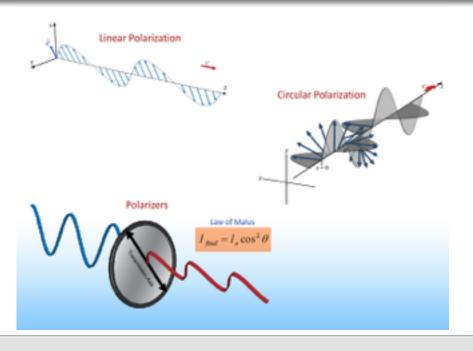
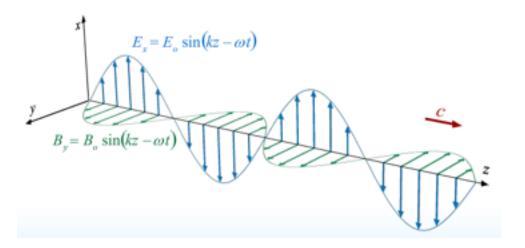
Physics 121 Lecture 24



So far we have considered plane waves that look like this:

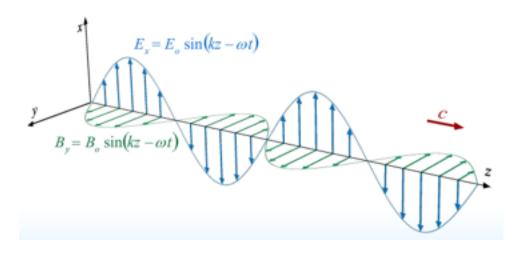


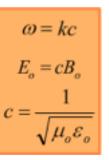
$$\omega = kc$$

$$E_o = cB_o$$

$$c = \frac{1}{\sqrt{\mu_o \varepsilon_o}}$$

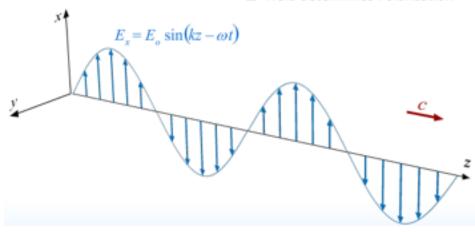
So far we have considered plane waves that look like this:



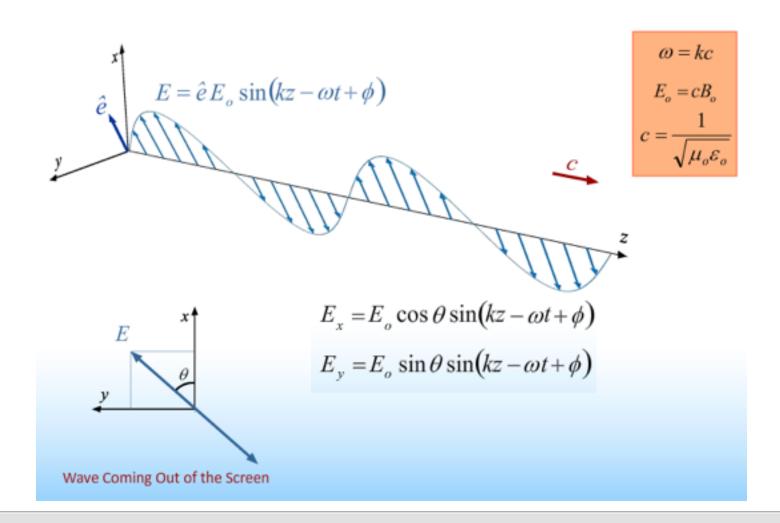


From now on just draw E and remember that B is still there:

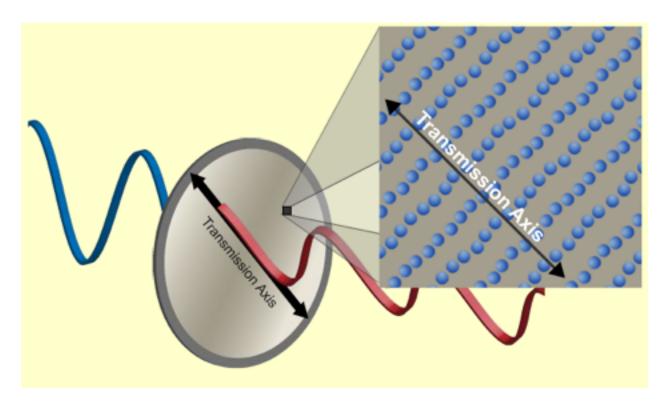
$ec{E}$ Field determines Polarization



Linear Polarization

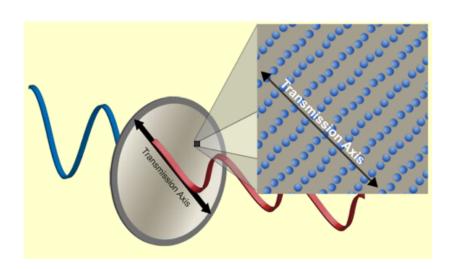


Polarizer



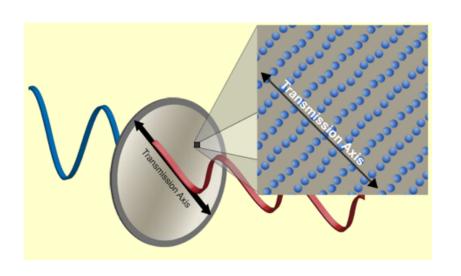
The molecular structure of a polarizer causes the component of the E field perpendicular to the Transmission Axis to be absorbed.





The molecular structure of a polarizer causes the component of the *E* field perpendicular to the Transmission Axis to be absorbed.





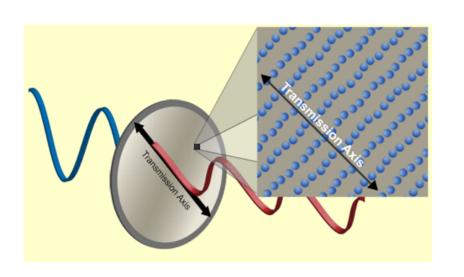
The molecular structure of a polarizer causes the component of the E field perpendicular to the Transmission Axis to be absorbed.

 E_{o}

Suppose we have a beam traveling in the +z – direction. At t=0 and z=0, the electric field is aligned along the positive x – axis and has a magnitude equal to E_o

Z





The molecular structure of a polarizer causes the component of the *E* field perpendicular to the Transmission Axis to be absorbed.

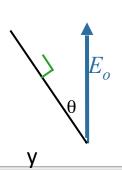
Suppose we have a beam traveling in the +z – direction.

At t = 0 and z = 0, the electric field is aligned along the positive x

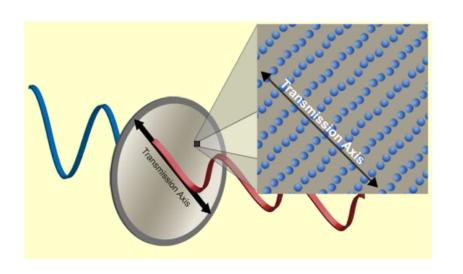
– axis and has a magnitude equal to E_{α}

What is the component of E_o along a direction in the x-y plane that makes an angle of θ with respect to the x – axis?

- $E_o \sin\theta$
- B) $E_o \cos\theta$
- C) 0 D) $E_o/\sin\theta$
- E) $E_o/\cos\theta$







The molecular structure of a polarizer causes the component of the *E* field perpendicular to the Transmission Axis to be absorbed.

