic field B at the points shown. Assume q,m,E,d, and x_0 are known.

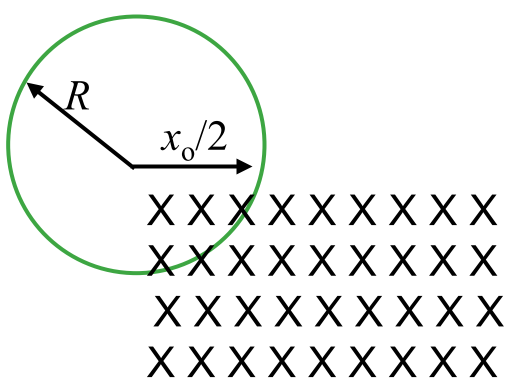
What is B? $v_o = \sqrt{\frac{2qEd}{m}}$



What is the radius of path of particle?

A	B	C	D	E
$R = x_o$	$R = 2x_o$	$R = \frac{1}{2}x_o$	$R = \frac{mv_o}{qB}$	$R = \frac{v_o^2}{a}$

Why?



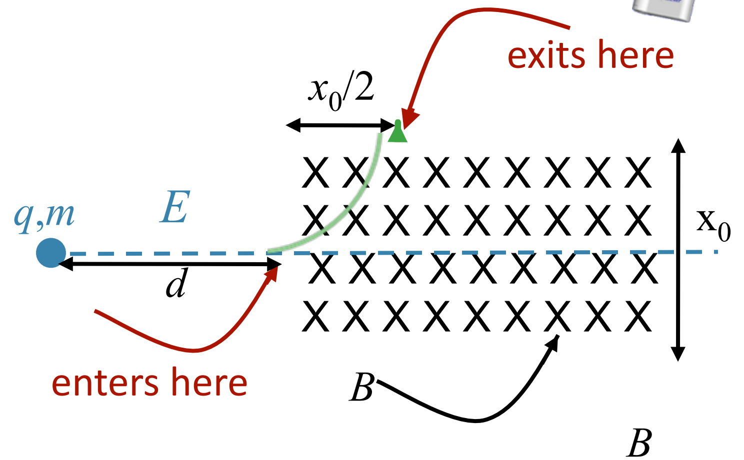
For D, we don't know *B* yet.

Calculation

A particle of charge q and mass m is accelerated from rest by an electric field E through a distance d and enters and exits a region containing a constant magnetic field B at the points shown. Assume q,m,E,d, and x_0 are known.

What is B?

$$v_o = \sqrt{\frac{2qEd}{m}} \qquad R = \tfrac{1}{2}x_0$$



A: $B = \frac{2}{x_o}\sqrt{\frac{2mEd}{q}}$

B: $B = \frac{E}{v}$

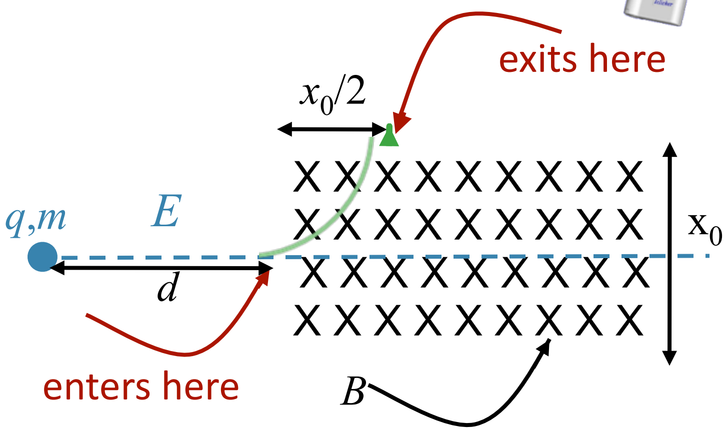
C: $B = E\sqrt{\frac{m}{2qEd}}$

D: $B = \frac{1}{x_o}\sqrt{\frac{2mEd}{q}}$

E: $B = \frac{mv_o}{qx_o}$

Follow-Up

A particle of charge q and mass m is accelerated from rest by an electric field E through a distance d and enters and exits a region containing a constant magnetic field B at the points shown. Assume q,m,E,d, and x_0 are known.

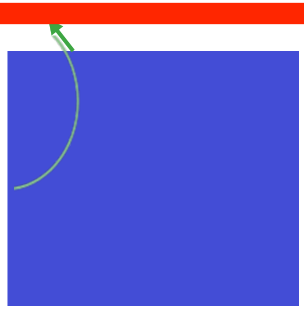


What is B?

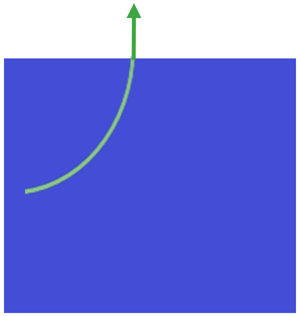
$$B = \frac{2}{x_o}\sqrt{\frac{2mEd}{q}}$$

B

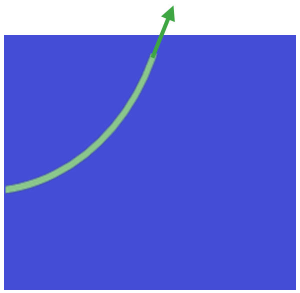
Suppose the charge of the particle is doubled $(Q = 2q)$,while keeping the mass constant. How does the path of the particle change?



