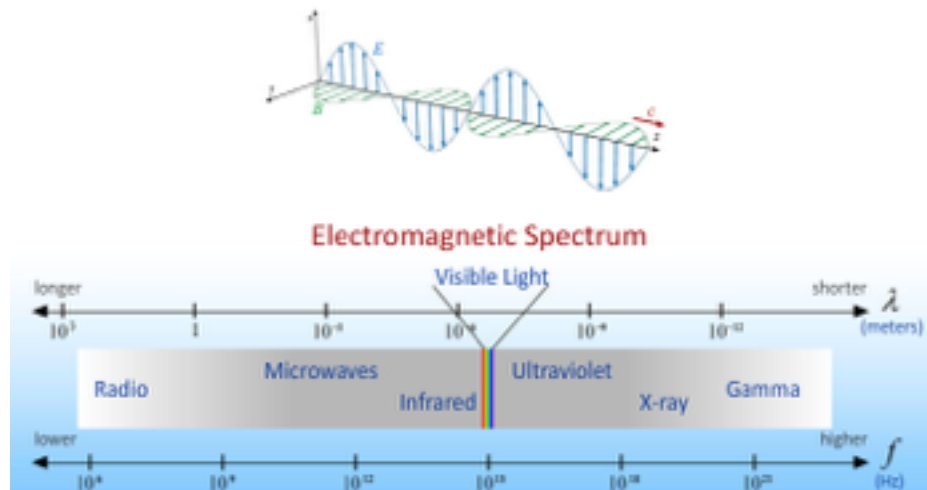


# Electricity & Magnetism

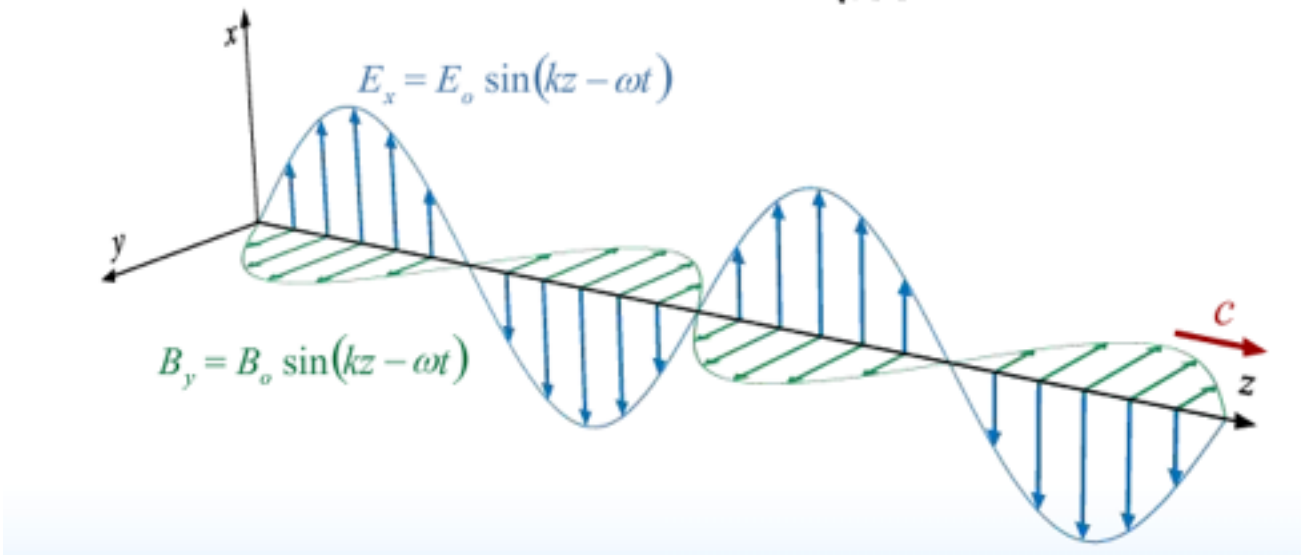
## Lecture 23

### PROPERTIES of ELECTROMAGNETIC WAVES



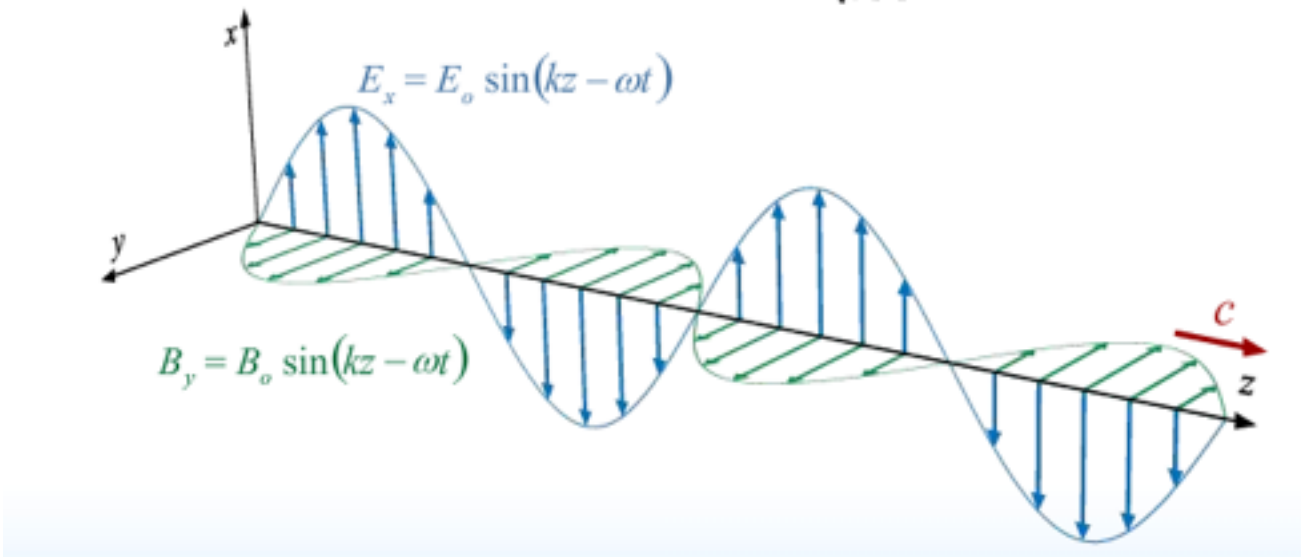
# Plane Waves from Last Time

Velocity  $c = \frac{\omega}{k} = \frac{1}{\sqrt{\mu_0 \epsilon_0}} = \frac{E_0}{B_0} = 3 \times 10^8 \text{ m/s}$



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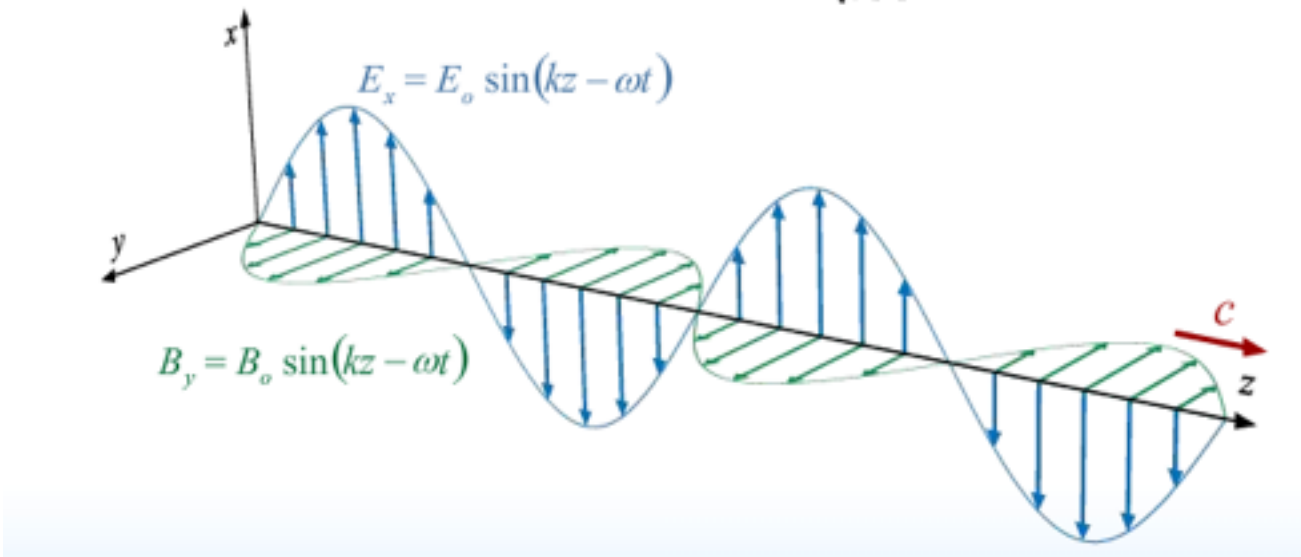
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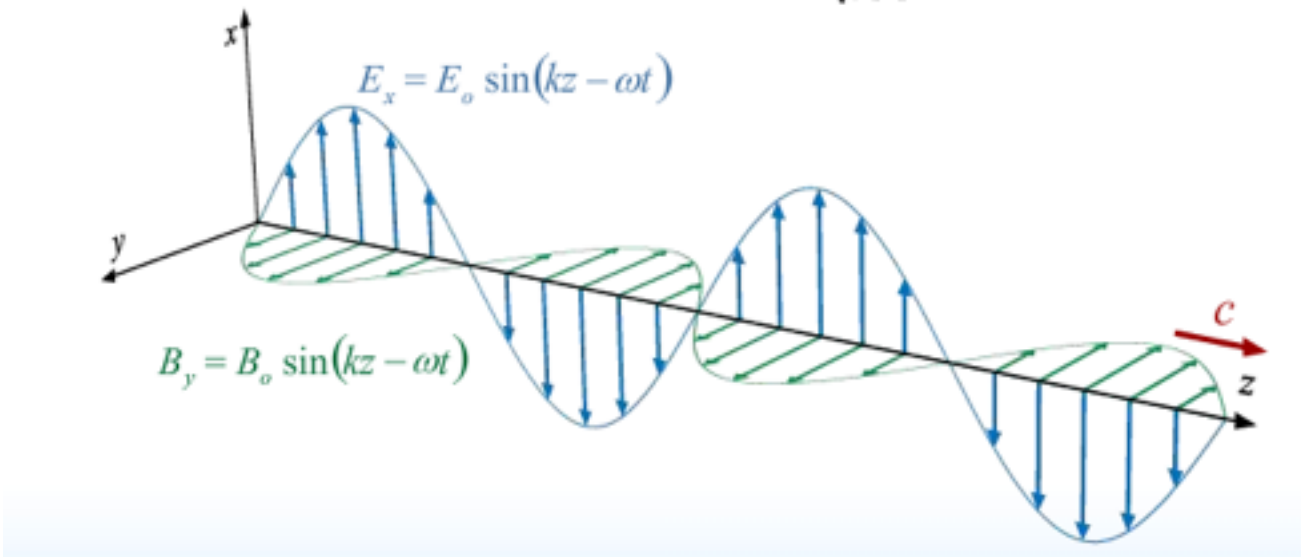


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Oscillate in time and space

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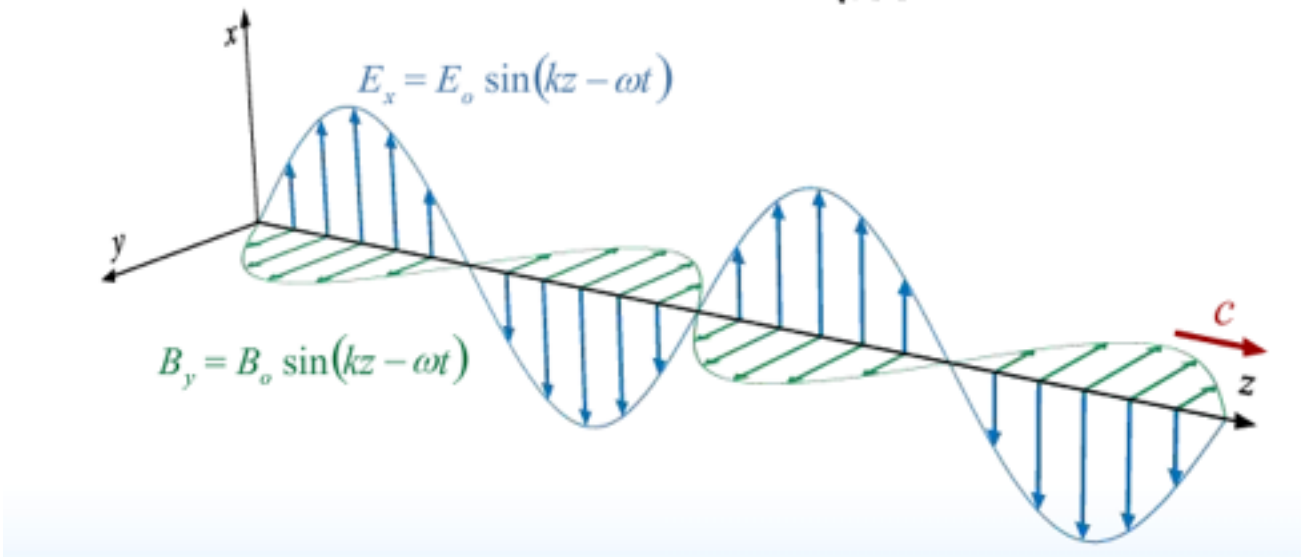
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Direction of propagation given by  $E \times B$

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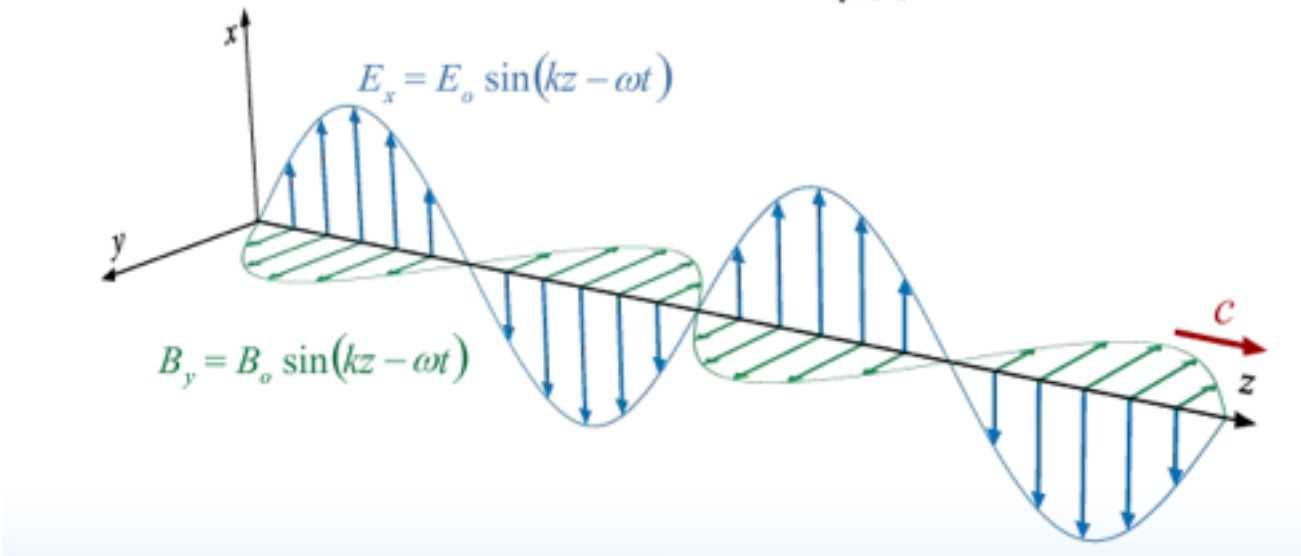
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$$B_0 = E_0/c$$