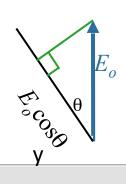
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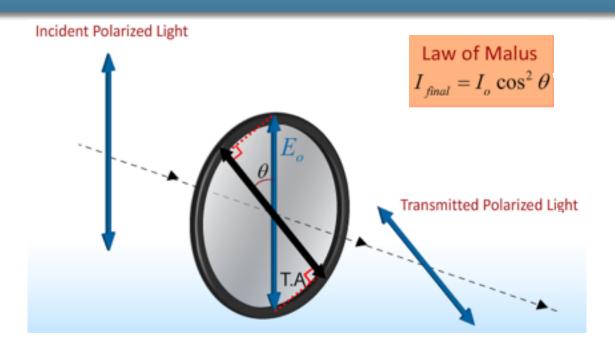
– axis and has a magnitude equal to E_o

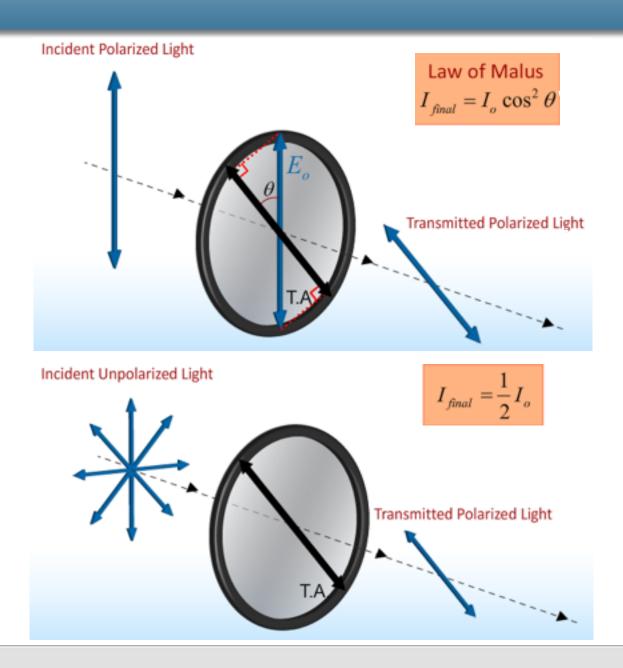
What is the component of E_o along a direction in the x-y plane that makes an angle of θ with respect to the x – axis?

- A) $E_o \sin\theta$
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- **C)** 0
- D) $E_o/\sin\theta$
- E) $E_o/\cos\theta$

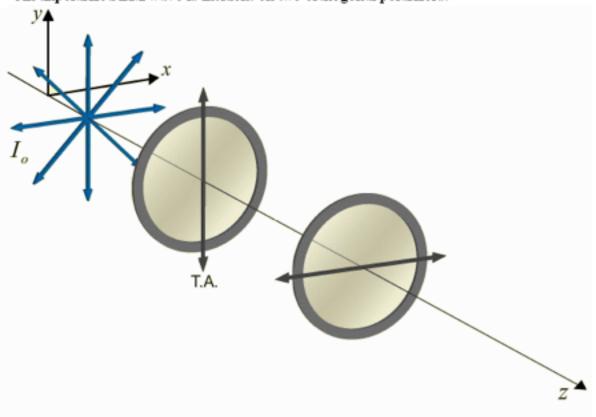


Z





An unpolarized EM wave is incident on two orthogonal polarizers.



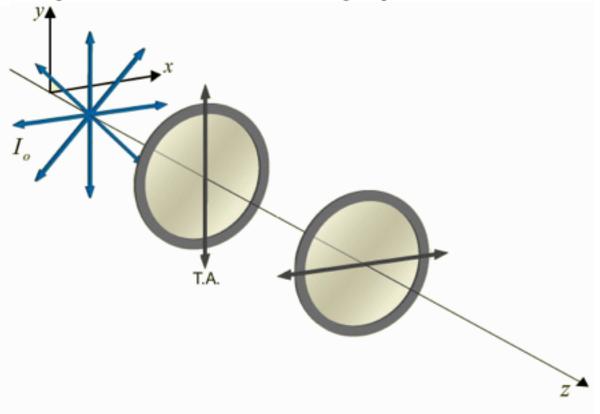
Two Polarizers

What percentage of the intensity gets through both polarizers?

- 50%
- O 25%
- 00%



An unpolarized EM wave is incident on two orthogonal polarizers.



Two Polarizers

What percentage of the intensity gets through both polarizers?

50%

O 25%

00%

The second polarizer is orthogonal to the first

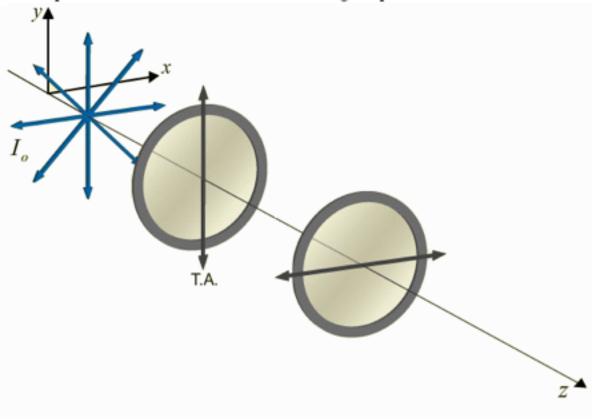


No light will come through.

 $\cos(90^{\circ}) = 0$



An unpolarized EM wave is incident on two orthogonal polarizers.



Two Polarizers

What percentage of the intensity gets through both polarizers?



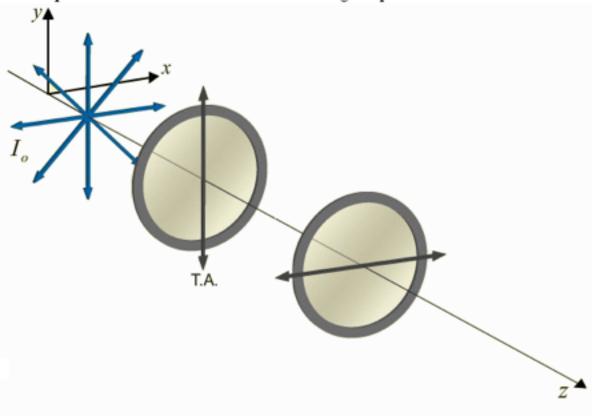
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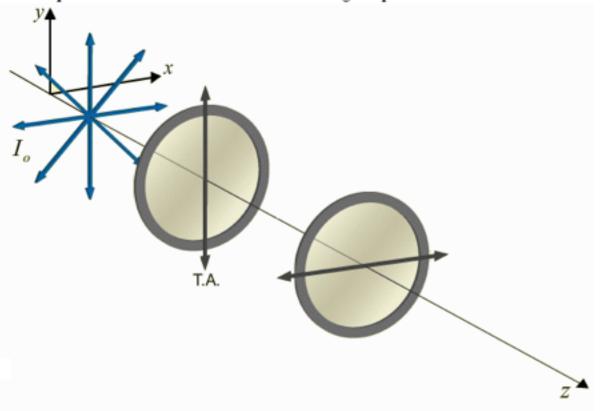
Two Polarizers

4) Is it possible to increase this percentage by inserting another polarizer between the original two?

Oyes

Ono

An unpolarized EM wave is incident on two orthogonal polarizers.