A



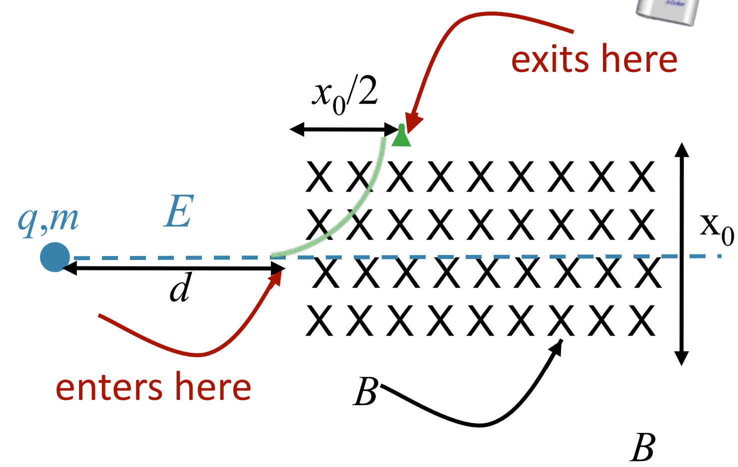
B



C

Follow-Up

A particle of charge q and mass m is accelerated from rest by an electric field E through a distance d and enters and exits a region containing a constant magnetic field B at the points shown. Assume q,m,E,d, and x_0 are known.



What is B?

$$B = \frac{2}{x_o}\sqrt{\frac{2mEd}{q}}$$

Suppose the charge of the particle is doubled $(Q = 2q)$, while keeping the mass constant. How does the path of the particle change?

How does v, the new velocity at the entrance, compare to the original velocity v_0?

A $v = \frac{v_o}{2}$

B $v = \frac{v_o}{\sqrt{2}}$

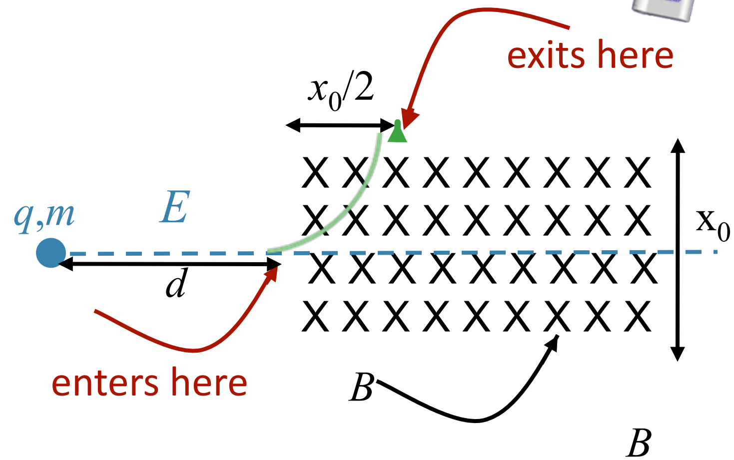
C $v = v_o$

D $v = \sqrt{2}v_o$

E $v = 2v_o$

Follow-Up

A particle of charge q and mass m is accelerated from rest by an electric field E through a distance d and enters and exits a region containing a constant magnetic field B at the points shown. Assume q,m,E,d, and x_0 are known.



What is B?

$$B = \frac{2}{x_o}\sqrt{\frac{2mEd}{q}}$$

Suppose the charge of the particle is doubled $(Q = 2q)$, while keeping the mass constant. How does the path of the particle change?

$$v = \sqrt{2}v_o$$

How does F, the magnitude of the new force at the entrance, compare to F_0, the magnitude of the original force?

A $F = \dfrac{F_o}{\sqrt{2}}$

B $F = F_o$

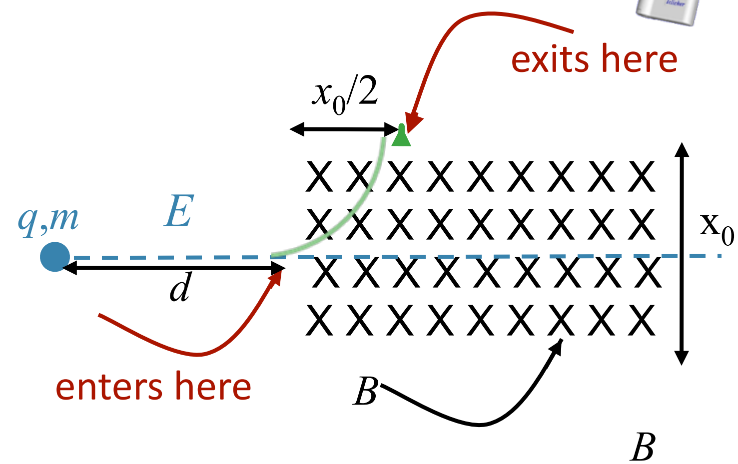
C $F = \sqrt{2}F_o$

D $F = 2F_o$

E $F = 2\sqrt{2}F_o$

Follow-Up

A particle of charge q and mass m is accelerated from rest by an electric field E through a distance d and enters and exits a region containing a constant magnetic field B at the points shown. Assume q,m,E,d, and x_0 are known.



What is B?

$$B = \frac{2}{x_o}\sqrt{\frac{2mEd}{q}}$$

Suppose the charge of the particle is doubled $(Q = 2q)$,while keeping the mass constant. How does the path of the particle change?

$$v = \sqrt{2}v_o \qquad F = 2\sqrt{2}F_o$$

How does R, the radius of curvature of the path, compare to R_0, the radius of curvature of the original path?

A $R = \frac{R_o}{2}$

B $R = \frac{R_o}{\sqrt{2}}$

C $R = R_o$

D $R = \sqrt{2}R_o$

E $R = 2R_o$

$$\frac{mv^2}{R} = F$$

$$R = \frac{mv^2}{F}$$

$$R = \frac{m2v_0^2}{2\sqrt{2}F_0} = \frac{mv_0^2}{\sqrt{2}F_0} = \frac{1}{\sqrt{2}}R_0$$