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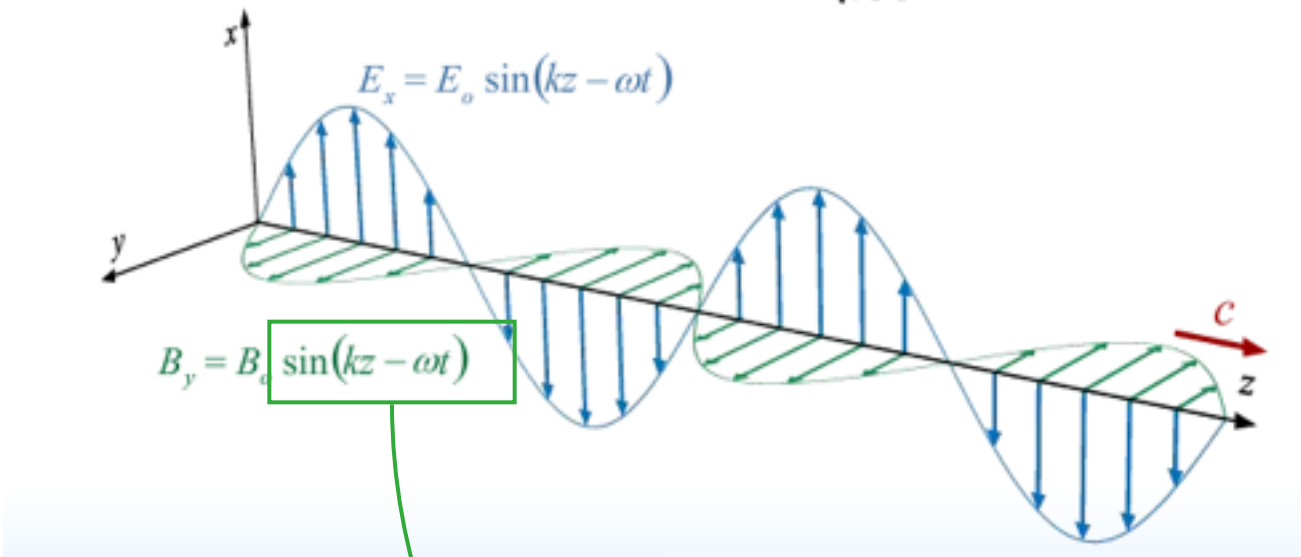
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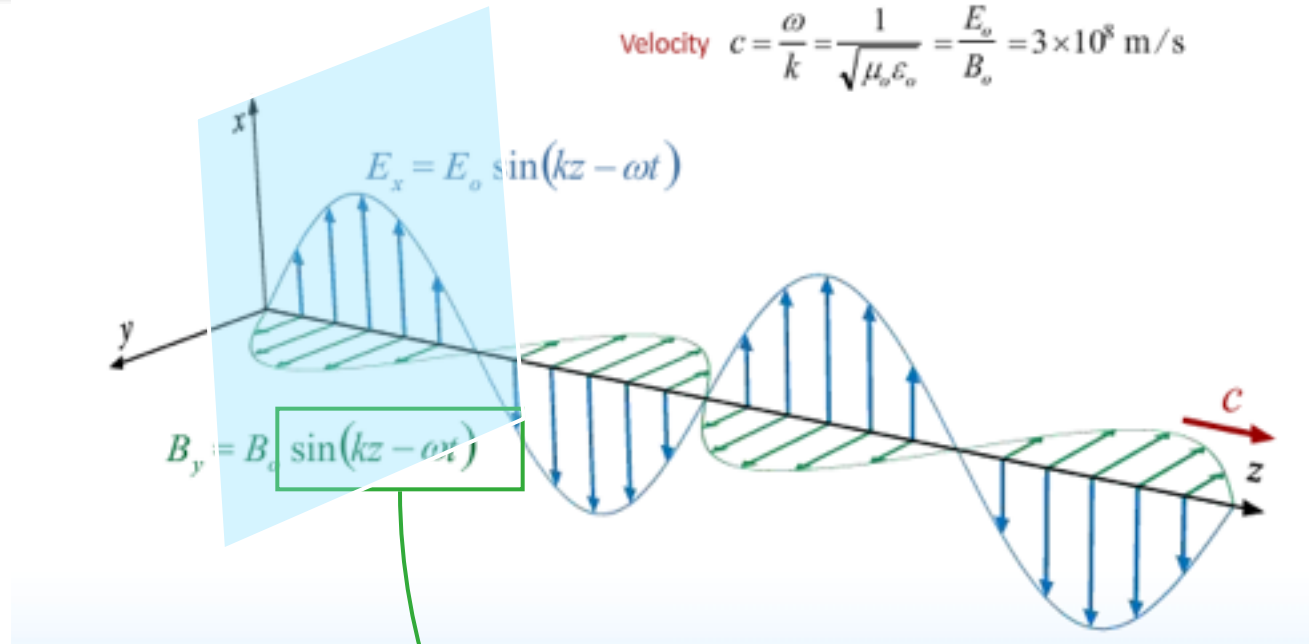
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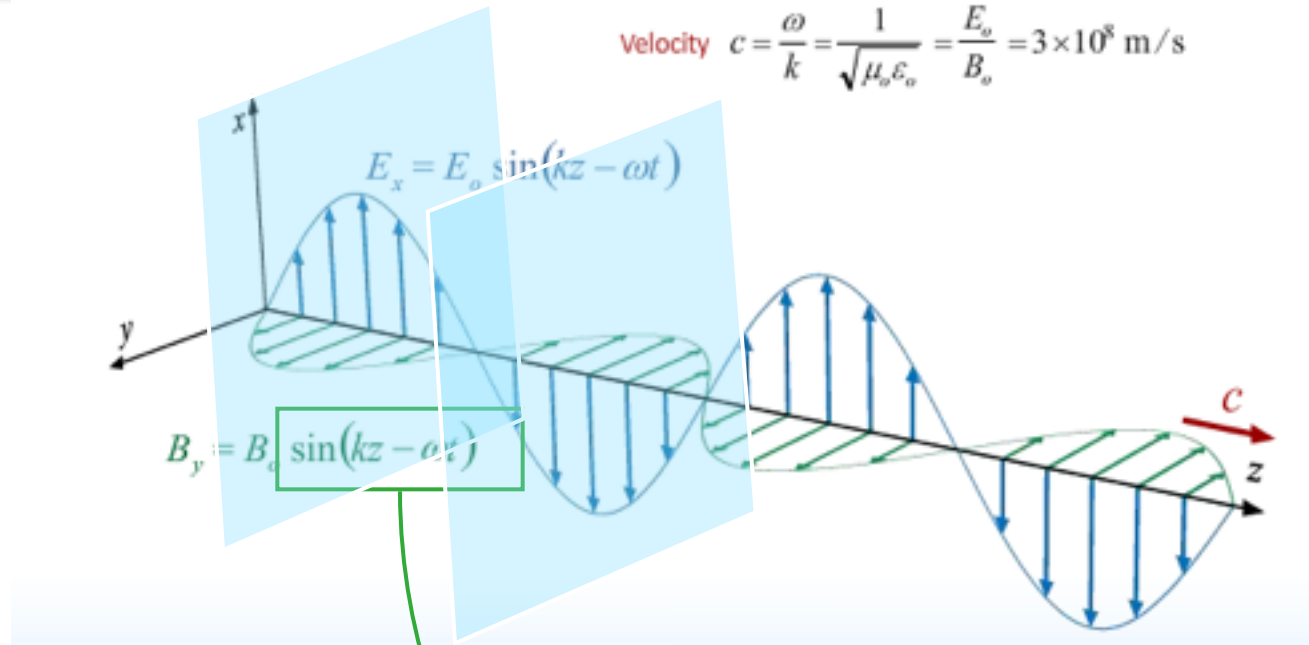
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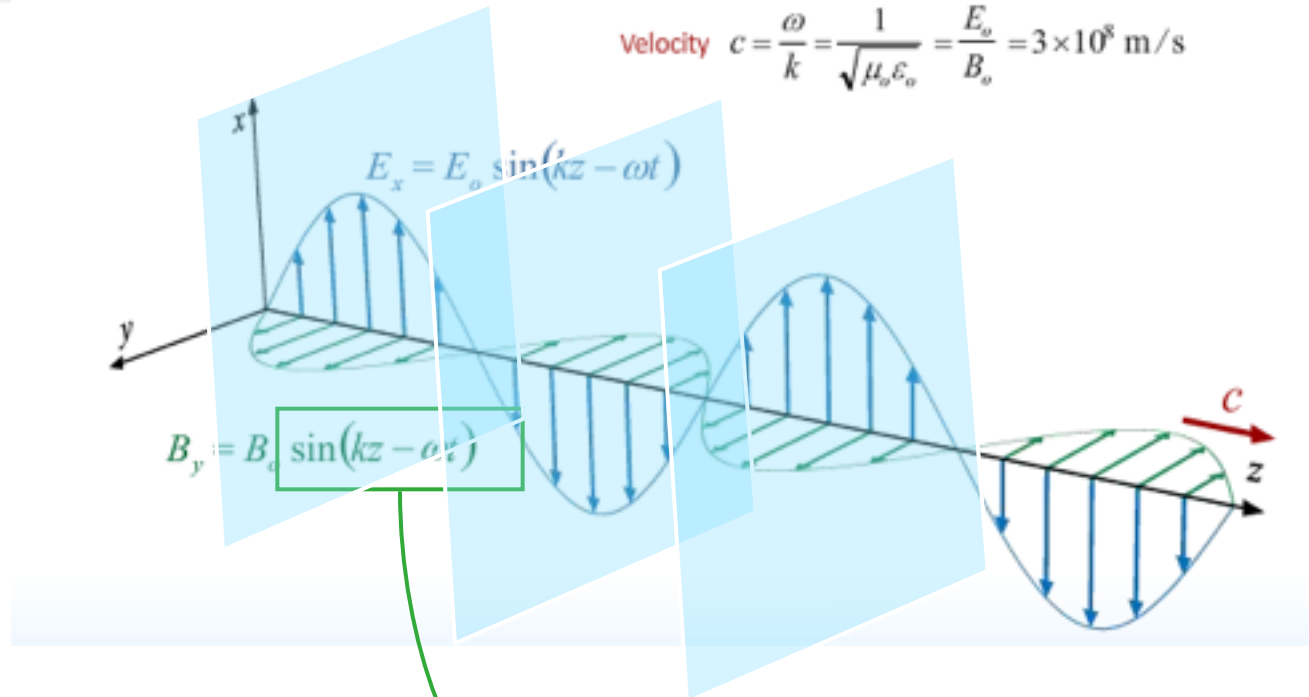
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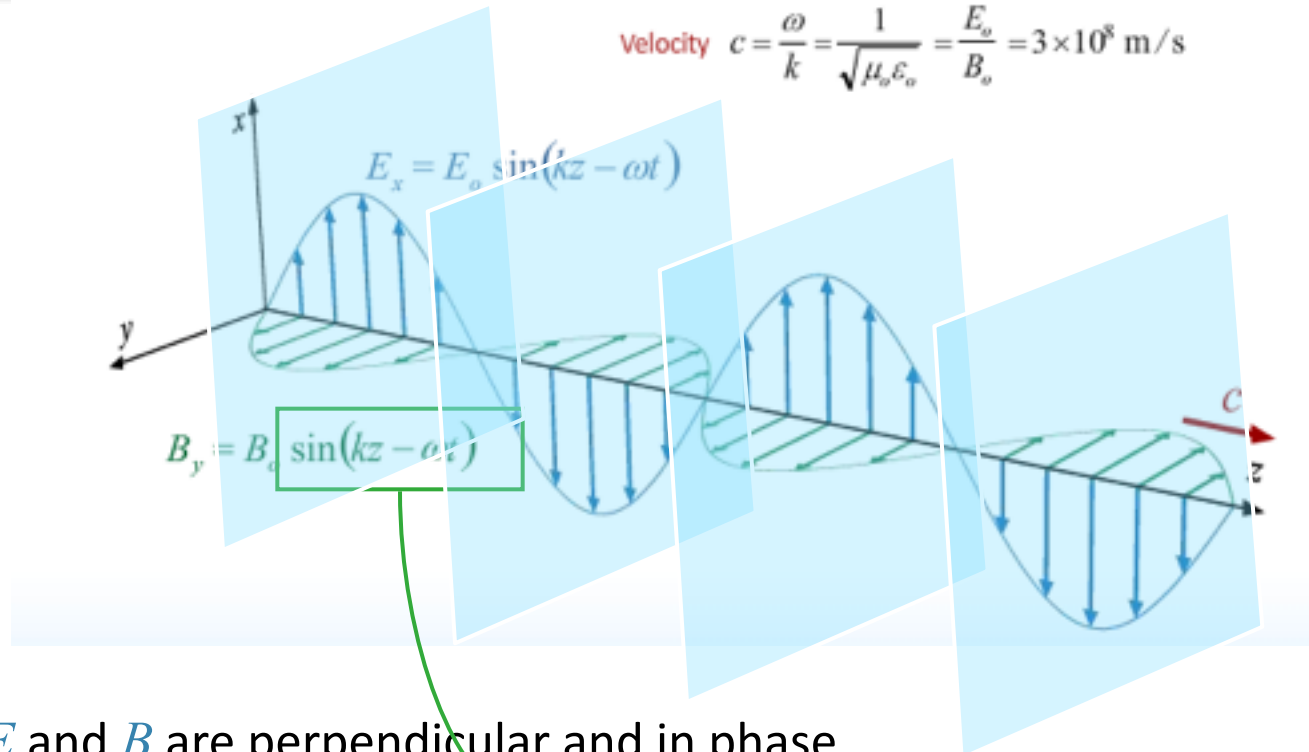
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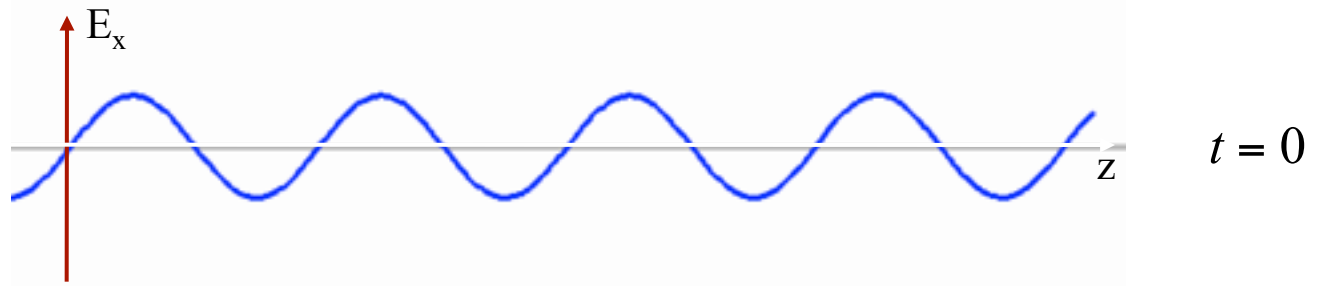
# *Understanding the speed and direction of the wave*

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$$E_x = E_0 \sin(kz - \omega t)$$

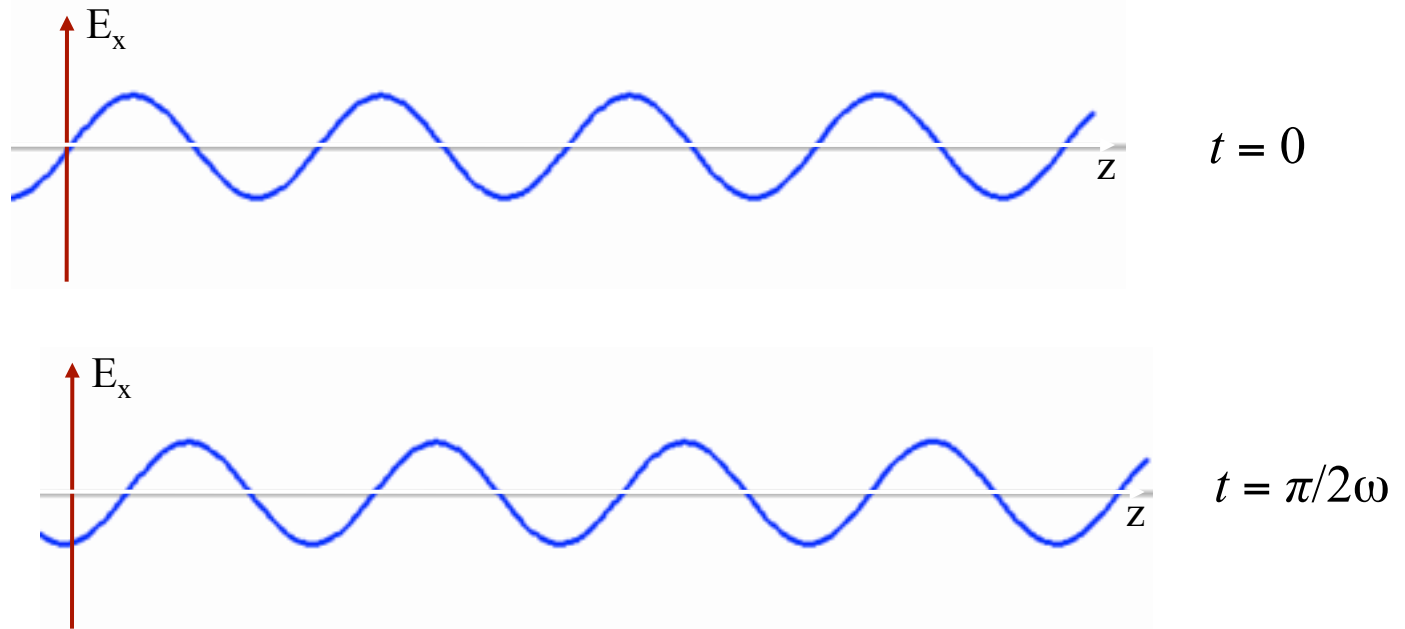
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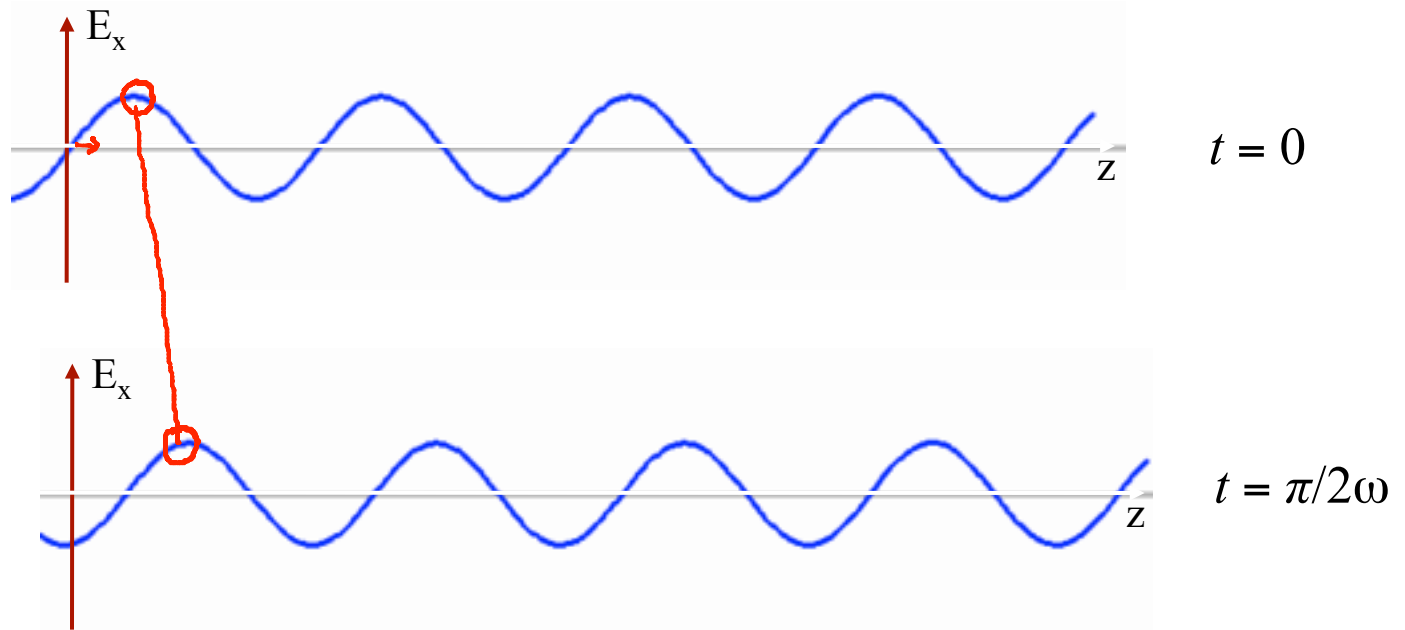
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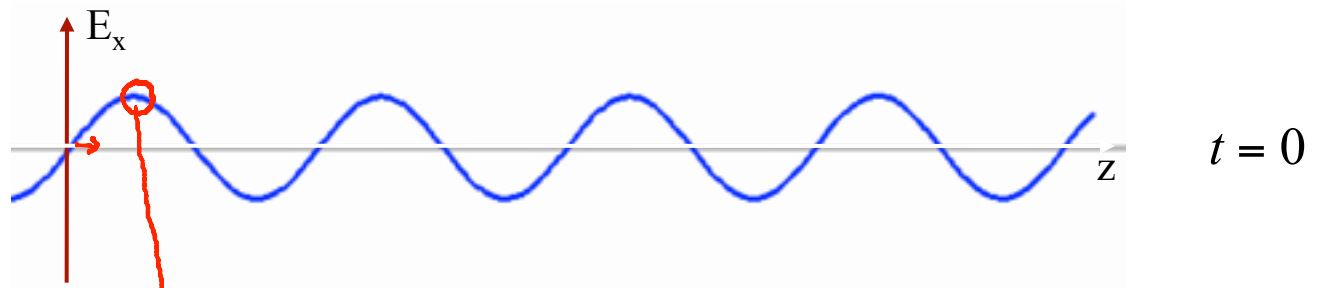
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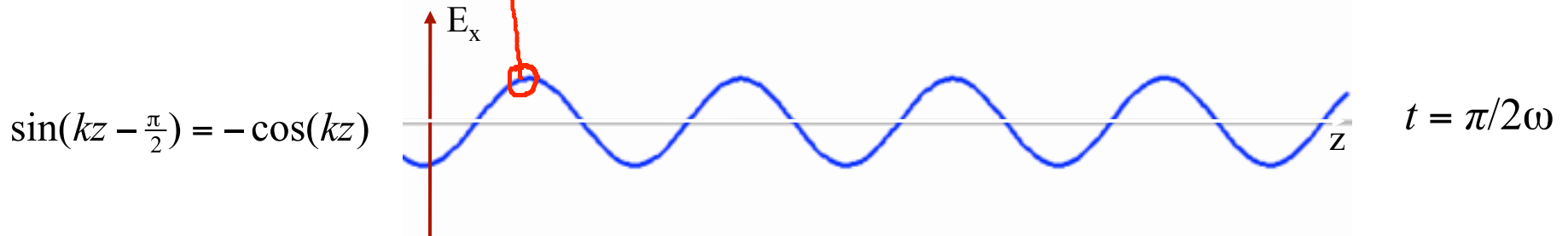


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$t = 0$

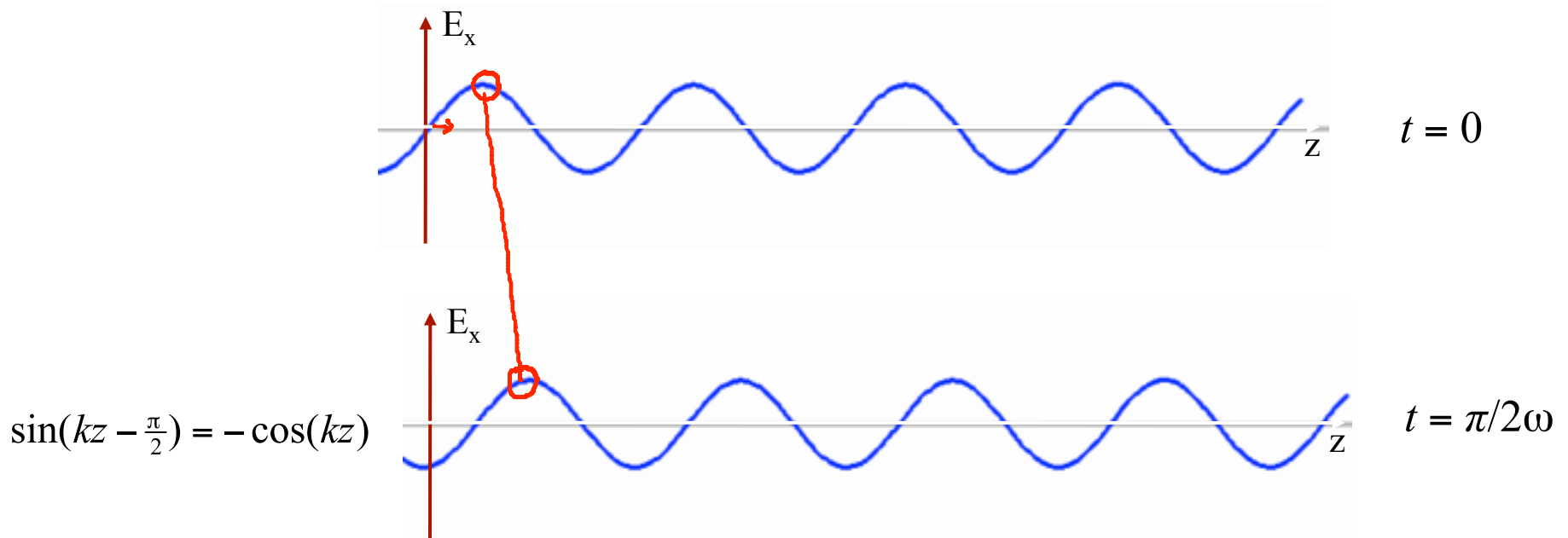


$t = \pi/2\omega$

$$\sin(kz - \frac{\pi}{2}) = -\cos(kz)$$

# Understanding the speed and direction of the wave

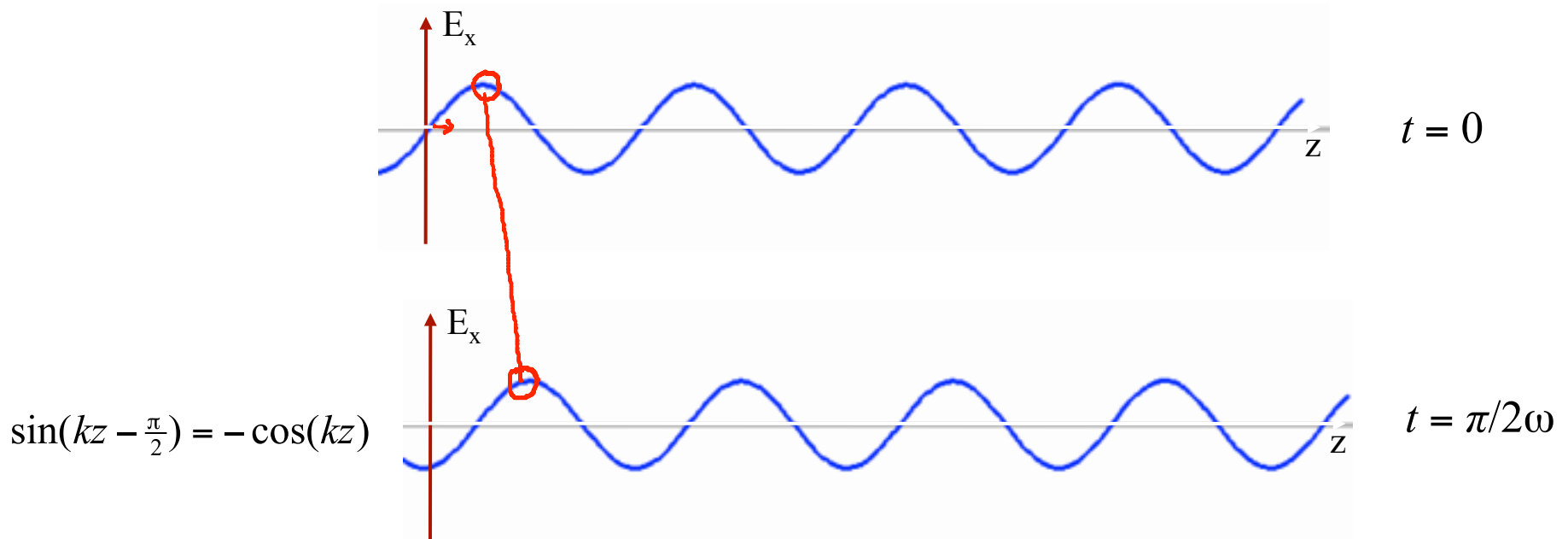
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What has happened to the wave form in this time interval?