Two Polarizers

4) Is it possible to increase this percentage by inserting another polarizer between

the original two?

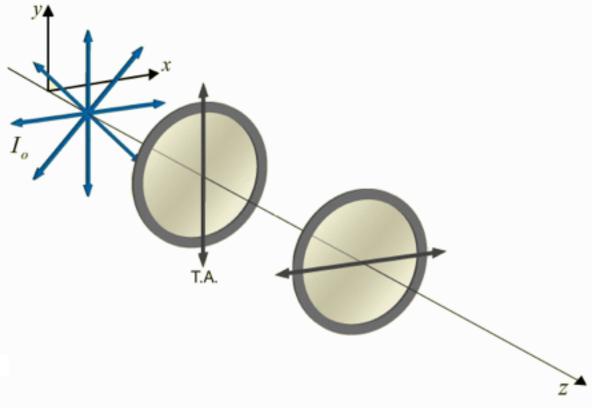
O yes

Ono

Any non-horizontal polarizer after the first polarizer will produce polarized light at that angle

Part of that light will make it through the horizontal polarizer

An unpolarized EM wave is incident on two orthogonal polarizers.



Two Polarizers

4) Is it possible to increase this percentage by inserting another polarizer between

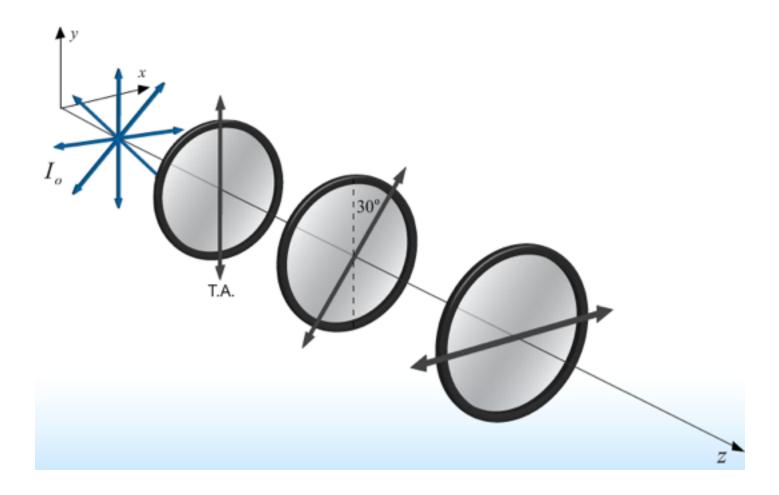




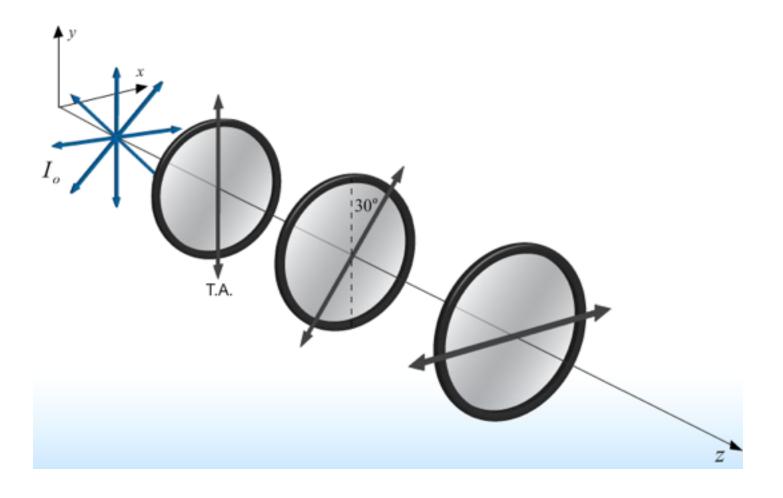
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Part of that light will make it through the horizontal polarizer

Demo

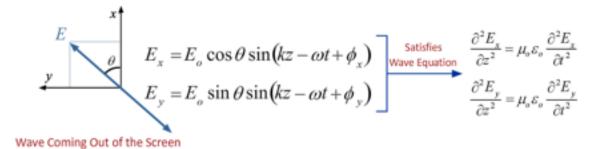


Demo

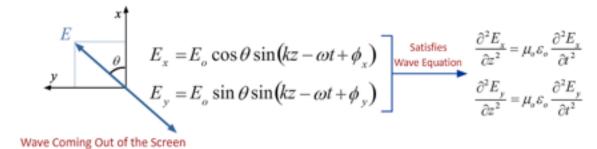


A third filter between the two crossed polarizzers allows some light through. The middle polarizer creates light with a component of E along the transmission axis of the third polarizer.

There is no reason that ϕ has to be the same for E_x and E_v :

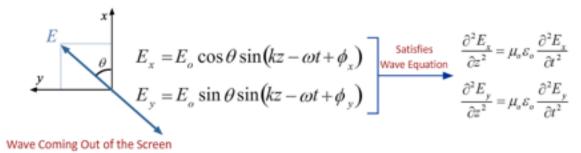


There is no reason that ϕ has to be the same for E_x and E_y :



Making ϕ_x different from ϕ_y causes circular or elliptical polarization:

There is no reason that ϕ has to be the same for E_x and E_y :



Making ϕ_x different from ϕ_y causes circular or elliptical polarization:

Example:

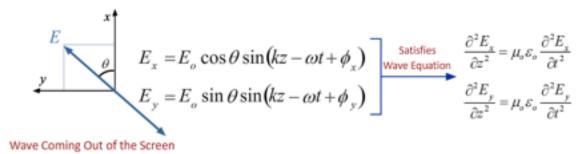
$$\phi_x - \phi_y = 90^\circ = \frac{\pi}{2}$$

$$\theta = 45^{\circ} = \pi / 4$$

$$E_x = \frac{E_0}{\sqrt{2}} \cos(kz - \omega t)$$

$$E_x = \frac{E_0}{\sqrt{2}} \sin(kz - \omega t)$$

There is no reason that ϕ has to be the same for E_x and E_y :



Making ϕ_x different from ϕ_y causes circular or elliptical polarization:

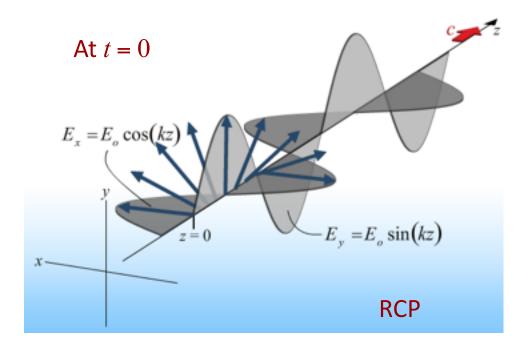
Example:

$$\phi_x - \phi_y = 90^\circ = \frac{\pi}{2}$$

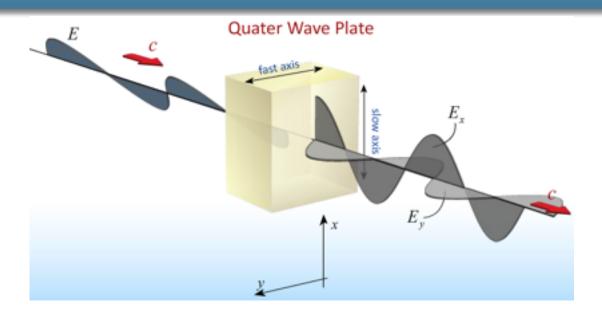
$$\theta = 45^{\circ} = \pi / 4$$

$$E_x = \frac{E_0}{\sqrt{2}} \cos(kz - \omega t)$$

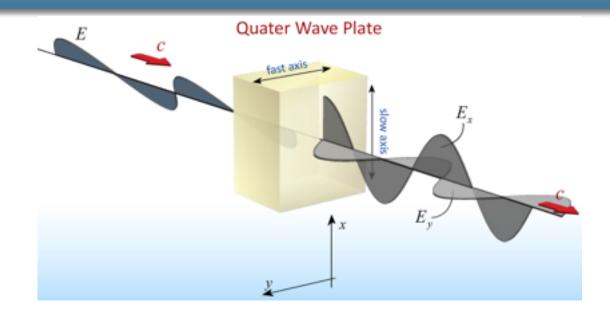
$$E_x = \frac{E_0}{\sqrt{2}} \sin(kz - \omega t)$$