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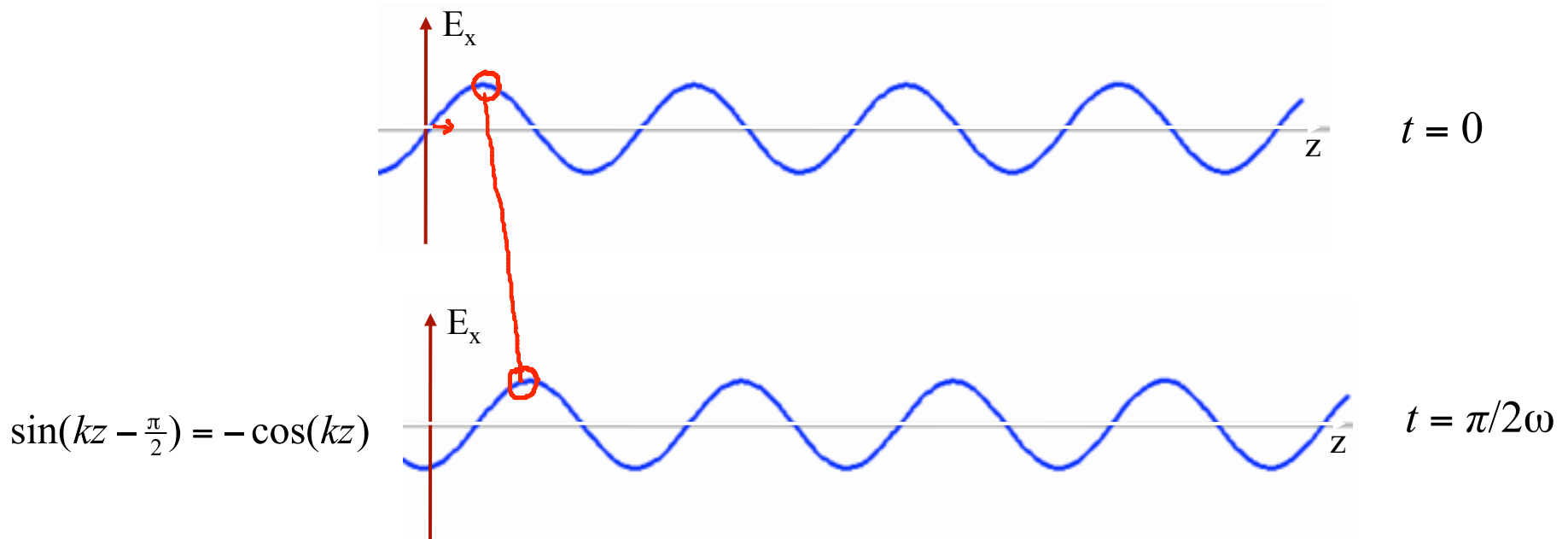


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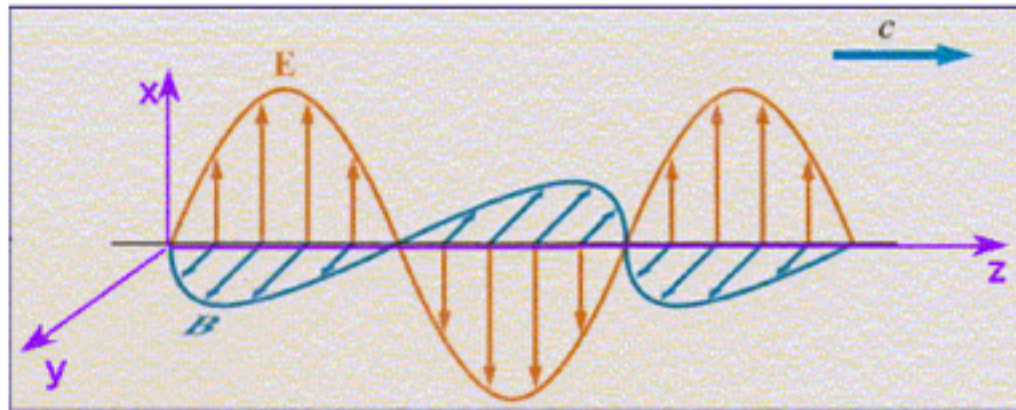


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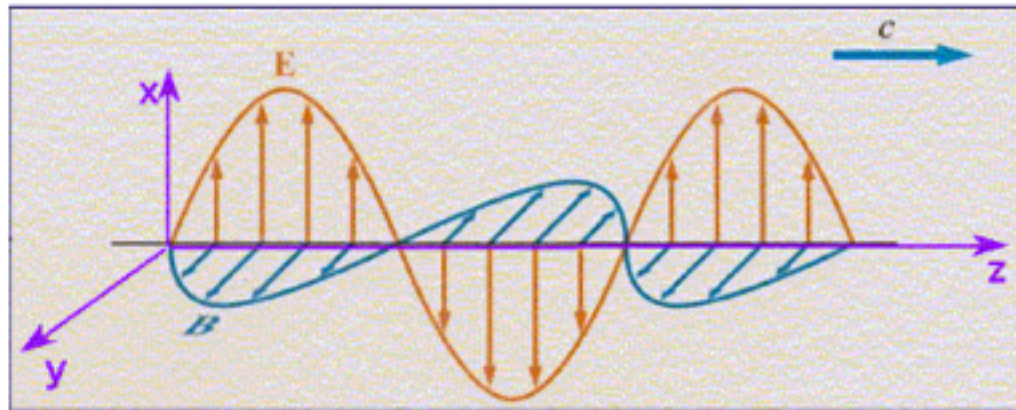
# CheckPoint 2



Which equation correctly describes this electromagnetic wave?

- ☐  $E_x = E_o \sin(kz + \omega t)$
- ☐  $E_y = E_o \sin(kz - \omega t)$
- ☐  $B_y = B_o \sin(kz - \omega t)$

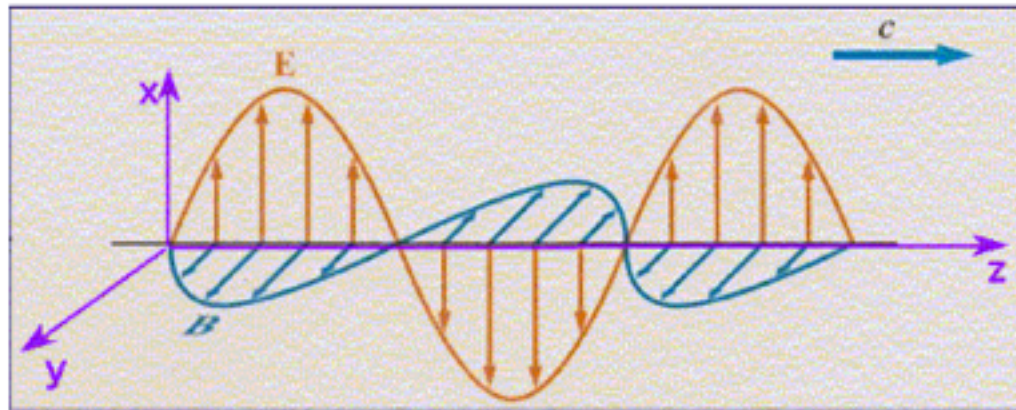
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Which equation correctly describes this electromagnetic wave?

- ☐  $E_x = E_o \sin(kz \oplus \omega t)$  No – moving in the minus  $z$  direction
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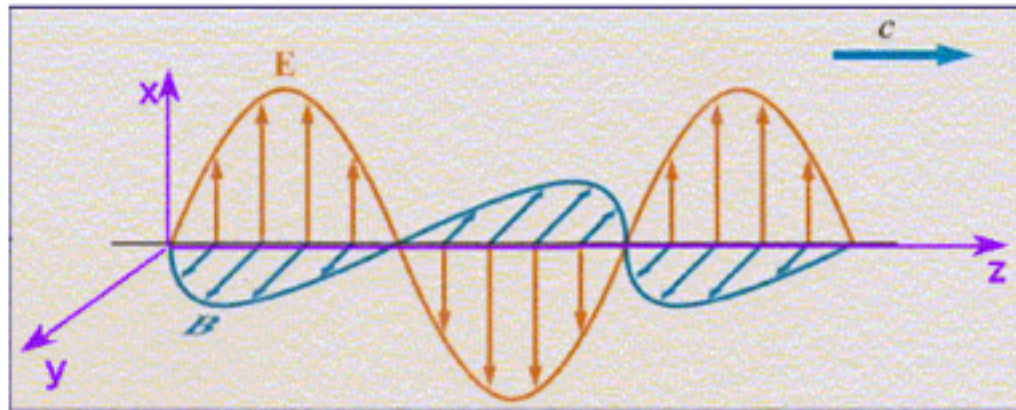
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The equation for the x-component of the electric field of a plane electromagnetic wave is given by:  $E_x = E_o \sin(kz - \omega t)$

Which of the following equations describes the associated magnetic field?

- A)  $B_y = E_o c \sin(kz - \omega t)$
- B)  $B_y = (E_o/c) \sin(kz - \omega t)$
- C)  $B_y = E_o c \cos(kz - \omega t)$
- D)  $B_y = (E_o/c) \cos(kz - \omega t)$



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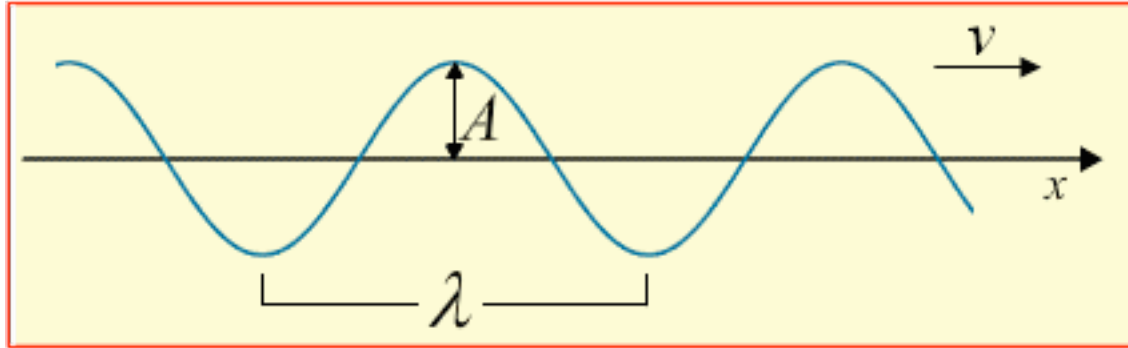
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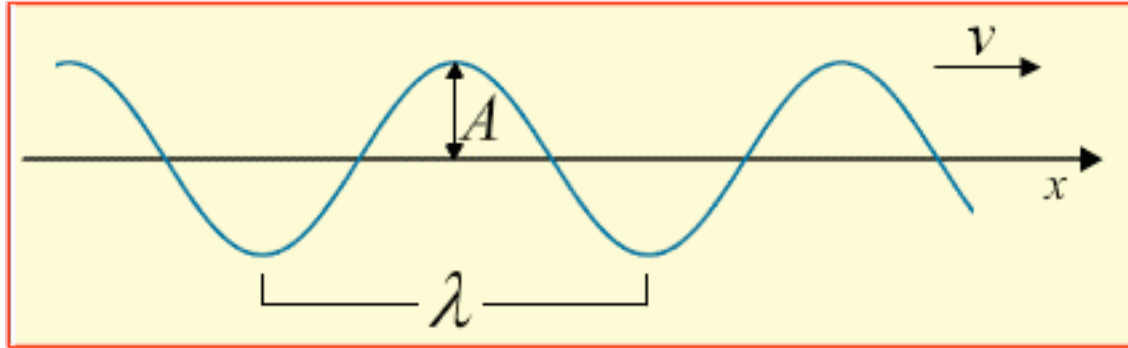
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# Prelecture question



- Which of the following statements does not correctly describe a harmonic plane wave traveling in some medium.
- A) The time taken by any point of the wave to make one complete oscillation does not depend on the amplitude.
  - B) Doubling the wavelength of the wave will halve its frequency.
  - C) Doubling the amplitude has no effect on the wavelength.
  - D) Doubling the frequency of the wave will double its speed.

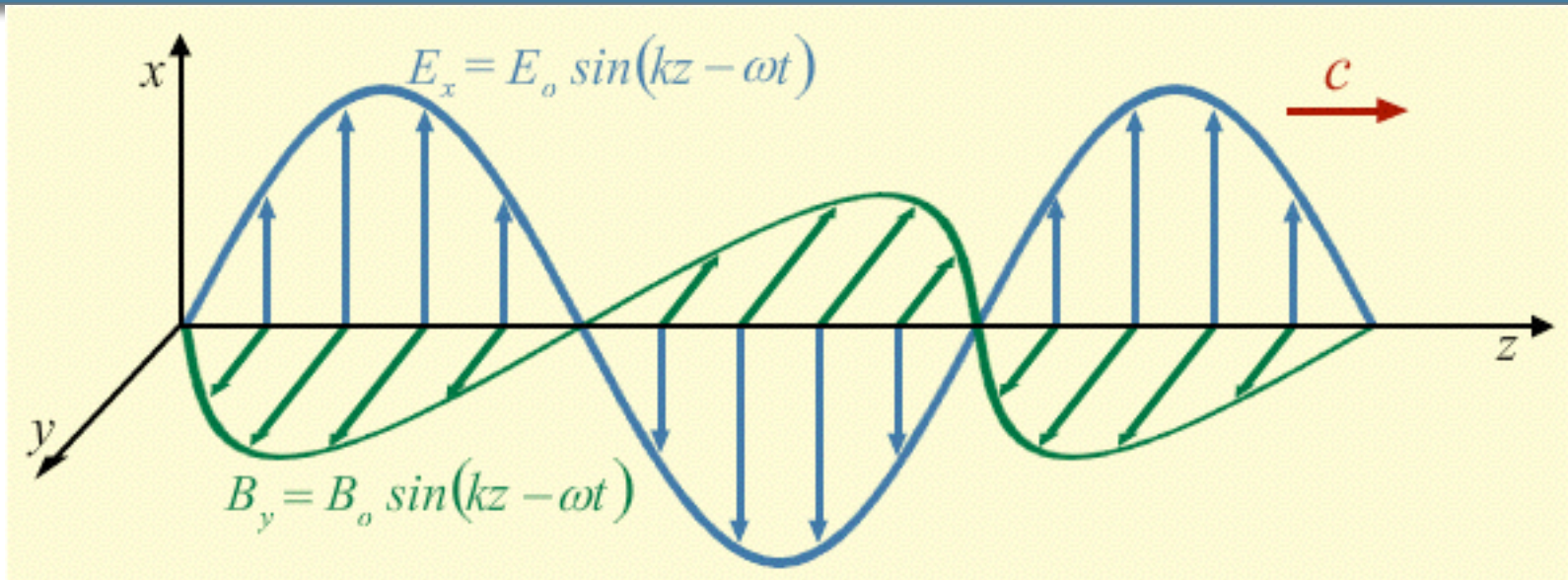
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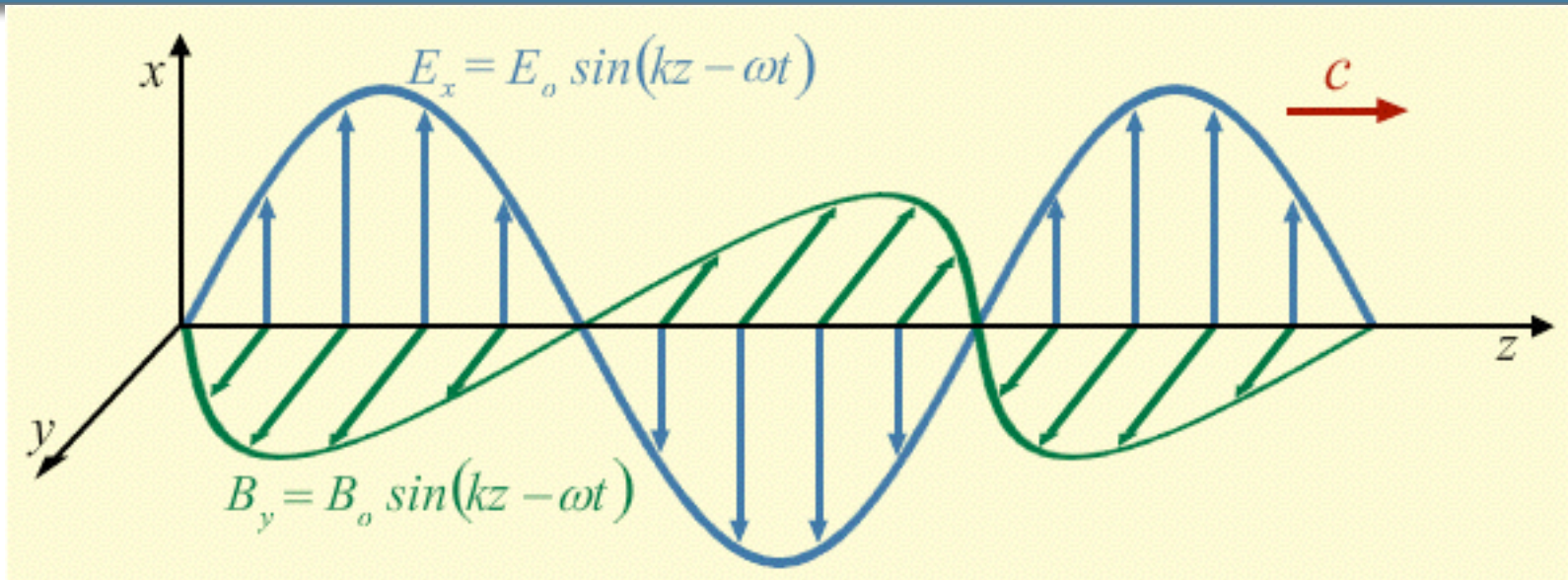
# Prelecture



An electromagnetic wave is traveling through free space and the magnitudes of its electric and magnetic fields are  $E_o$  and  $B_o$  respectively. It then passes through a filter that cuts the magnitude of the electric field by a quarter ( $E = E_o/4$ ). What happens to the magnitude of the magnetic field?

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The color of the stars we observe in galaxies can be used to deduce the velocity of the galaxy relative to Earth.

Suppose the average color of the stars in a newly discovered galaxy is **bluer** than the average color of stars in our own galaxy. What would be a sensible conclusion about the motion of the new galaxy relative to our own?

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# CheckPoint 6



Your iclicker operates at a frequency of approximately 900 MHz ( $900 \times 10^6$  Hz). What is the approximately wavelength of the EM wave produced by your iclicker?