A: Birefringence

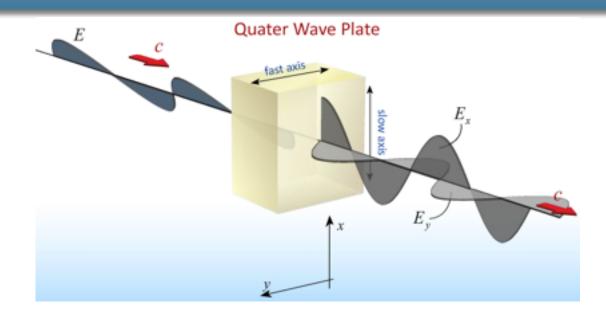


A: Birefringence



By picking the right thickness we can change the relative phase by exactly 90° .

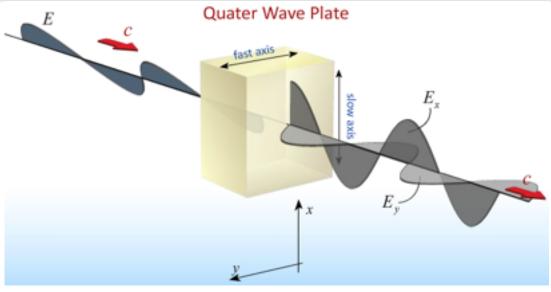
A: Birefringence

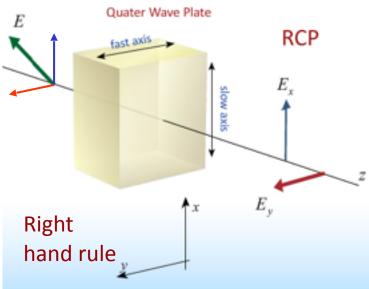


By picking the right thickness we can change the relative phase by exactly 90° .

This changes <u>linear</u> to <u>circular</u> polarization and is called a *quarter wave plate*

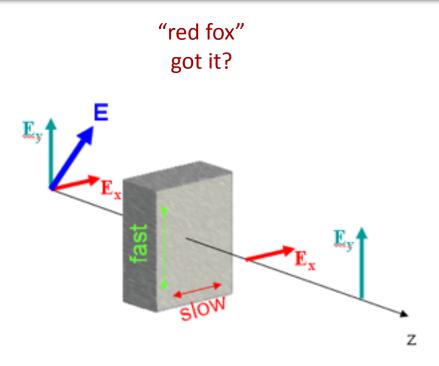
A: Birefringence

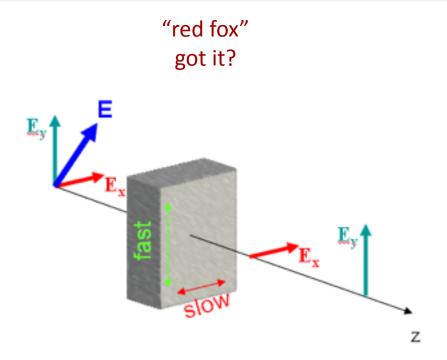




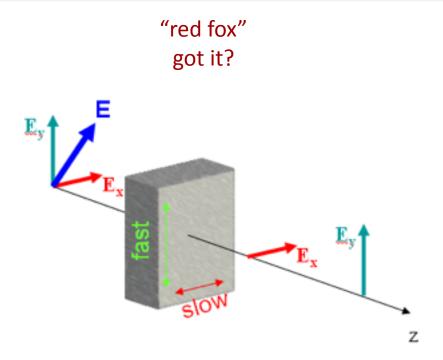
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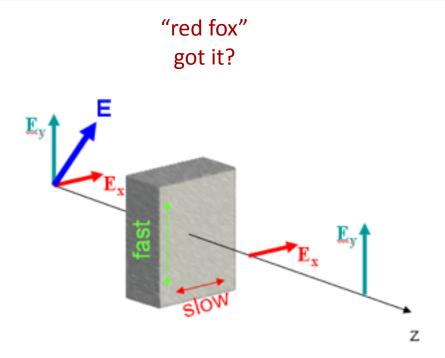




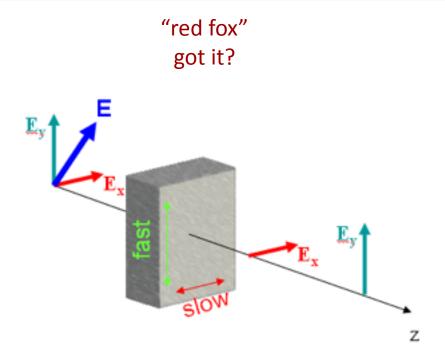
Right circularly polarized



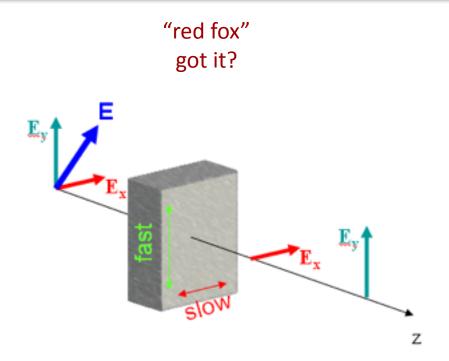
Right circularly polarized Do right hand rule



Right circularly polarized
Do right hand rule
Fingers along slow direction



Right circularly polarized
Do right hand rule
Fingers along slow direction
Cross into fast direction



Right circularly polarized

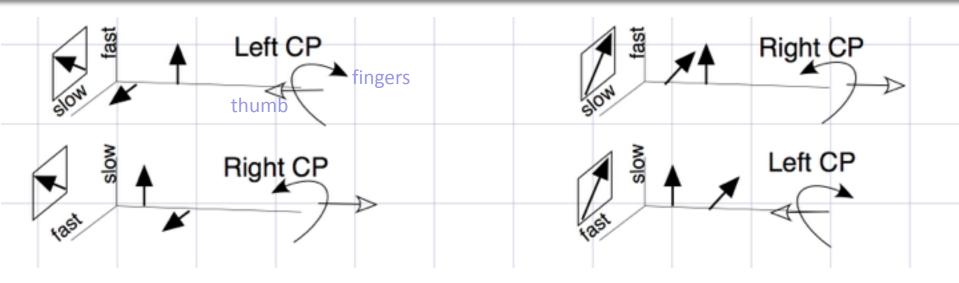
Do right hand rule

Fingers along slow direction

Cross into fast direction

If thumb points in direction of propagation: RCP

Identifying handedness of CP



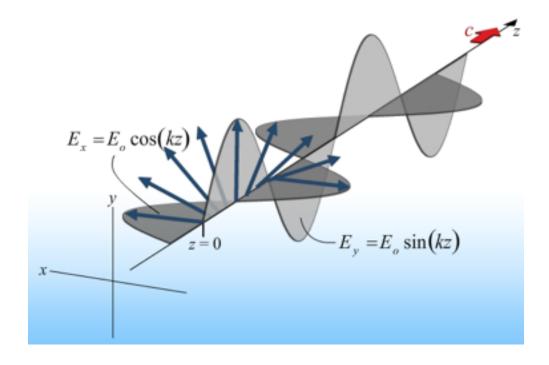
Here are four different possibilities of incident linearly polarized light passing thru a qwp and the resulting circular polarization

Circular Light on Linear Polarizer



Q: What happens when circularly polarized light is put through a polarizer along the y (or x) axis?

- A) I = 0
- B) $I = \frac{1}{2} I_0$
- C) $I = I_0$



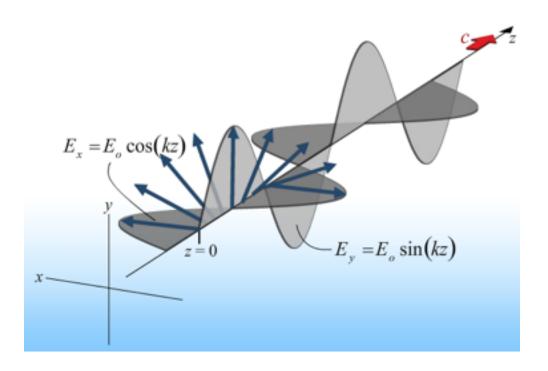
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$$I = \varepsilon_0 c \langle E^2 \rangle$$



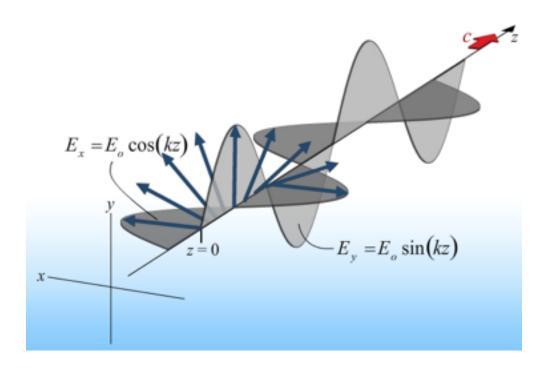


A)
$$I=0$$

B)
$$I = \frac{1}{2} I_0$$

C)
$$I = I_0$$

$$I = \varepsilon_0 c \langle E^2 \rangle$$
$$= \varepsilon_0 c \langle E_x^2 + E_y^2 \rangle$$



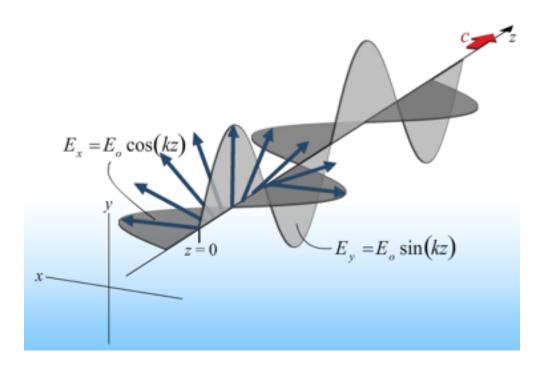


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A)
$$I = 0$$

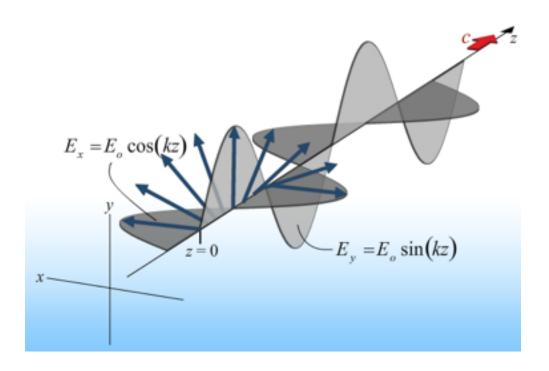
B)
$$I = \frac{1}{2} I_0$$

C)
$$I = I_0$$

$$I = \varepsilon_0 c \langle E^2 \rangle$$

$$= \varepsilon_0 c \langle E_x^2 + \mathbf{K}_y^2 \rangle$$

$$= \varepsilon_0 c \frac{E_0^2}{2} \langle \cos^2(kz - \omega t) \rangle$$





A)
$$I = 0$$

B)
$$I = \frac{1}{2} I_0$$

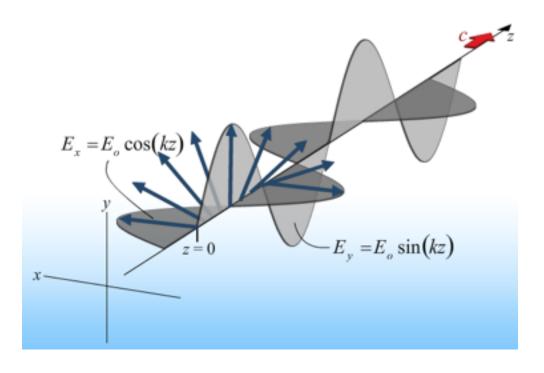
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$$= \varepsilon_0 c \frac{E_0^2}{2} \langle \cos^2(kz - \omega t) \rangle$$

$$= \frac{1}{2}$$





Q: What happens when circularly polarized light is put through a polarizer along the y (or x) axis?

A)
$$I=0$$

B)
$$I = \frac{1}{2} I_0$$

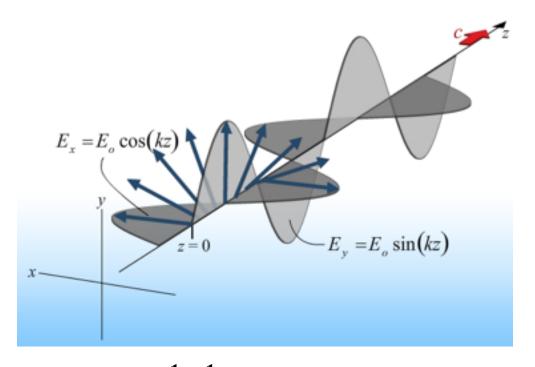
C)
$$I = I_0$$

$$I = \varepsilon_0 c \langle E^2 \rangle$$

$$= \varepsilon_0 c \langle E_x^2 + \mathbf{R}_y^2 \rangle$$

$$= \varepsilon_0 c \frac{E_0^2}{2} \langle \cos^2(kz - \omega t) \rangle$$

$$= \frac{1}{2}$$



$$=\frac{1}{2}\cdot\frac{1}{2}\varepsilon_0cE_0^2$$

Half of before



Q: What happens when circularly polarized light is put through a polarizer along the y (or x) axis?