- ☐ 0.03 meters
- ☐ 0.3 meters
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$$C = 3.0 \times 10^8 \text{ m/s}$$

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Check:

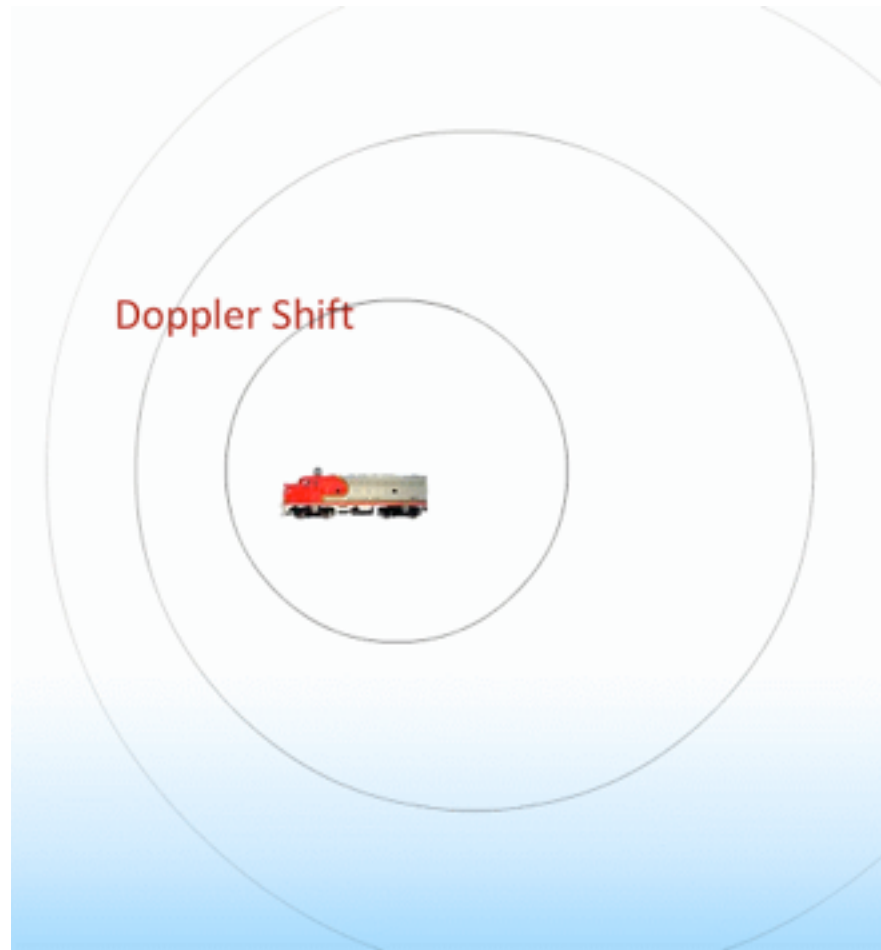
Look at size of antenna on base unit

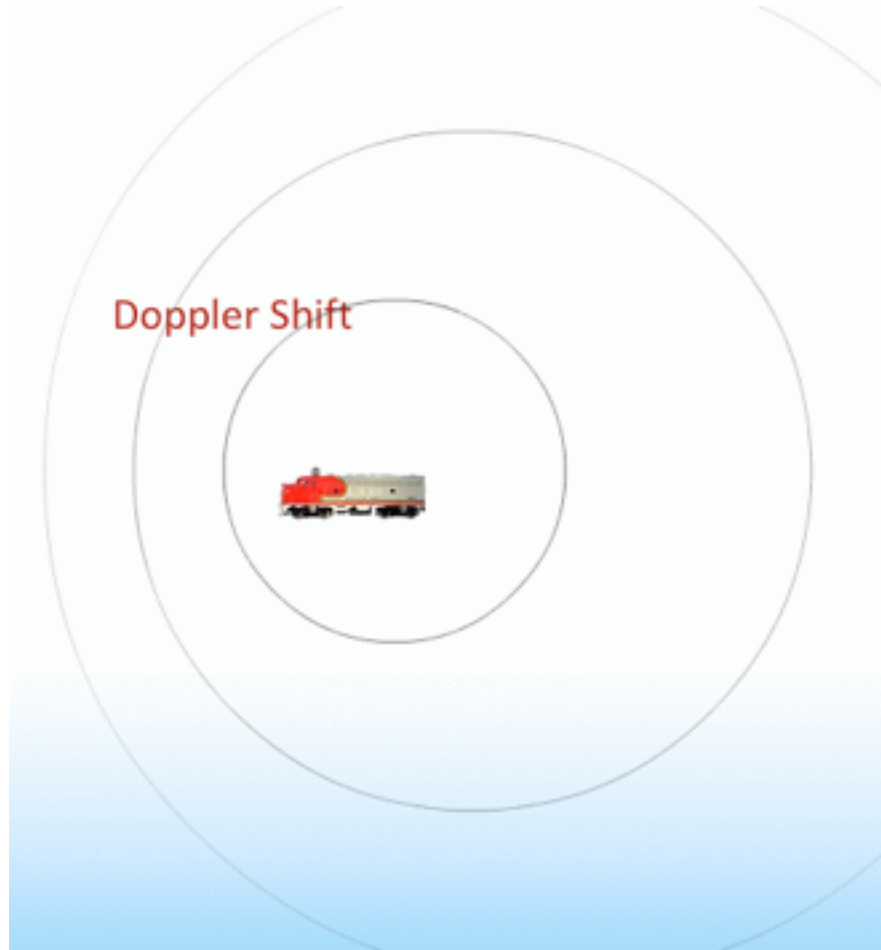
Paris Ambulance

# *Doppler Shift*

Dr Chai

Demo





## The Big Idea

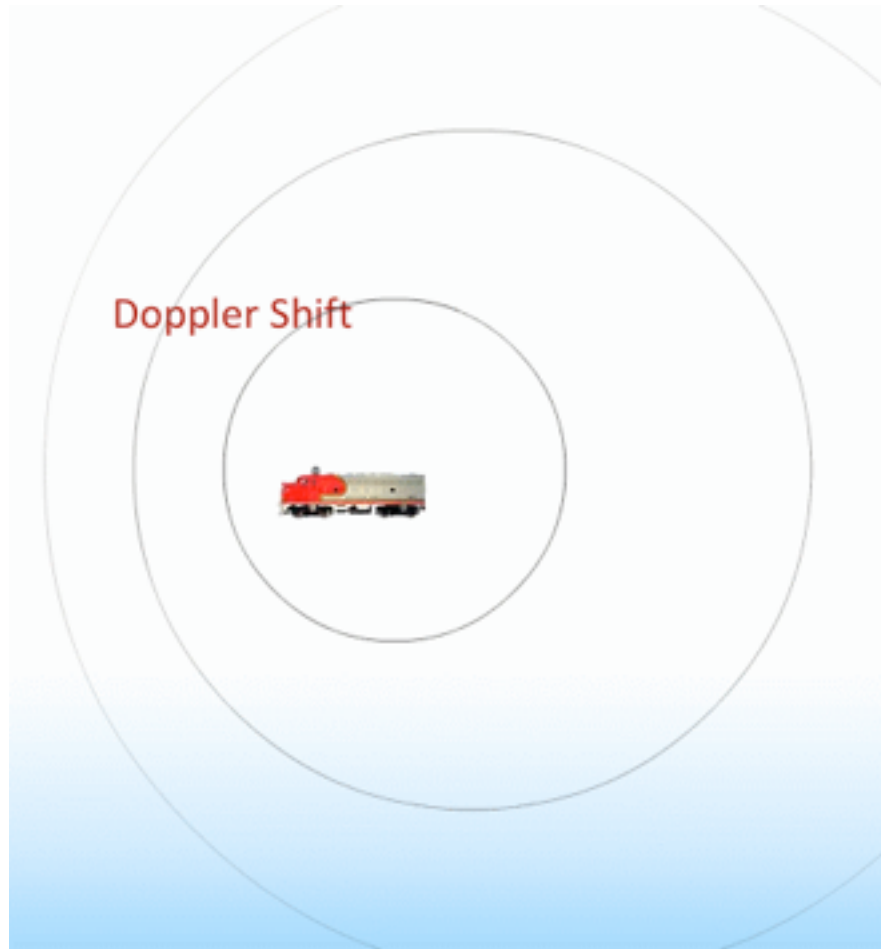
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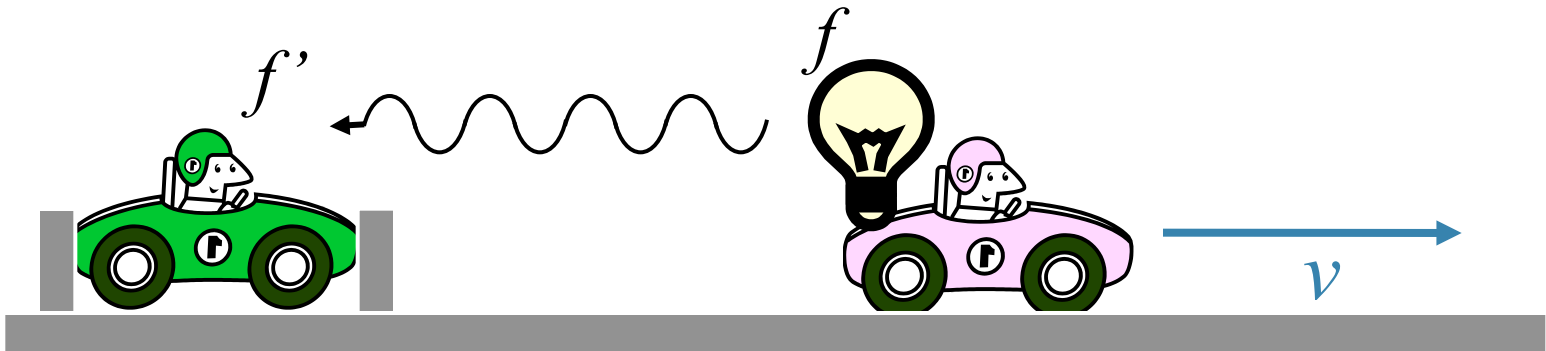
$$\beta = v/c$$

$\beta > 0$  if source & observer are approaching

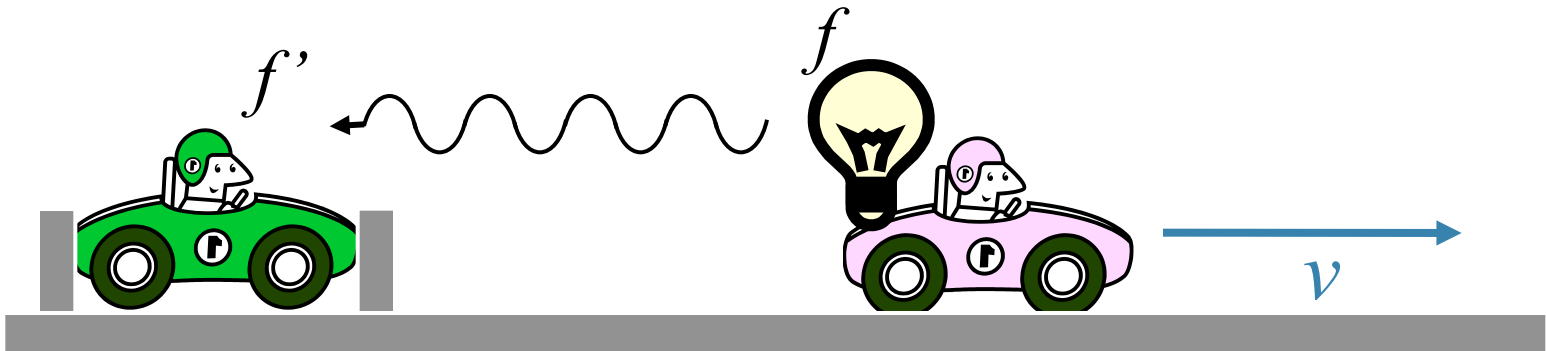
$\beta < 0$  if source & observer are separating

# *Doppler Shift for E-M Waves*

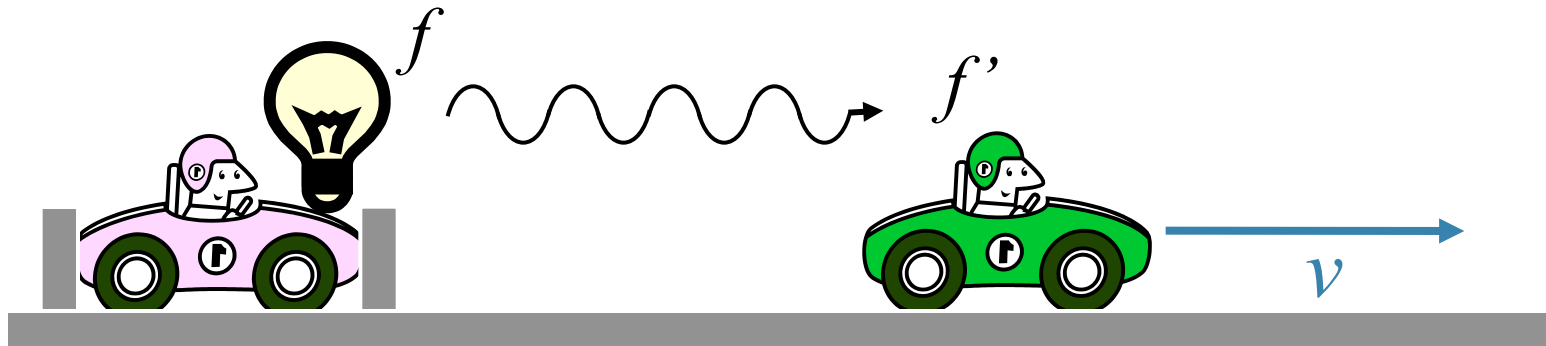
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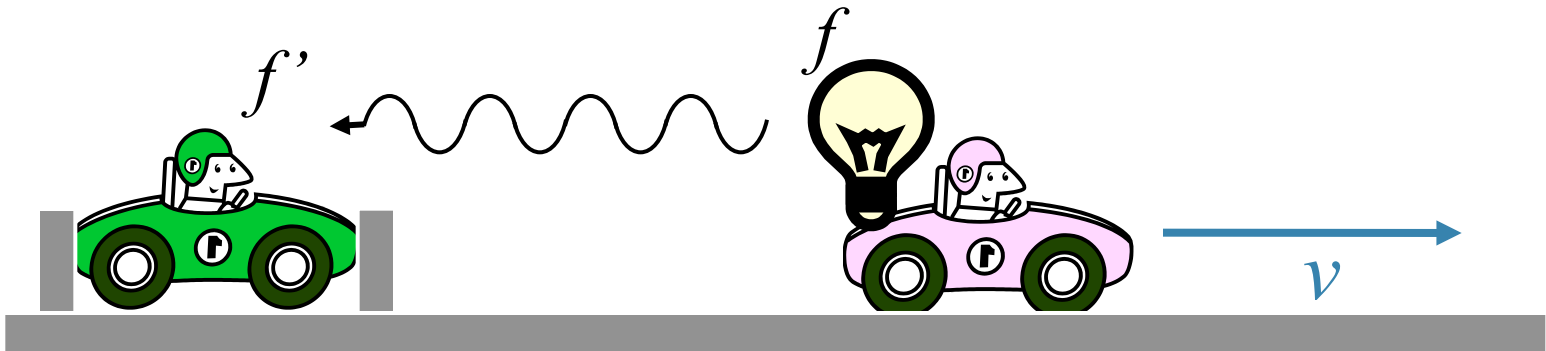
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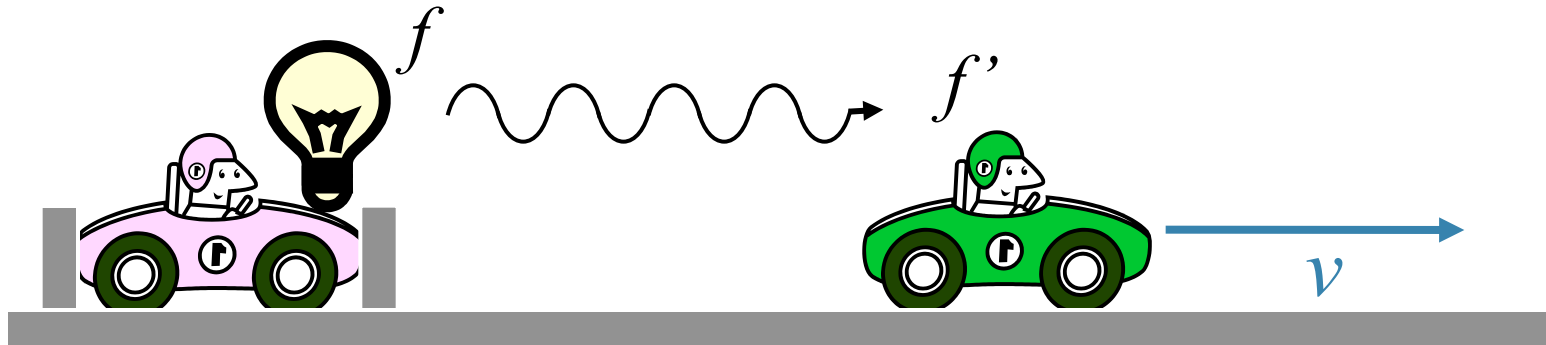
or



# Doppler Shift for E-M Waves



or



The Doppler Shift is the SAME for both cases!

$f'/f$  only depends on the relative velocity

$$f' = f \sqrt{\frac{1 + \beta}{1 - \beta}}$$

# *Doppler Shift for E-M Waves*

## A Note on Approximations

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$$f' = f \sqrt{\frac{1 + \beta}{1 - \beta}} \quad \xrightarrow{\beta \ll 1} \quad f' \approx f(1 + \beta)$$

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Evaluate:

$$F(0) = 1$$

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$$f' = f \sqrt{\frac{1 + \beta}{1 - \beta}} \quad \xrightarrow{\beta \ll 1} \quad f' \approx f(1 + \beta)$$

why?

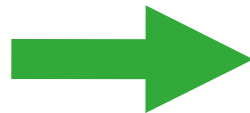
Taylor Series: Expand  $F(\beta) = \left(\frac{1 + \beta}{1 - \beta}\right)^{1/2}$  around  $\beta = 0$

$$F(\beta) = F(0) + \frac{F'(0)}{1!} \beta + \frac{F''(0)}{2!} \beta^2 + \dots$$

Evaluate:

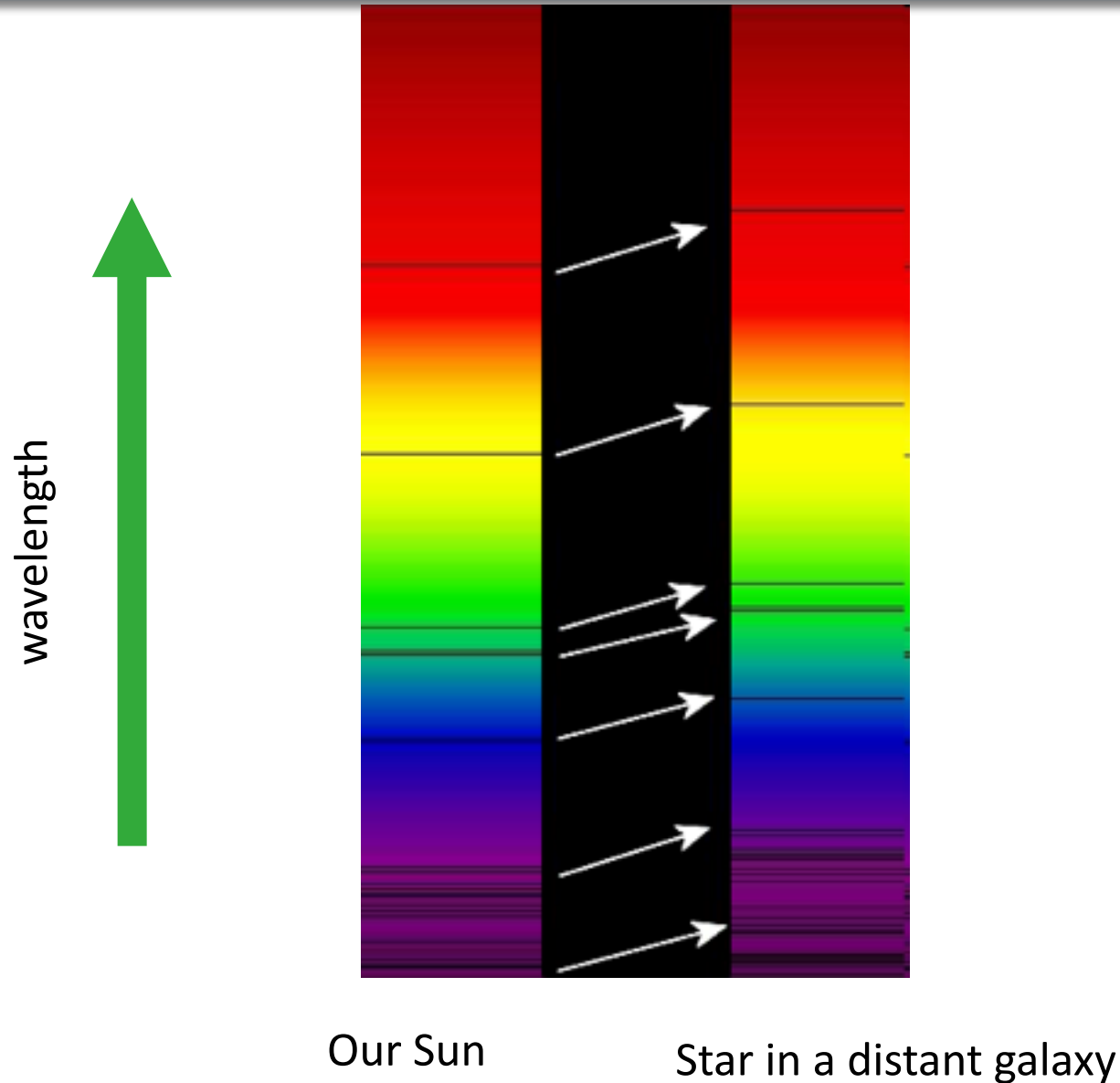
$$F(0) = 1$$

$$F'(0) = 1$$

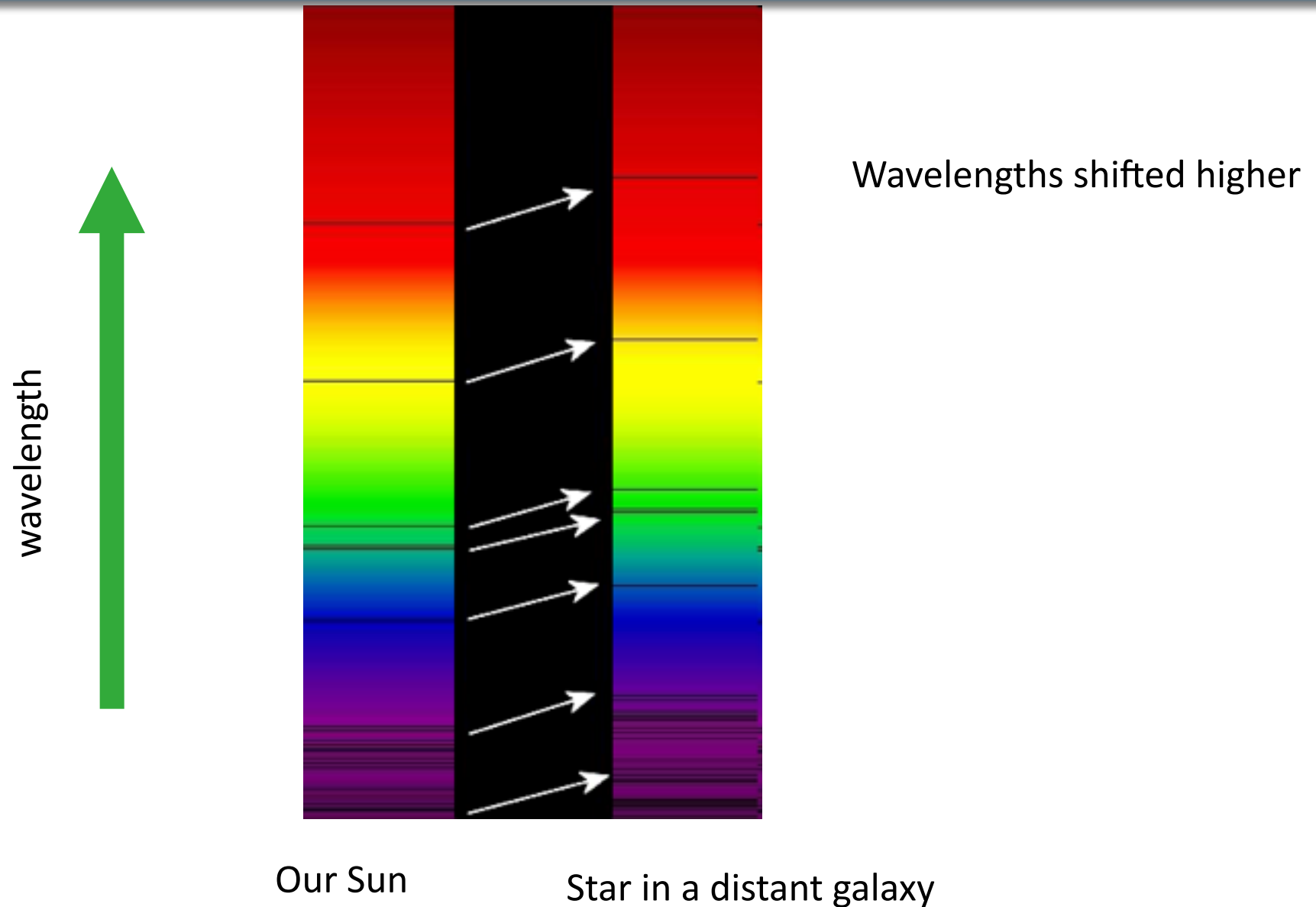


$$F(\beta) \approx 1 + \beta$$

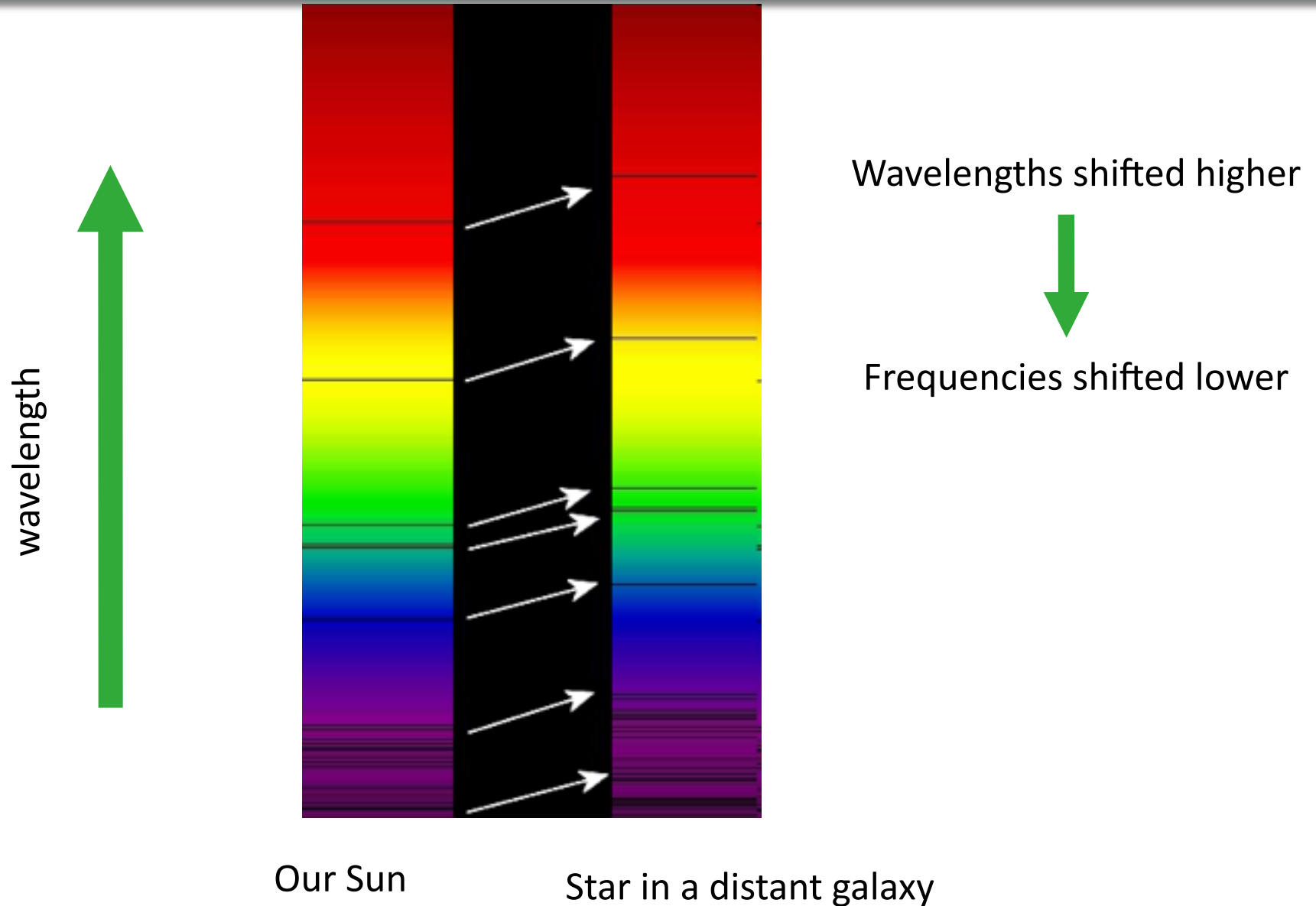
# Red Shift of Stellar Spectra



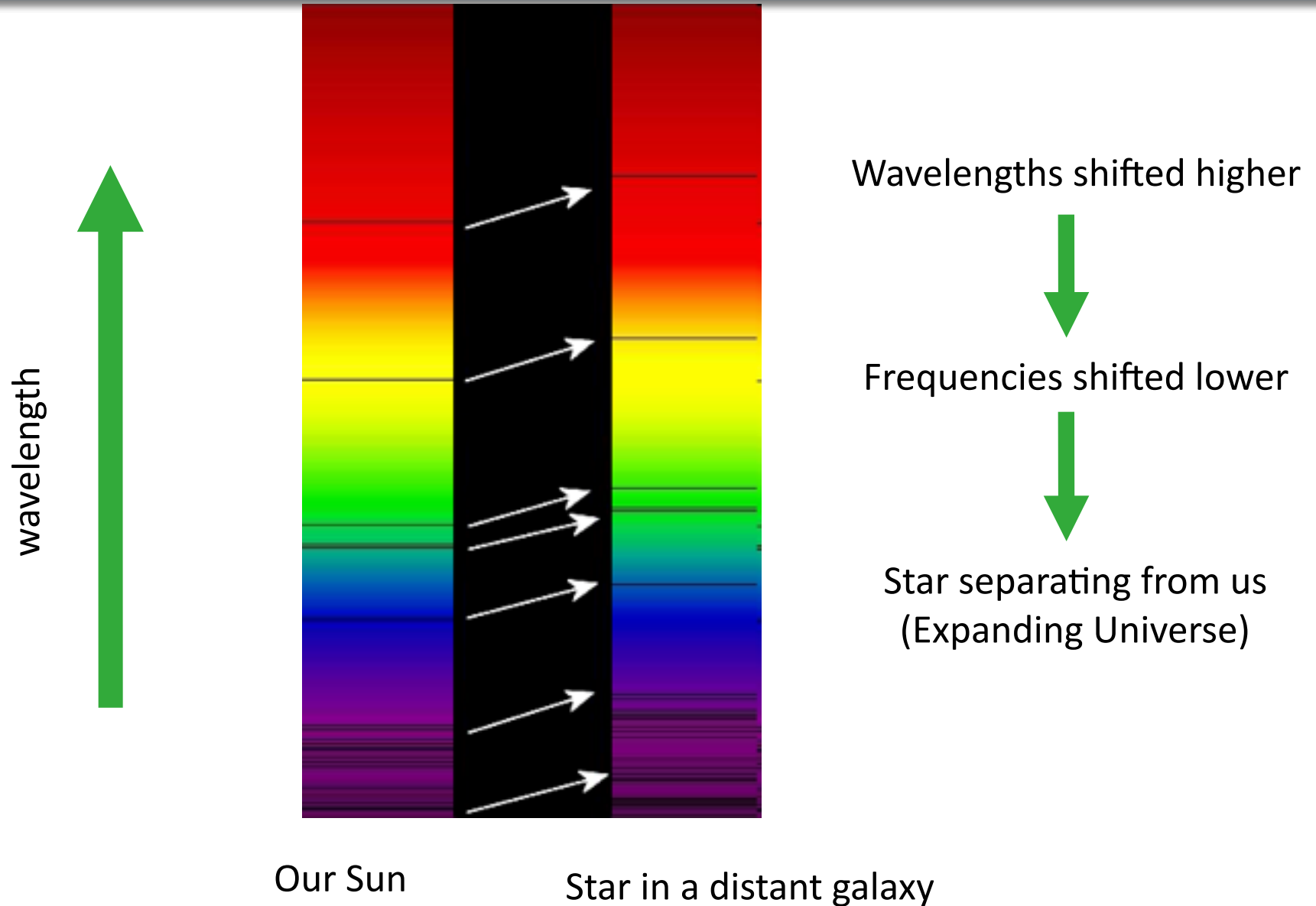
# Red Shift of Stellar Spectra



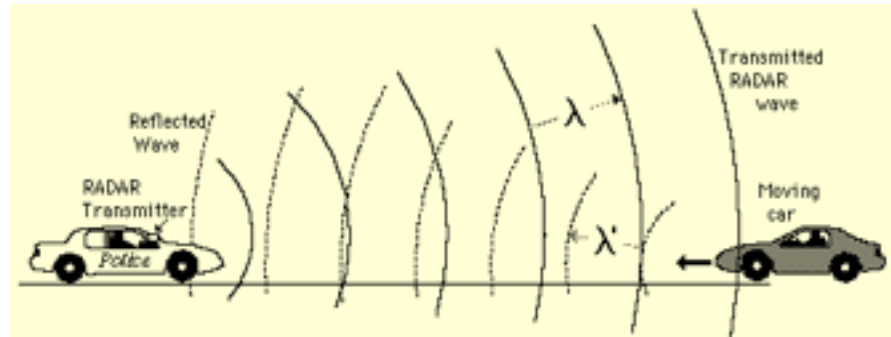
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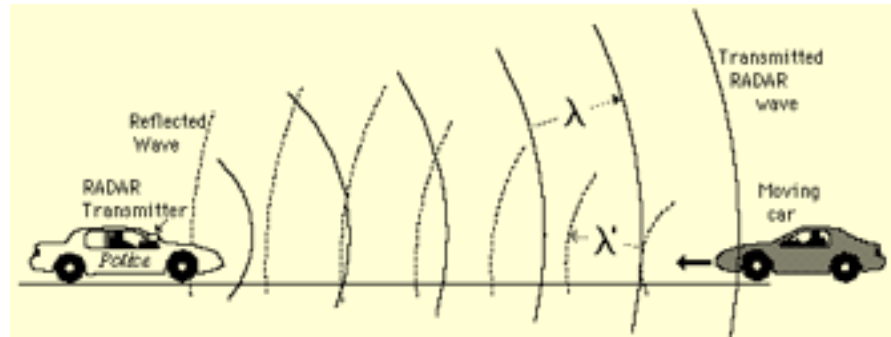
# Example



Police radars get twice the effect since the EM waves make a round trip:

$$f' \approx f(1 + 2\beta)$$

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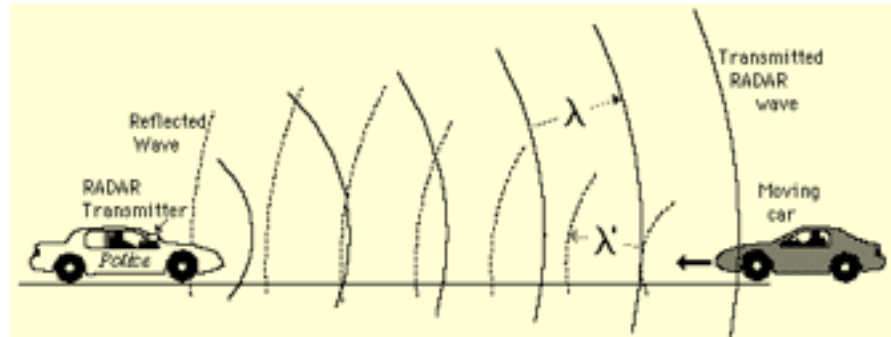
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If  $f = 24,000,000,000$  Hz (k-band radar gun)

$c = 300,000,000$  m/s

# Example



Police radars get twice the effect since the EM waves make a round trip:

$$f' \approx f(1 + 2\beta)$$

If  $f = 24,000,000,000$  Hz (k-band radar gun)

$c = 300,000,000$  m/s

$v$	$\beta$	$f'$	$f' - f$
30 m/s (108 km/h)	$1.000 \times 10^{-7}$	24,000,004,800	4800 Hz
31 m/s (112 km/h)	$1.033 \times 10^{-7}$	24,000,004,959	4959 Hz

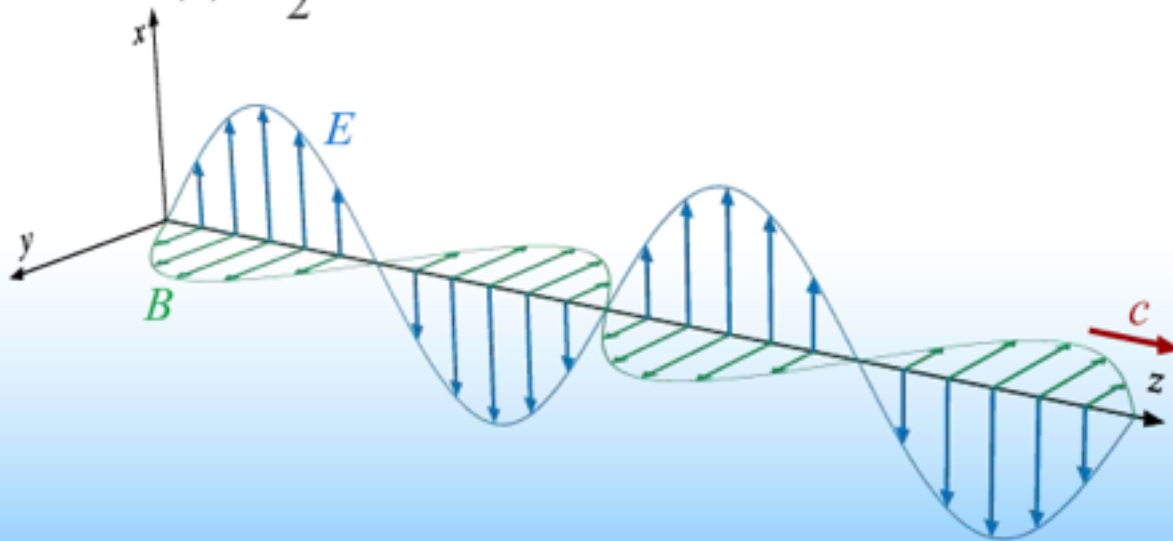
# Waves Carry Energy

Total Energy Density

$$u = \epsilon_o E^2$$

Average Energy Density

$$\langle u \rangle = \frac{1}{2} \epsilon_o E_o^2$$



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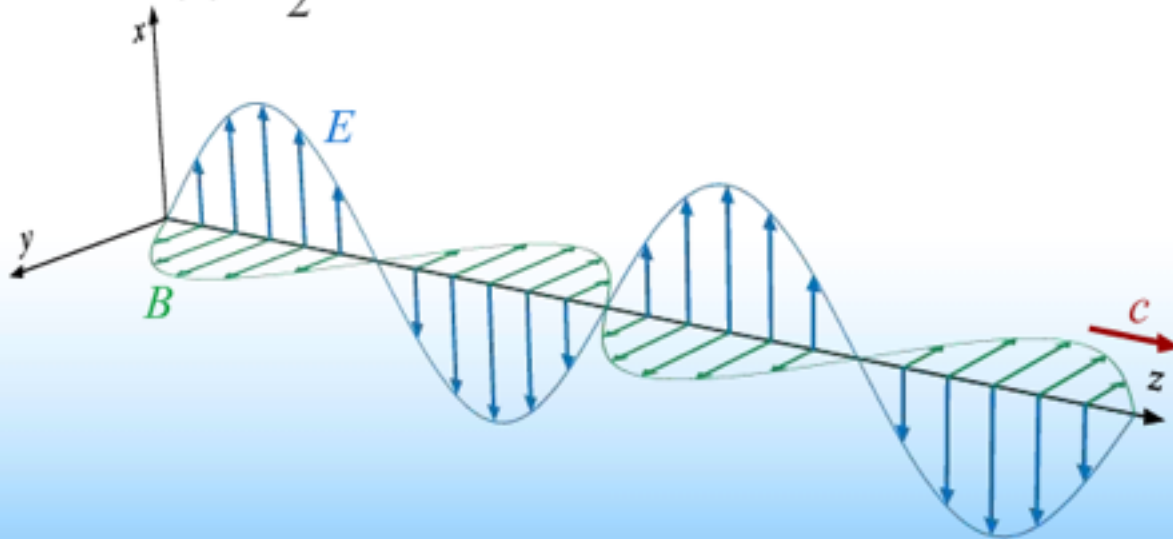
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$$I = \frac{1}{2} c \epsilon_o E_o^2 = c \langle u \rangle$$



# Intensity

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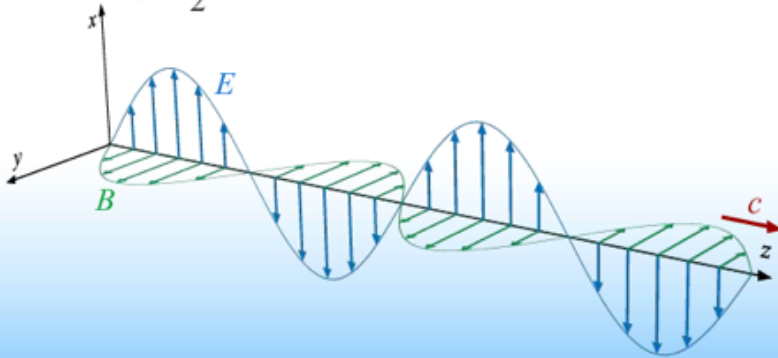
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# Intensity