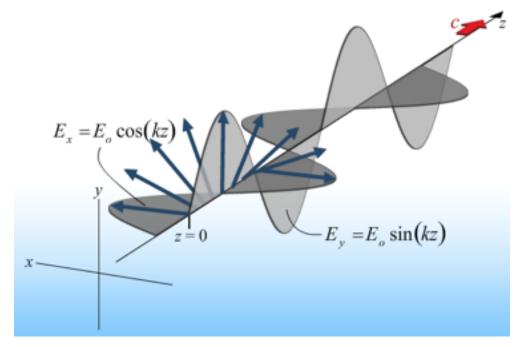
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$$= \varepsilon_0 c \frac{E_0^2}{2} \langle \cos^2(kz - \omega t) \rangle$$

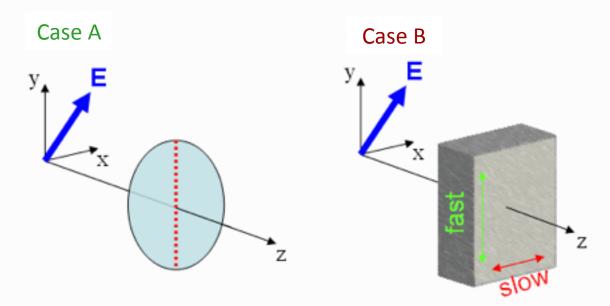
$$= \frac{1}{2}$$



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Half of before

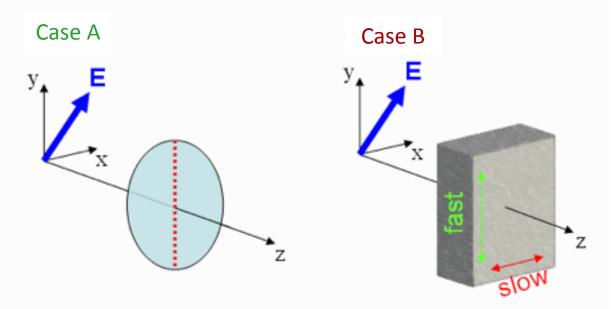
Identical linearly polarized light at 45° from the y-axis and propagating along the z-axis is incident on two different objects. In cas—the light intercepts a linear polarizer with polarization along the y-axis. In case B the light intercepts a quality wave plate with fast axis along the y-axis



Compare the intensities of the light waves after transmission.

- $\bigcirc I_A < I_B$
- $\bigcirc I_A = I_B$
- $\bigcirc I_A > I_B$

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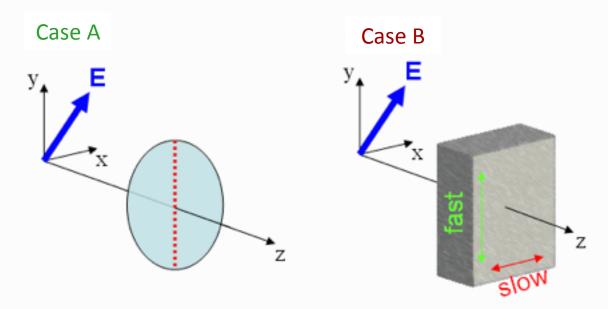
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Case A:

 E_x is absorbed



Identical linearly polarized light at 45° from the y-axis and propagating along the z-axis is incident on two different objects. In cas—the light intercepts a linear polarizer with polarization along the y-axis. In case B the light intercepts a quality wave plate with fast axis along the y-axis



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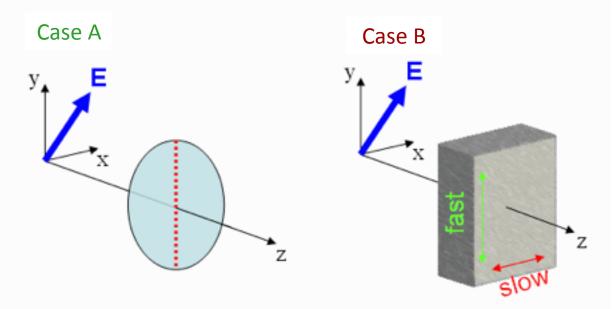
Case A:

 E_x is absorbed

$$I_A = I_0 \cos^2(45^\circ)$$



Identical linearly polarized light at 45° from the y-axis and propagating along the z-axis is incident on two different objects. In cas—the light intercepts a linear polarizer with polarization along the y-axis. In case B the light intercepts a quality wave plate with fast axis along the y-axis



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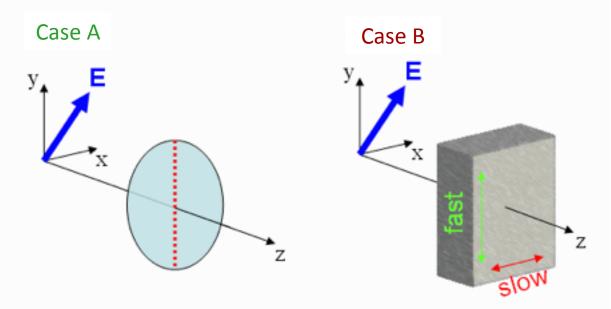
 E_x is absorbed

$$I_A = I_0 \cos^2(45^\circ)$$

$$I_A = \frac{1}{2}I_0$$



Identical linearly polarized light at 45° from the y-axis and propagating along the z-axis is incident on two different objects. In cas—the light intercepts a linear polarizer with polarization along the y-axis. In case B the light intercepts a quality wave plate with fast axis along the y-axis



Compare the intensities of the light waves after transmission.

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Case A:

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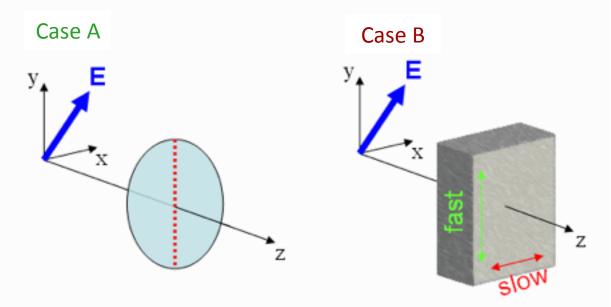
$$I_A = \frac{1}{2}I_0$$

Case B:

$$(E_x, E_y)$$
 phase changed



Identical linearly polarized light at 45° from the y-axis and propagating along the z-axis is incident on two different objects. In cas—the light intercepts a linear polarizer with polarization along the y-axis. In case B the light intercepts a quality wave plate with fast axis along the y-axis



Compare the intensities of the light waves after transmission.

- $\bigcirc I_A < I_B$
- $\bigcirc I_A = I_B$
- $\bigcirc I_A > I_B$

Case A:

 E_x is absorbed

$$I_A = I_0 \cos^2(45^\circ)$$

$$I_A = \frac{1}{2}I_0$$

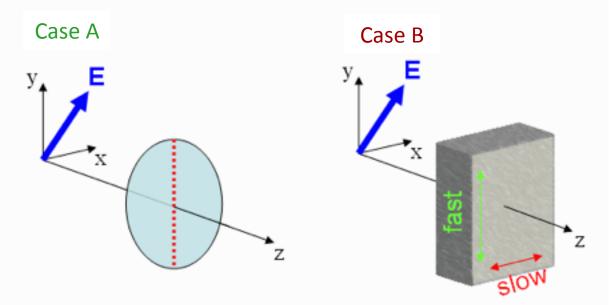
Case B:

 (E_x, E_y) phase changed

$$I_R = I_0$$



Identical linearly polarized light at 45° from the y-axis and propagating along the z-axis is incident on two different objects. In cas—the light intercepts a linear polarizer with polarization along the y-axis. In case B the light intercepts a quality wave plate with fast axis along the y-axis



Compare the intensities of the light waves after transmission.

$$\bigcirc I_A < I_B$$

$$\bigcirc I_A = I_B$$

$$\bigcirc I_A > I_B$$

Case A:

 E_x is absorbed

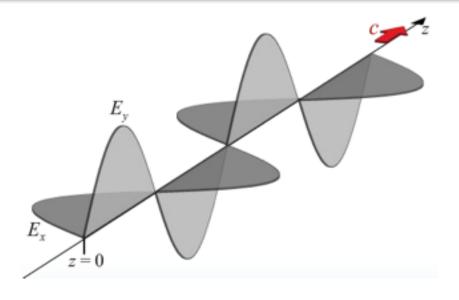
$$I_A = I_0 \cos^2(45^o)$$

$$I_A = \frac{1}{2}I_0$$

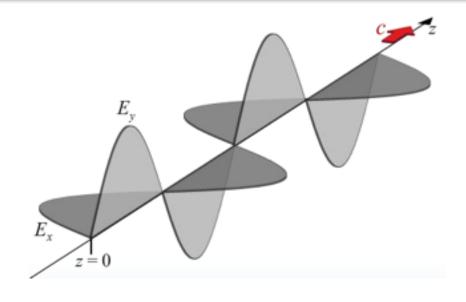
Case B:

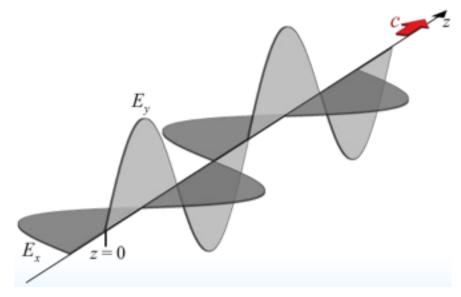
$$(E_x, E_y)$$
 phase changed

$$I_B = I_0$$

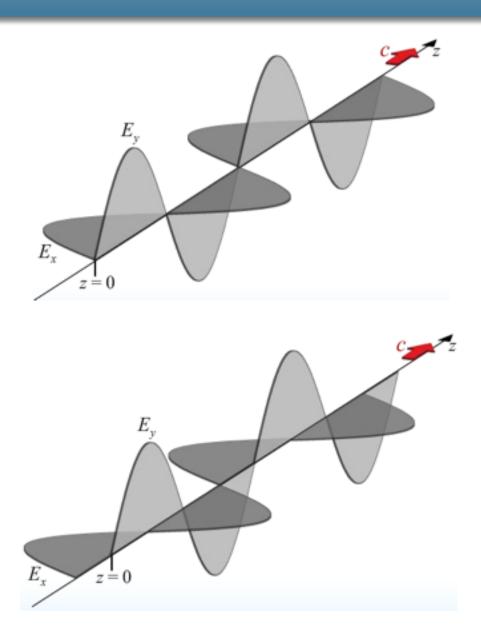










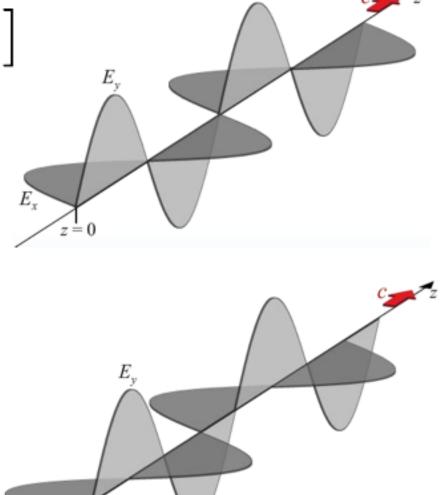


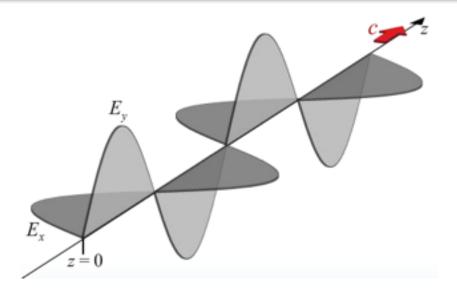
Intensity:

$$I = \epsilon_0 c \left[\langle E_x^2 \rangle + \langle E_y^2 \rangle \right]$$

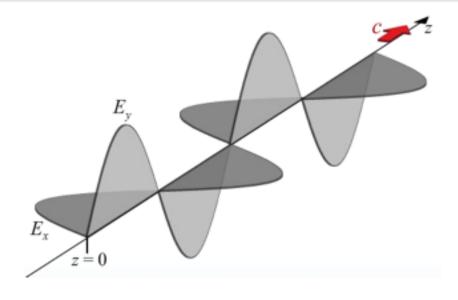


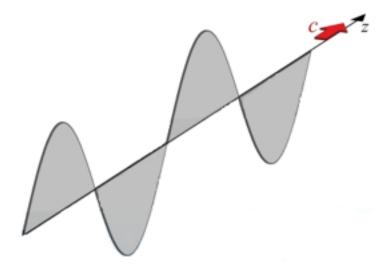
are still there, so intensity is the same







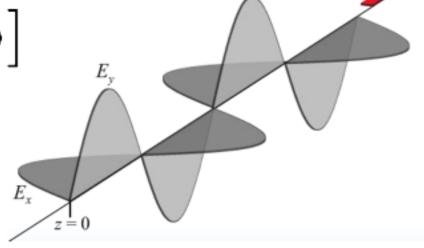


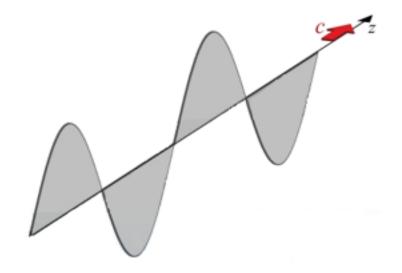


Intensity:

 $I = \epsilon_0 c \left[\langle E_x^2 \rangle + \langle E_y^2 \rangle \right]$





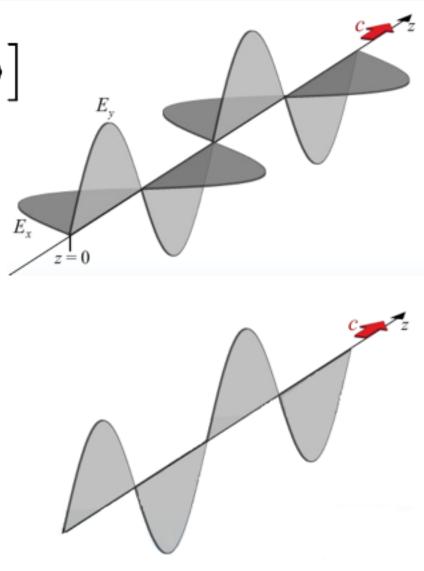


Intensity:

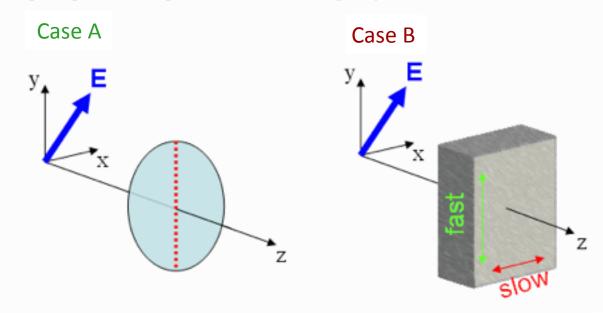
$$I = \epsilon_0 c \left[\langle \mathbf{Z}_x^2 \rangle + \langle E_y^2 \rangle \right]$$



 E_x is missing, so intensity is lower



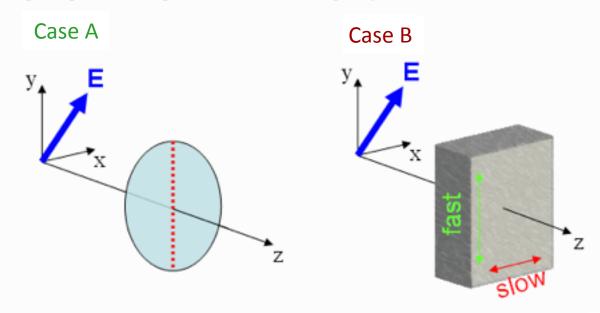




- 8) What is the polarization of the light wave in case B after it passed through the quarter wave plate?
- ate?