Intensity = Average energy delivered per unit time, per unit area

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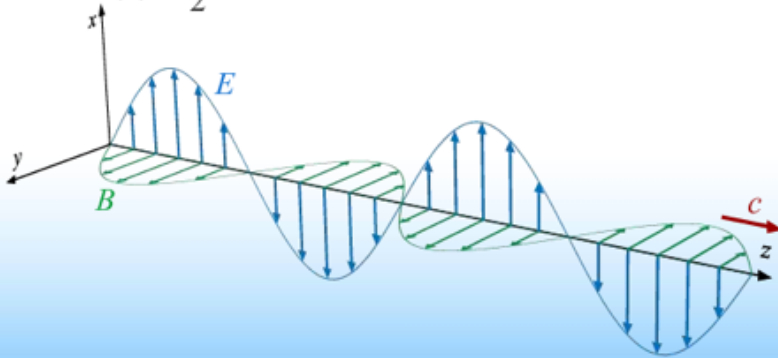
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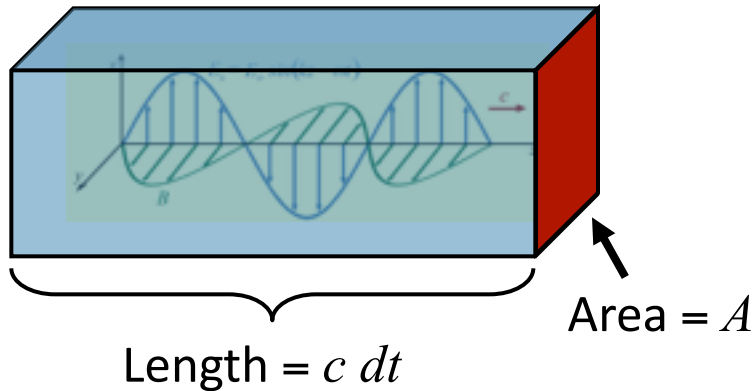
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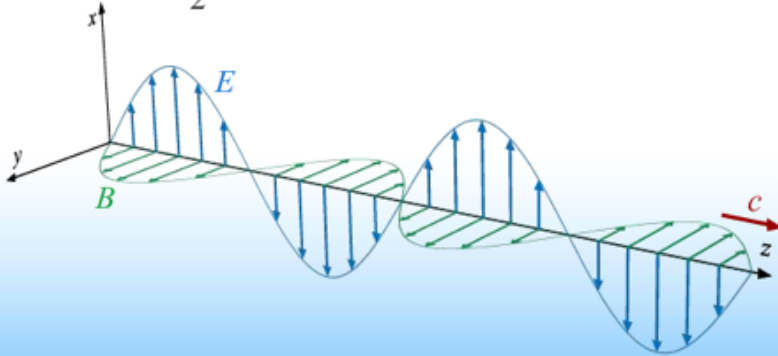
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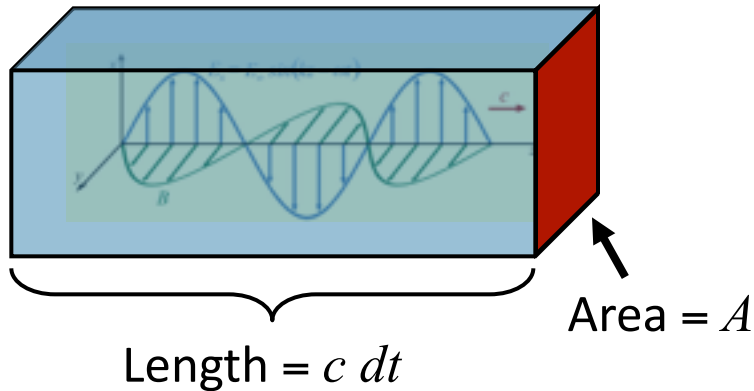
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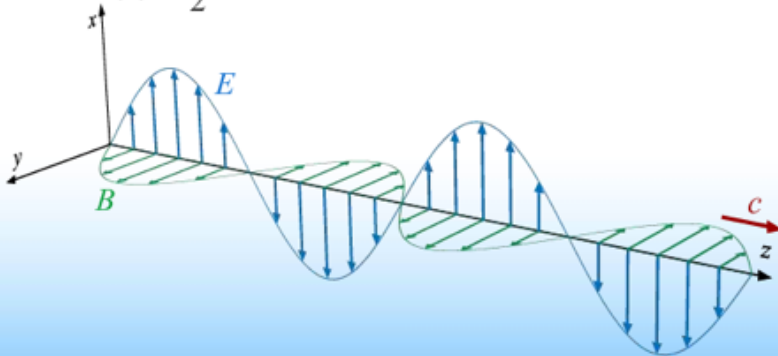
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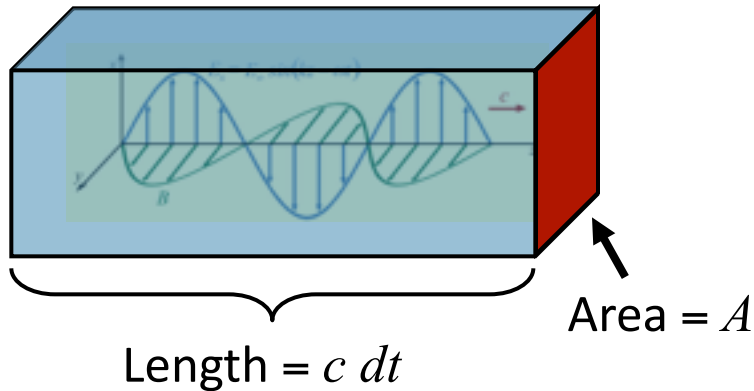
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$$\rightarrow \langle dU \rangle = \langle u \rangle \times \text{volume} = \langle u \rangle A c dt$$

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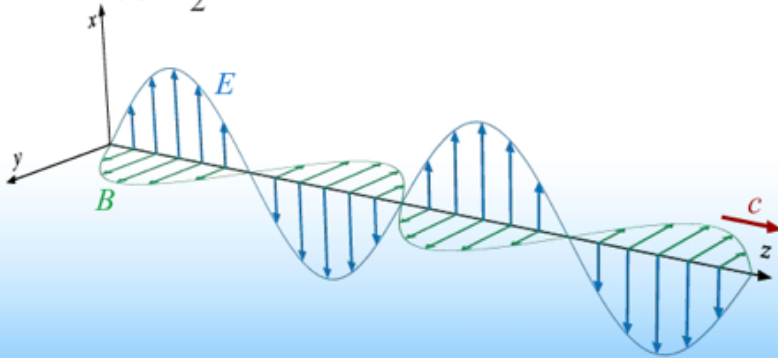
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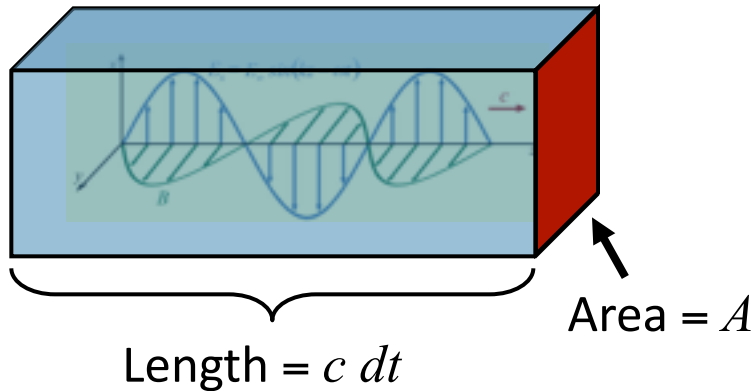
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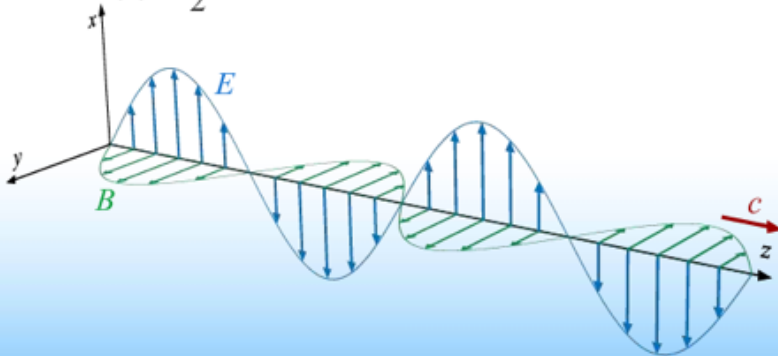
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Sunlight on Earth:

$$I \sim 1000 \text{ J/s/m}^2$$

$$\sim 1 \text{ kW/m}^2$$

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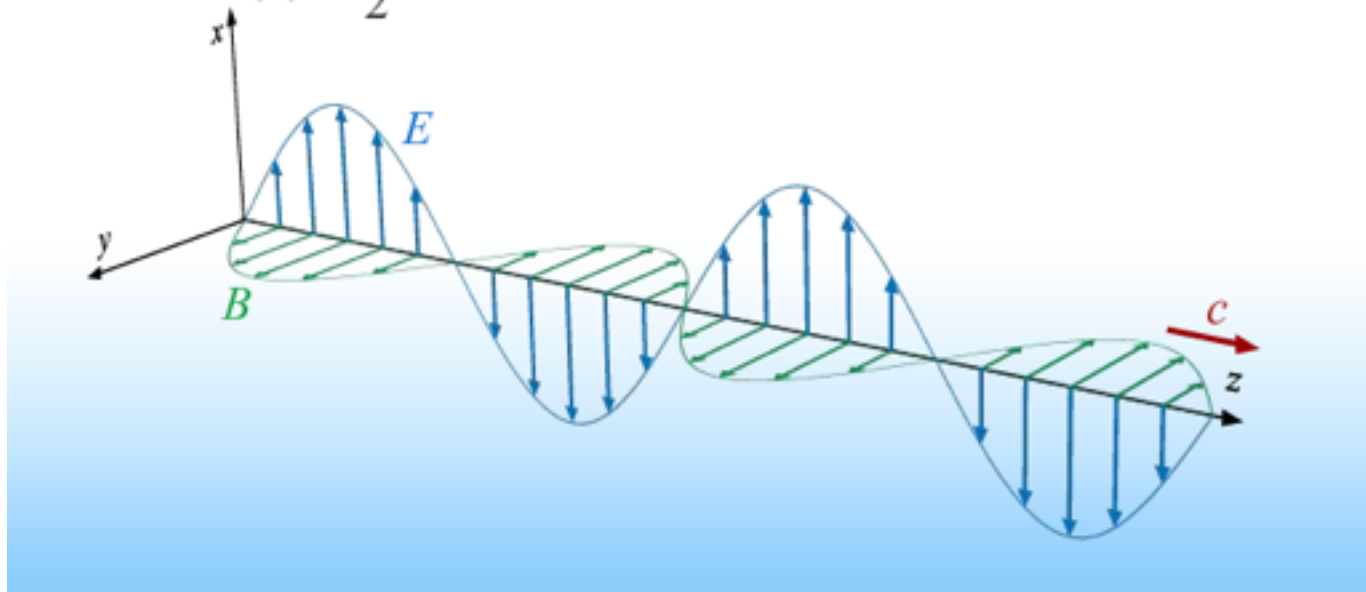
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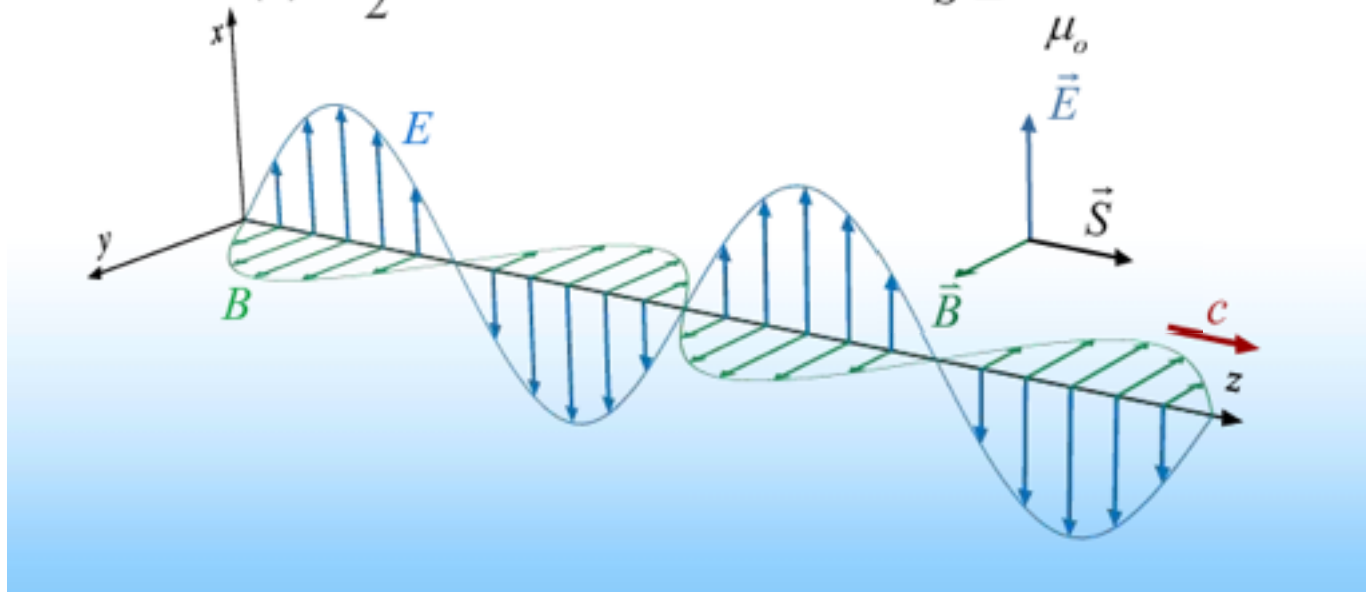
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Poynting Vector

$$\vec{S} \equiv \frac{\vec{E} \times \vec{B}}{\mu_o}$$



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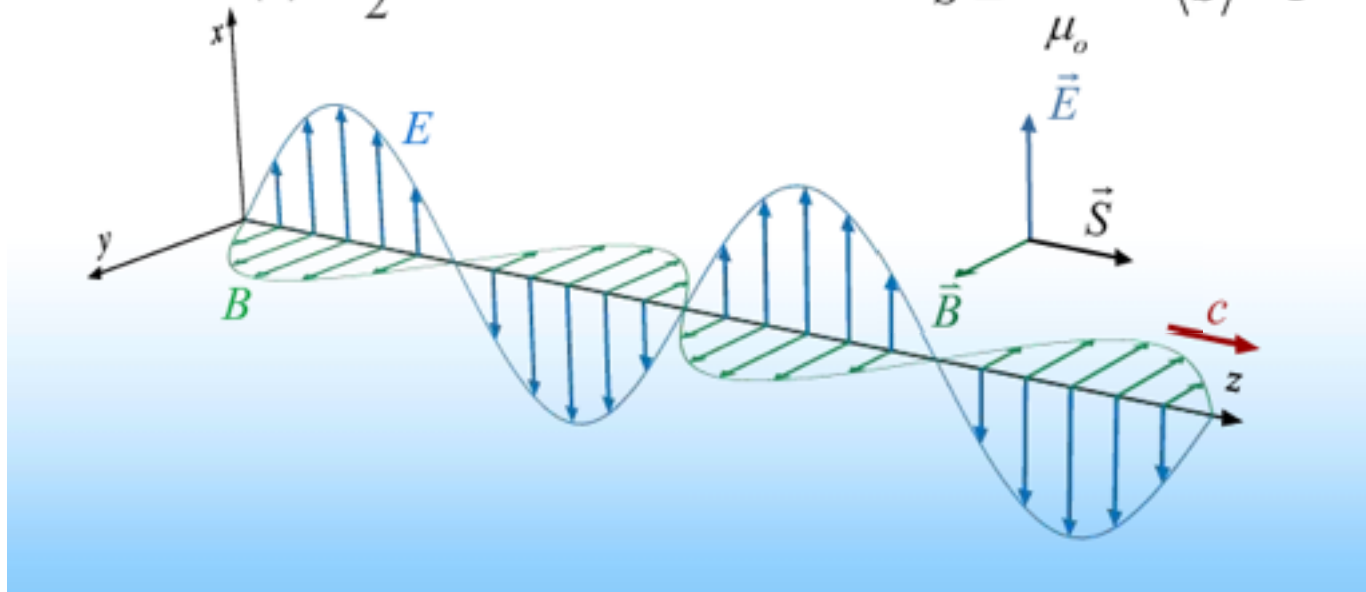
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$$\vec{S} \equiv \frac{\vec{E} \times \vec{B}}{\mu_o} \quad \langle S \rangle = I$$

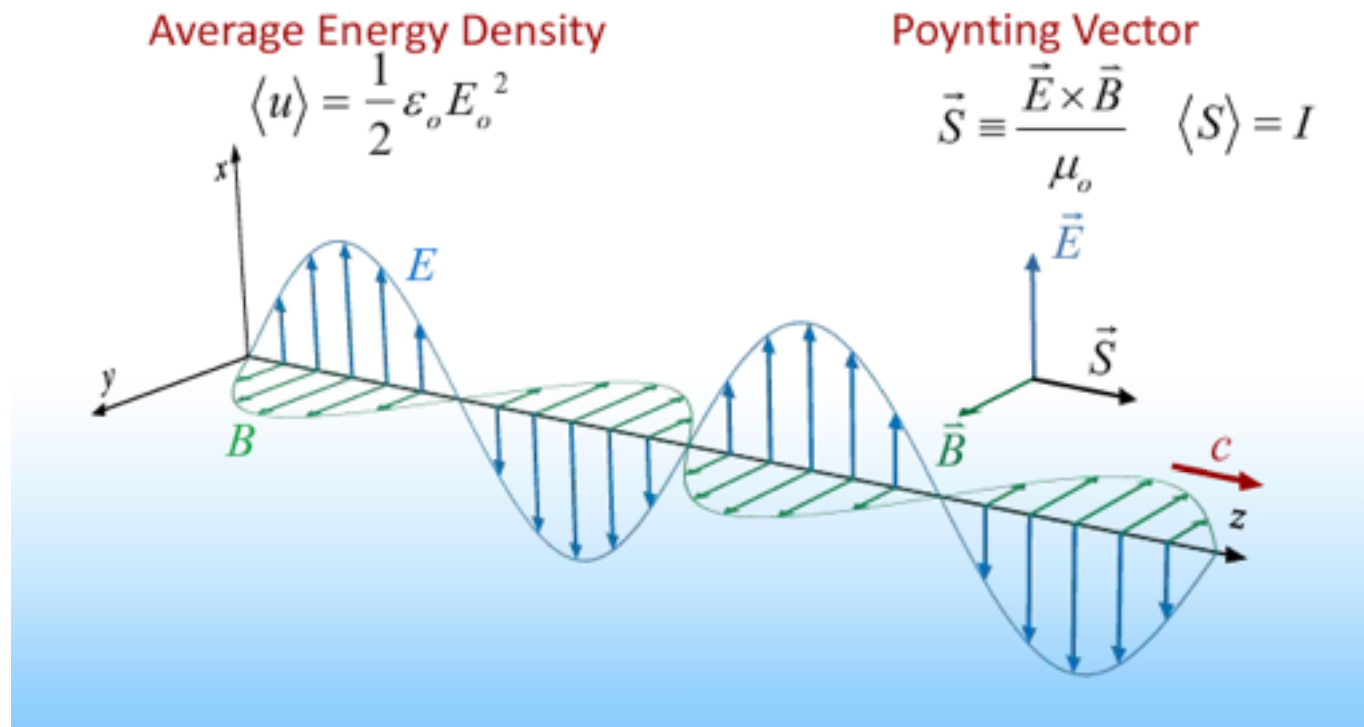


# Comment on Poynting Vector

Just another way to keep track of all this:

Its magnitude is equal to  $I$

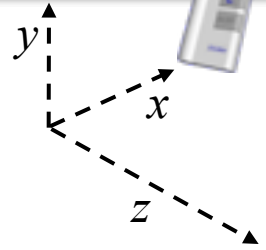
Its direction is the direction of propagation of the wave



# Exercise

An electromagnetic wave is described by:  
where  $\hat{j}$  is the unit vector in the  $+y$  direction.

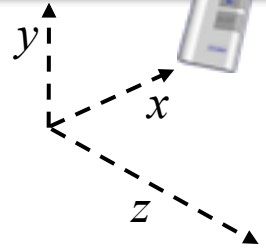
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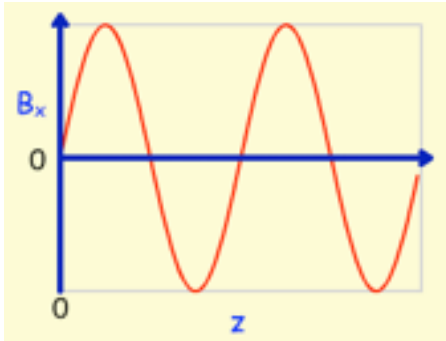
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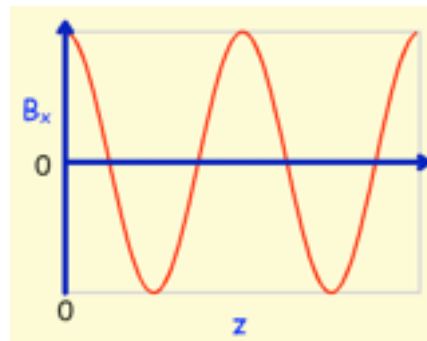
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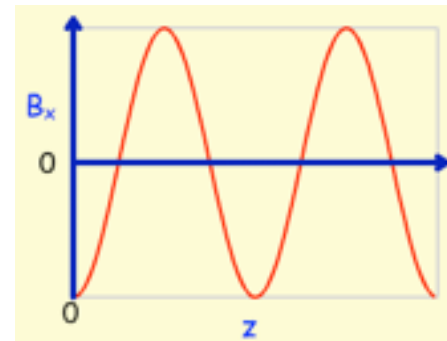
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A



B



C

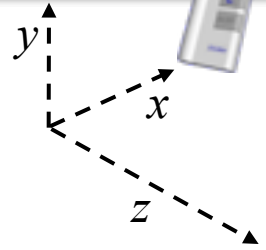


D

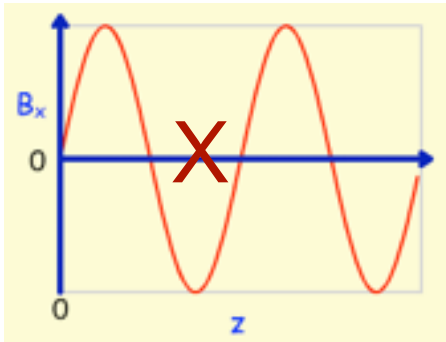
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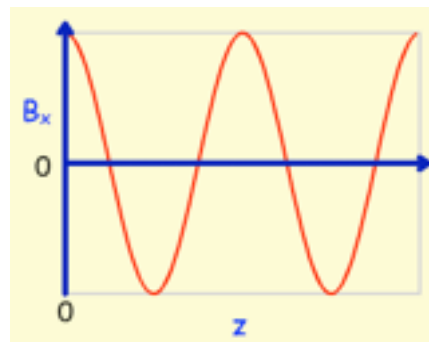
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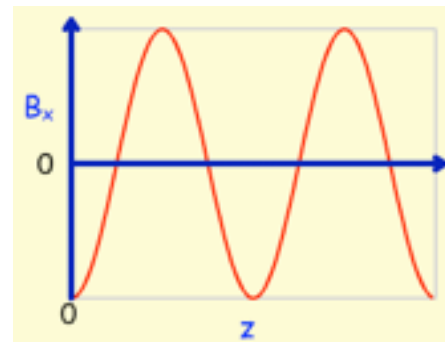
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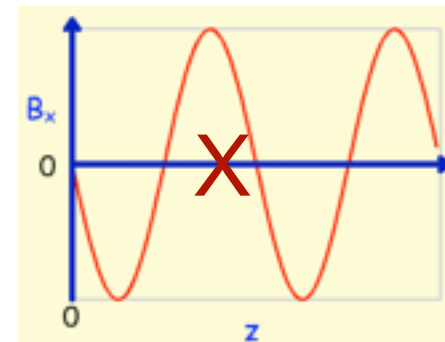
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C



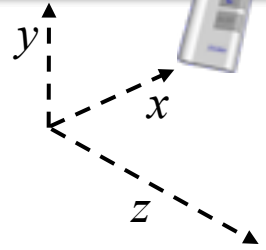
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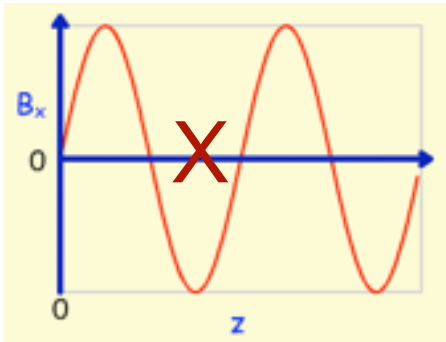
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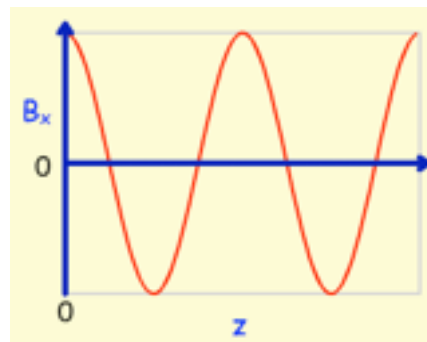
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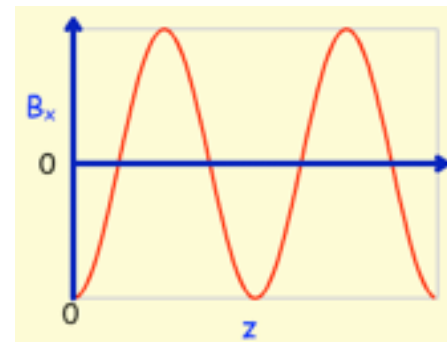
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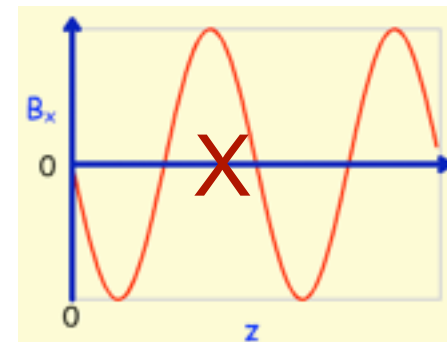
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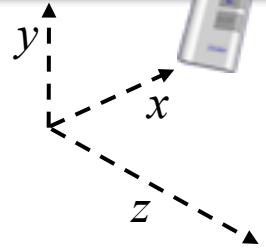
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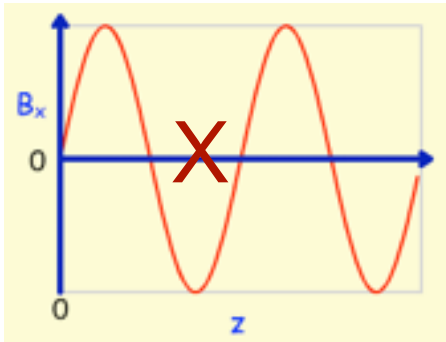
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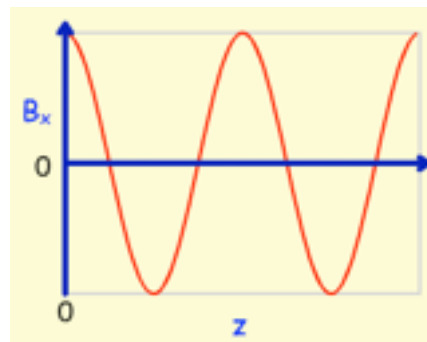
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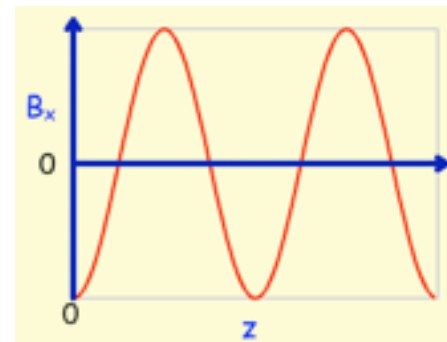
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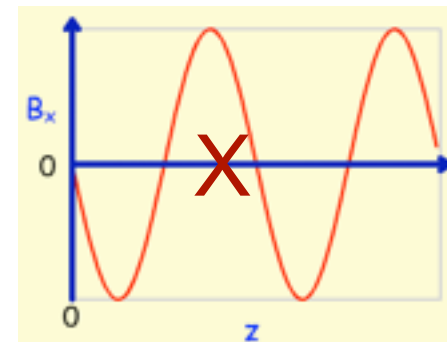
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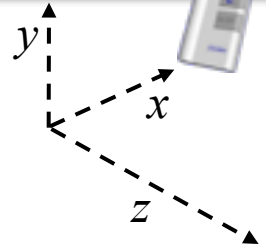
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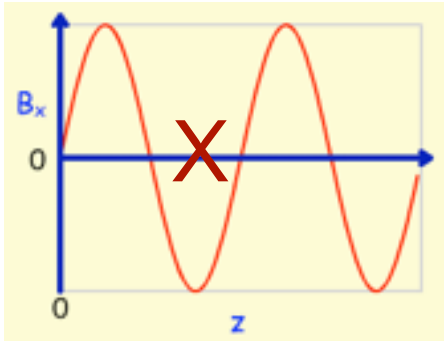
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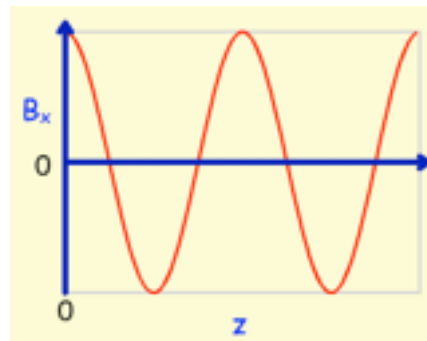
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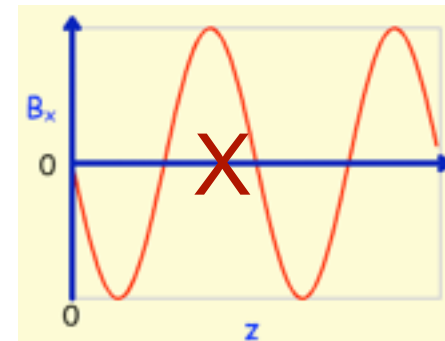
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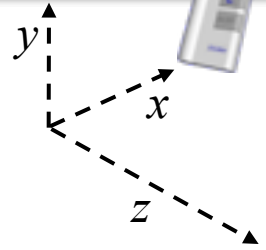
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$\vec{E} \times \vec{B}$  Points in direction of propagation

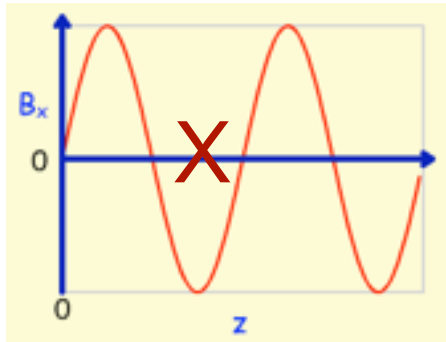
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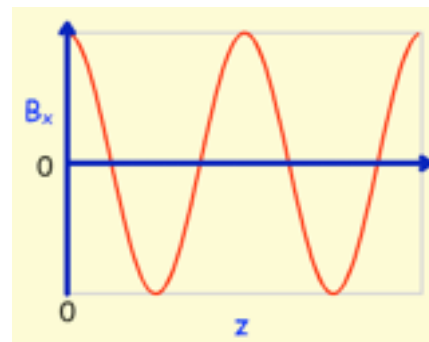
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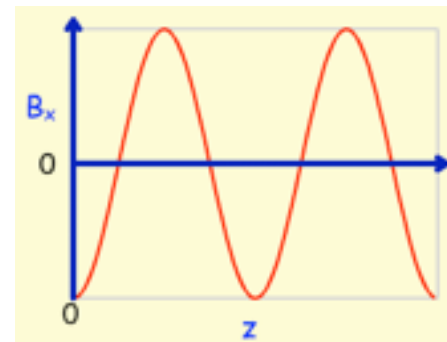
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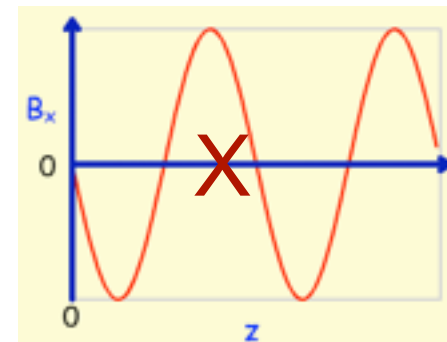
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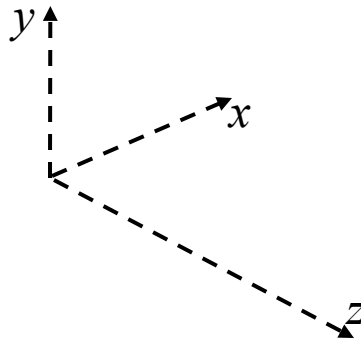


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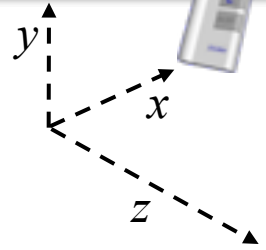
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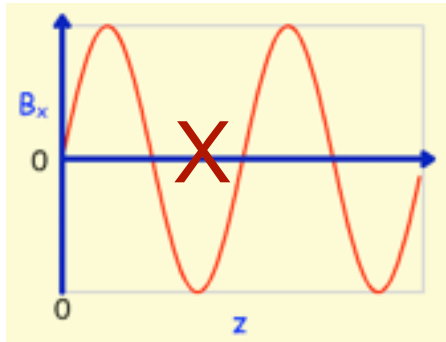
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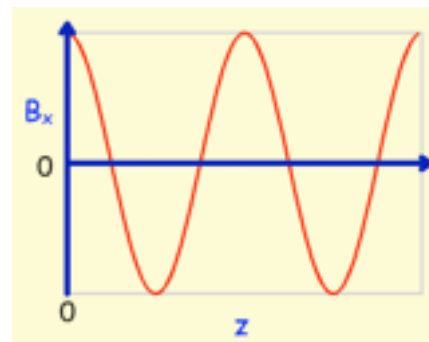
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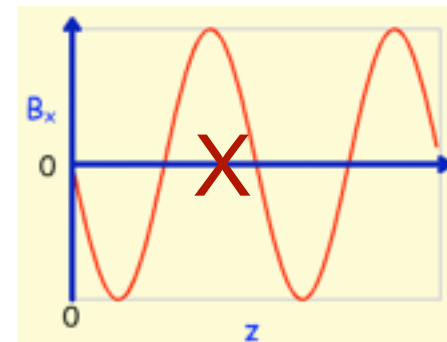
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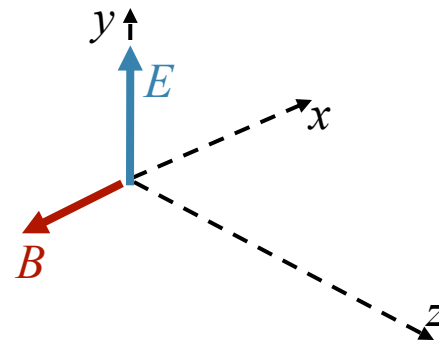


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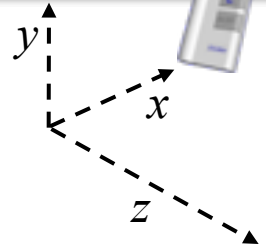
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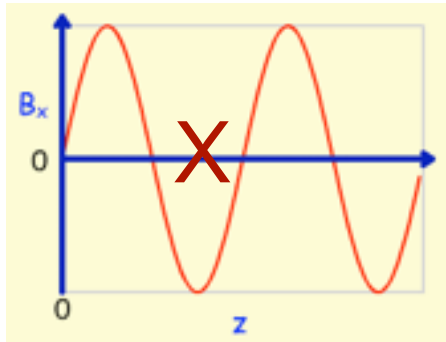
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where  $\hat{j}$  is the unit vector in the  $+y$  direction.

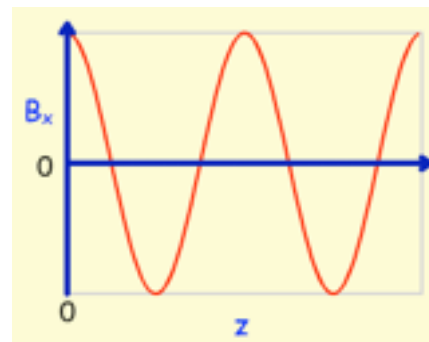
$$\vec{E} = \hat{j}E_0 \cos(kz - \omega t)$$



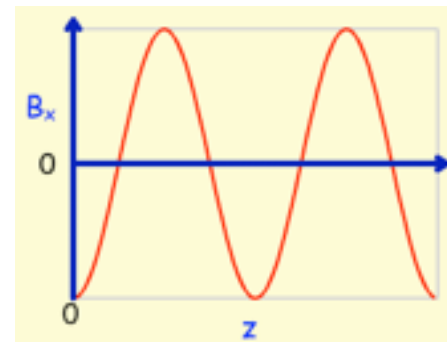
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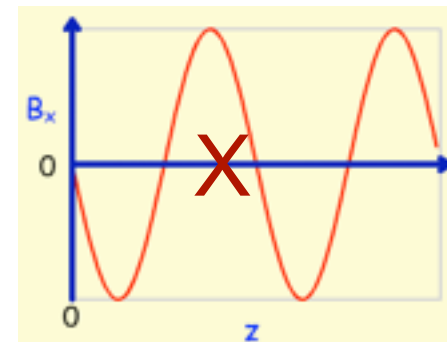
A



B



C

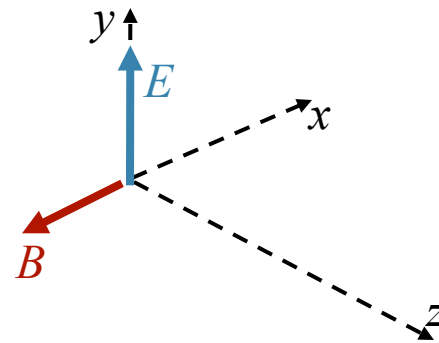


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$E$  and  $B$  are “in phase” (or  $180^\circ$  out of phase)

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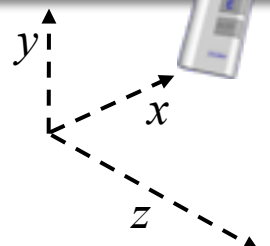


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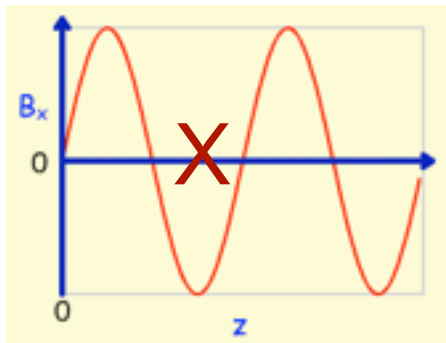
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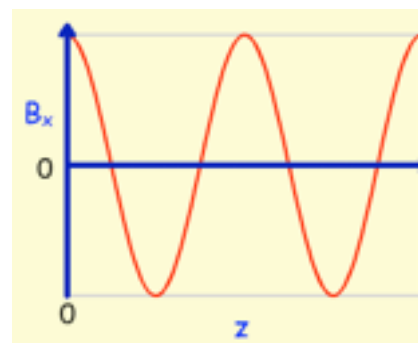
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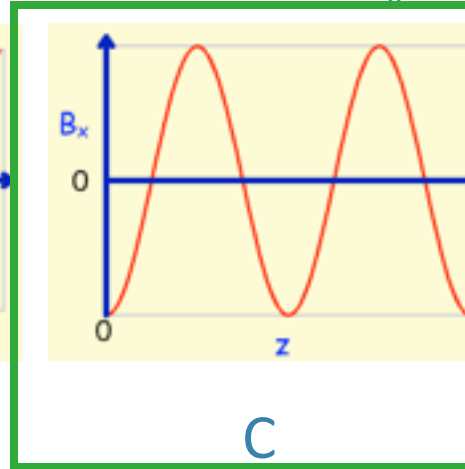
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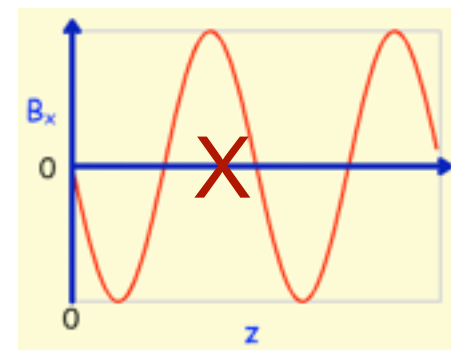
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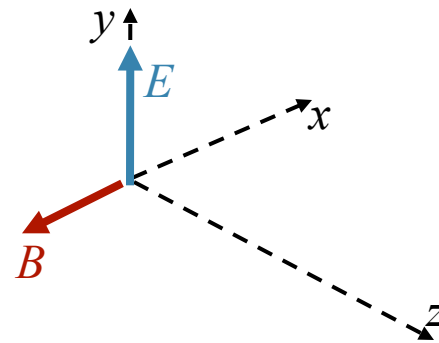


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If it has energy and its moving, then it also has momentum:

Analogy from mechanics:

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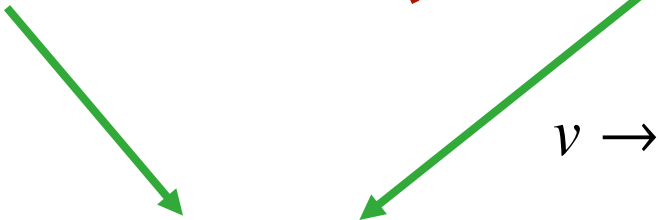
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., An electromagnetic wave has electric field amplitude  $E$ , wavelength  $\lambda$ , and frequency  $\omega$ . Which should we increase if we want the energy carried by the wave to increase (you can mark more than one answer).

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But then again, what are we keeping constant here?

WHAT ABOUT PHOTONS?

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**The mystery of quantum mechanics: More on this in PHYS 285**

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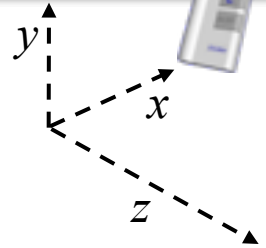
$$\vec{E} = \frac{\hat{i} + \hat{j}}{\sqrt{2}} E_0 \cos(kz + \omega t)$$

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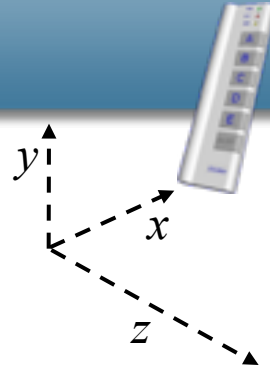
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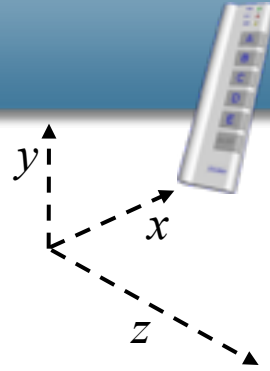
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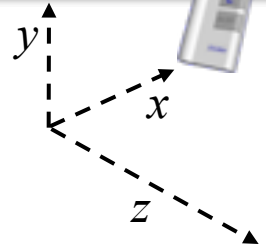


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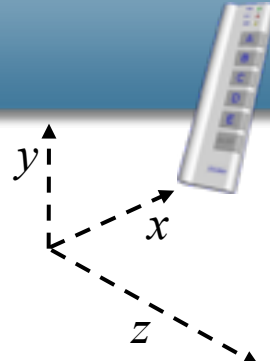
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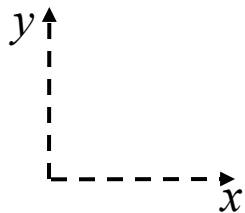
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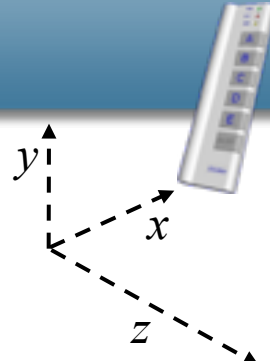
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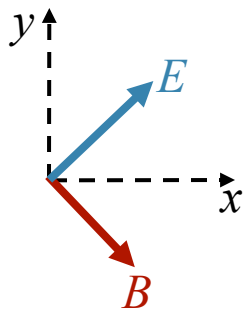
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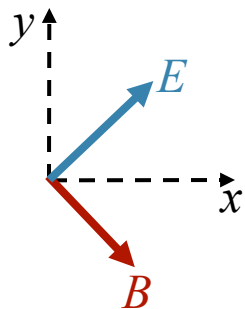
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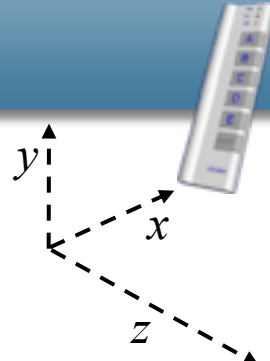
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An electromagnetic wave is described by:

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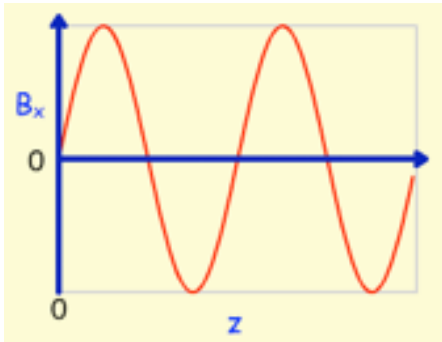
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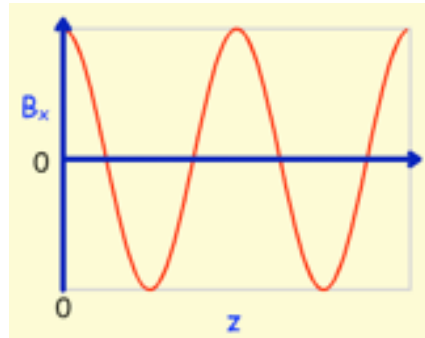
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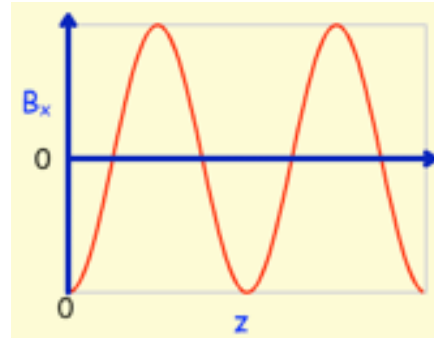
Which of the following plots represents  $B_x(z)$  at time  $t = \pi/2\omega$  ?



A  
D



B



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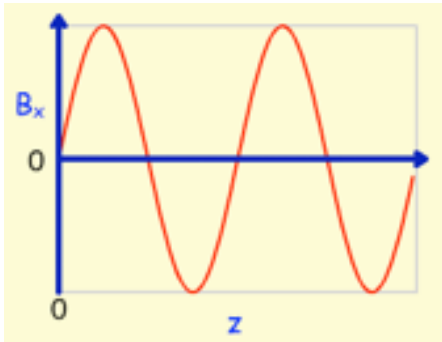
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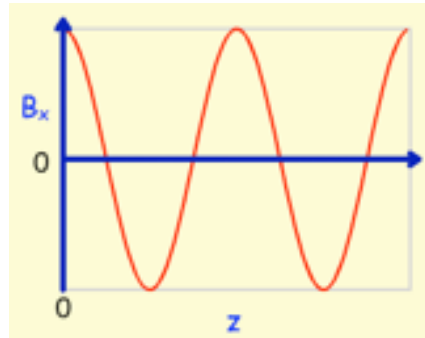
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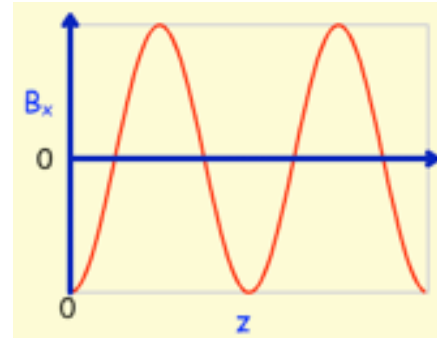
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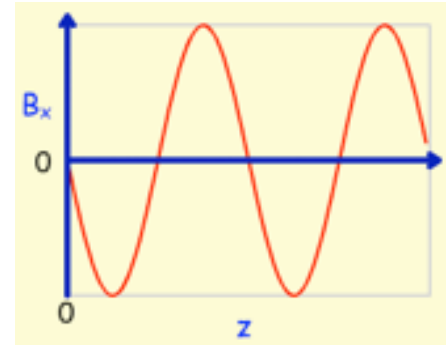
A



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C



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Wave moves in negative  $z$  direction

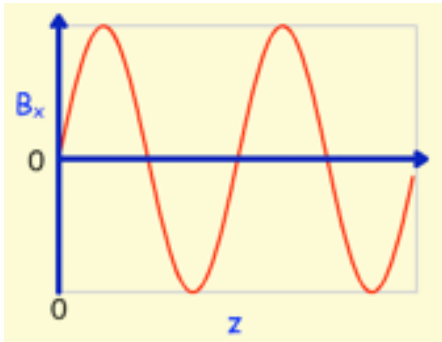
# Exercise



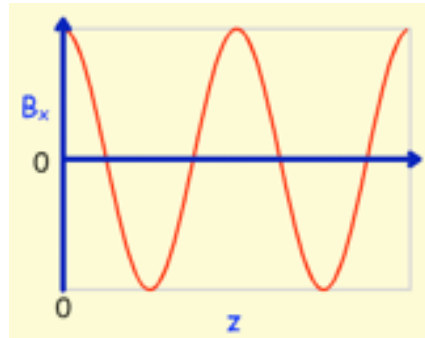
An electromagnetic wave is described by:

$$\vec{E} = \hat{j}E_0 \sin(kz + \omega t)$$

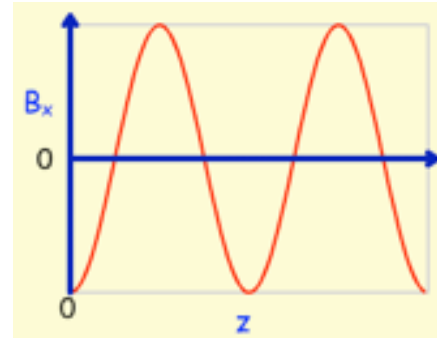
Which of the following plots represents  $B_x(z)$  at time  $t = \pi/2\omega$  ?



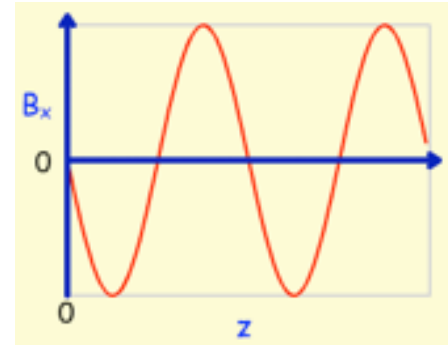
A  
D



B



C



D

Wave moves in negative  $z$  direction



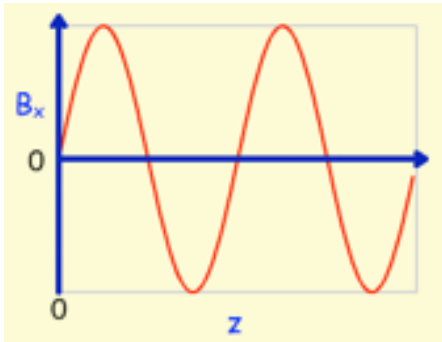
$$\vec{B} = \hat{i}(E_0 / c) \sin(kz + \omega t)$$

# Exercise

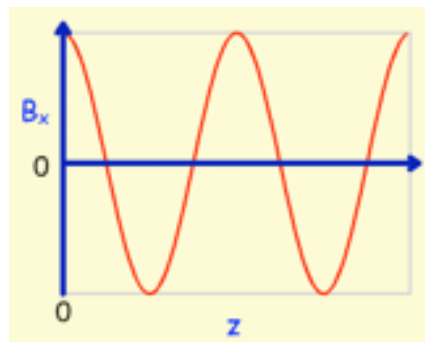
An electromagnetic wave is described by:

$$\vec{E} = \hat{j}E_0 \sin(kz + \omega t)$$

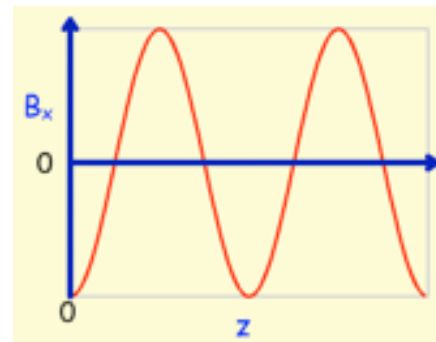
Which of the following plots represents  $B_x(z)$  at time  $t = \pi/2\omega$  ?



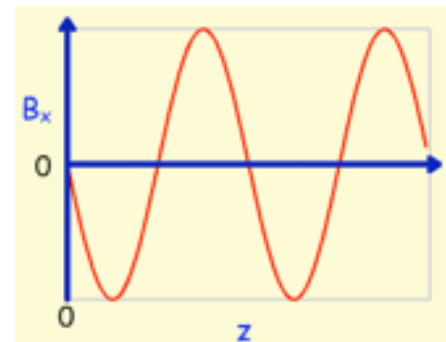
A  
D



B



C

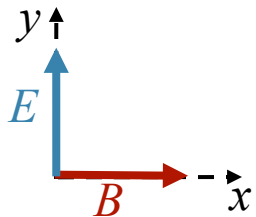


D

Wave moves in negative  $z$  direction



$$\vec{B} = \hat{i}(E_0 / c) \sin(kz + \omega t)$$



+  $z$  points out of screen

-  $z$  points into screen

$\vec{E} \times \vec{B}$  Points in direction of propagation

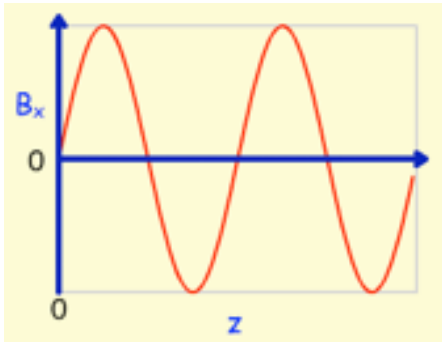
# Exercise



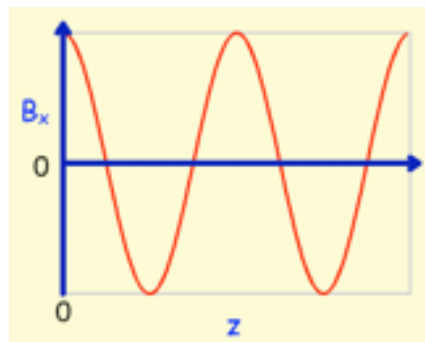
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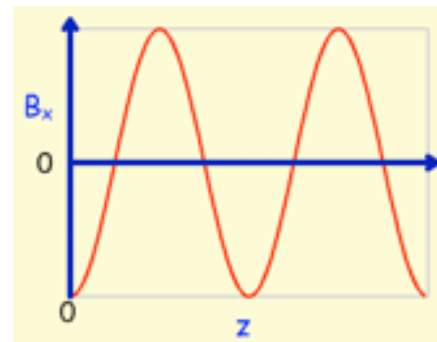
Which of the following plots represents  $B_x(z)$  at time  $t = \pi/2\omega$  ?



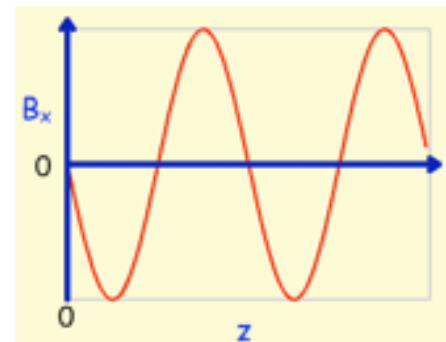
A  
D



B

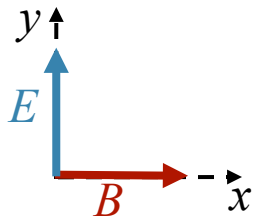


C



D

Wave moves in negative  $z$  direction



+  $z$  points out of screen

-  $z$  points into screen



$$\vec{B} = \hat{i}(E_0 / c) \sin(kz + \omega t)$$

at  $\omega t = \pi/2$ :

$$B_x = (E_0 / c) \sin(kz + \pi / 2)$$

$\vec{E} \times \vec{B}$  Points in direction of propagation

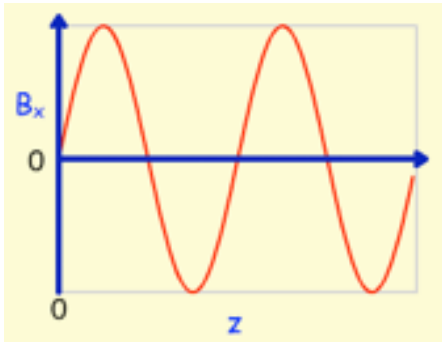
# Exercise



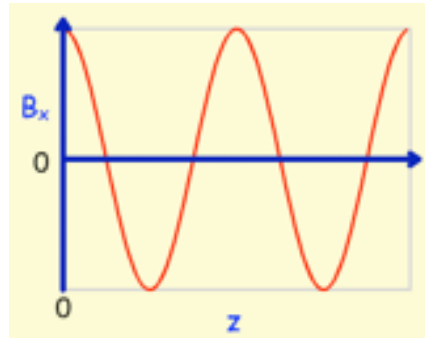
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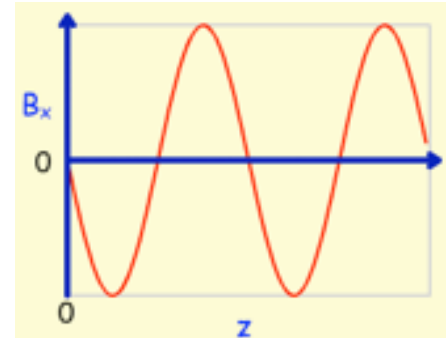
A  
D



B

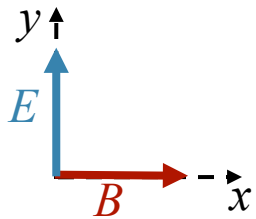


C



D

Wave moves in negative  $z$  direction



+  $z$  points out of screen

-  $z$  points into screen

$\vec{E} \times \vec{B}$  Points in direction of propagation



$$\vec{B} = \hat{i}(E_0 / c) \sin(kz + \omega t)$$

at  $\omega t = \pi/2$ :

$$B_x = (E_0 / c) \sin(kz + \pi / 2)$$

$$B_x = (E_0 / c) \{ \sin kz \cos(\pi / 2) + \cos kz \sin(\pi / 2) \}$$

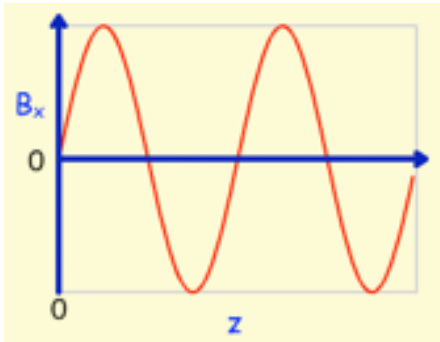
# Exercise



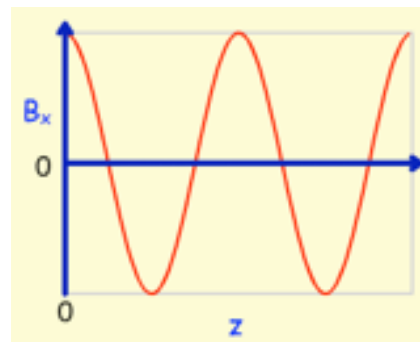
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$$\vec{E} = \hat{j}E_0 \sin(kz + \omega t)$$

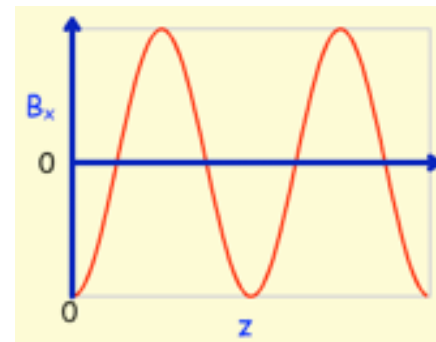
Which of the following plots represents  $B_x(z)$  at time  $t = \pi/2\omega$  ?



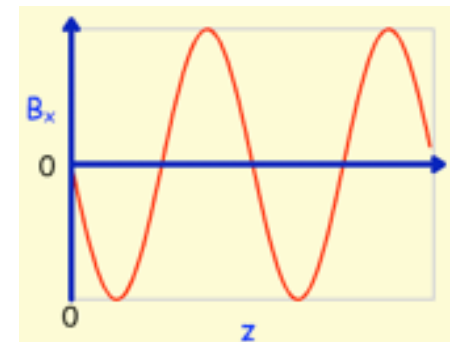
A  
D



B

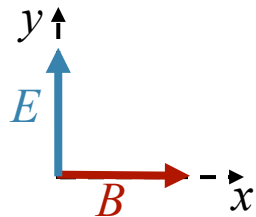


C



D

Wave moves in negative  $z$  direction



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$\vec{E} \times \vec{B}$  Points in direction of propagation



$$\vec{B} = \hat{i}(E_0 / c) \sin(kz + \omega t)$$

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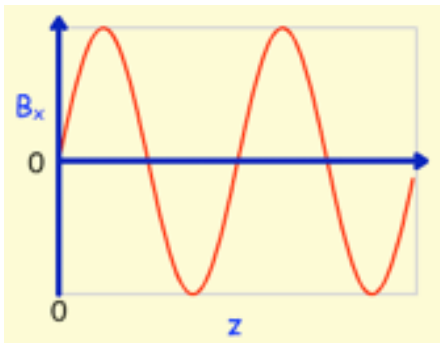
$$B_x = (E_0 / c) \cos(kz)$$

# Exercise

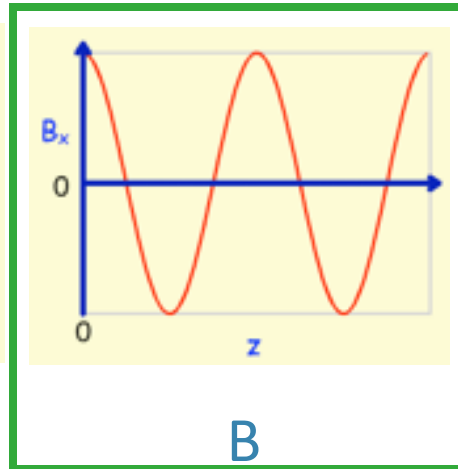
An electromagnetic wave is described by:

$$\vec{E} = \hat{j}E_0 \sin(kz + \omega t)$$

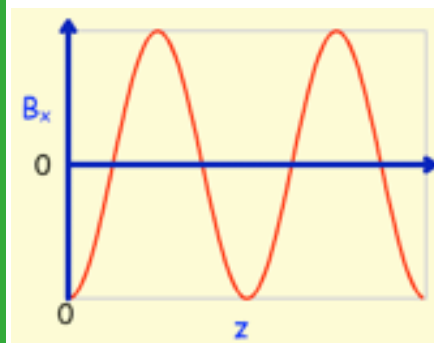
Which of the following plots represents  $B_x(z)$  at time  $t = \pi/2\omega$  ?



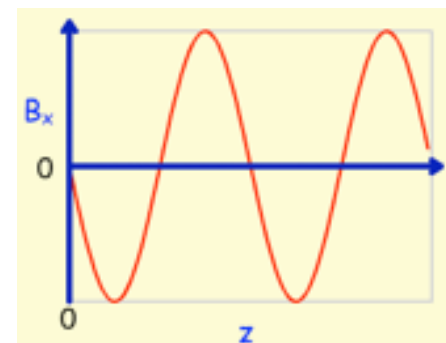
A  
D



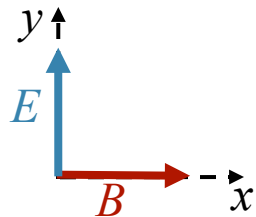
B



C



Wave moves in negative  $z$  direction



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$$\vec{B} = \hat{i}(E_0 / c) \sin(kz + \omega t)$$

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$$B_x = (E_0 / c) \cos(kz)$$