- Olinearly polarized
- Oleft circularly polarized
- oright circularly polarized
- Oundefined

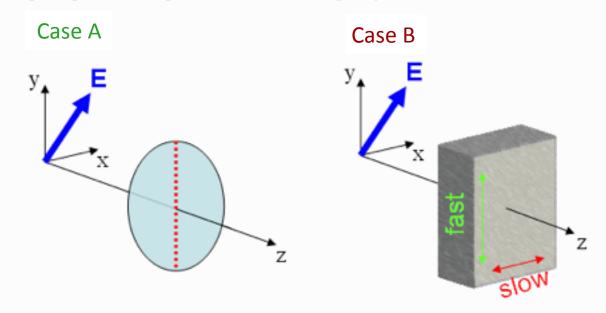




- 8) What is the polarization of the light wave in case B after it passed through the quarter wave plate?
- ate?

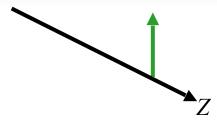
- Olinearly polarized
- Oleft circularly polarized
- oright circularly polarized
- undefined



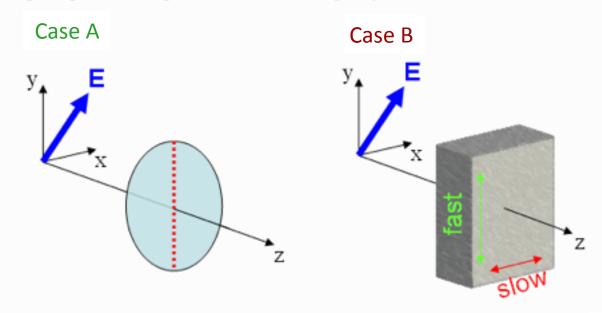


- 8) What is the polarization of the light wave in case B after it passed through the quarter wave plate?
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- oright circularly polarized
- undefined

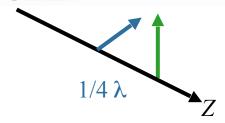






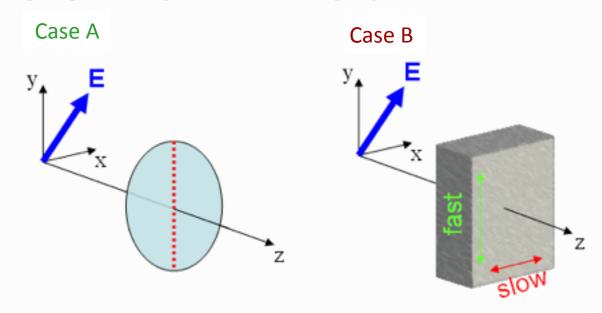
- 8) What is the polarization of the light wave in case B after it passed through the quarter wave plate?
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- undefined





Identical linearly polarized light at 45° from the y-axis and propagating along the z-axis is incident on two different objects. In case A the light intercepts a linear polarizer with polarization along the y-axis. In case B the light intercepts a quarter wave plate with fast axis along the y-axis



- 8) What is the polarization of the light wave in case B after it passed through the quarter wave plate?
- ate?

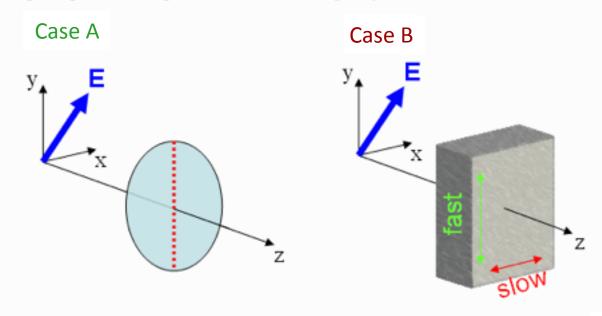
- Olinearly polarized
- Oleft circularly polarized
- oright circularly polarized
- undefined



RCP



Identical linearly polarized light at 45° from the y-axis and propagating along the z-axis is incident on two different objects. In case A the light intercepts a linear polarizer with polarization along the y-axis. In case B the light intercepts a quarter wave plate with fast axis along the y-axis

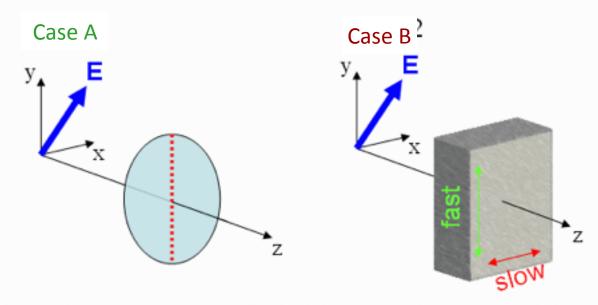


- 8) What is the polarization of the light wave in case B after it passed through the quarter wave plate? Olinearly polarized
- ate?

- Oleft circularly polarized
- night circularly polarized
- undefined

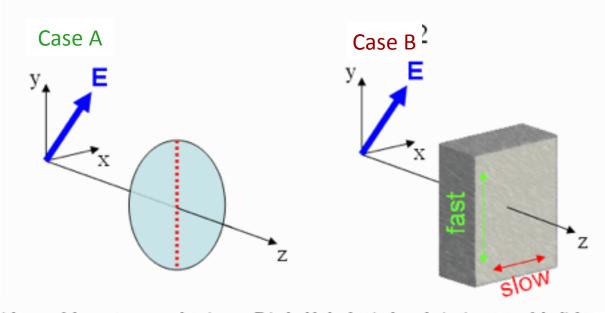


RCP

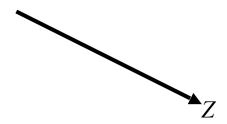


- 10) If the thickness of the quater-wave plate in case B is doubled, what is the polarization state of the light wave after passing through the wave plate?
 - Olinearly polarized
 - oright or left circularly polarized
 - undefined

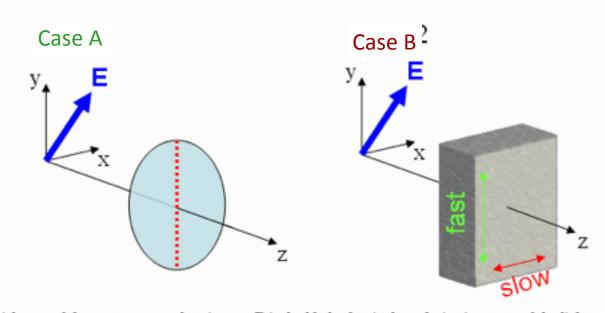




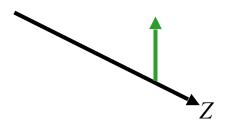
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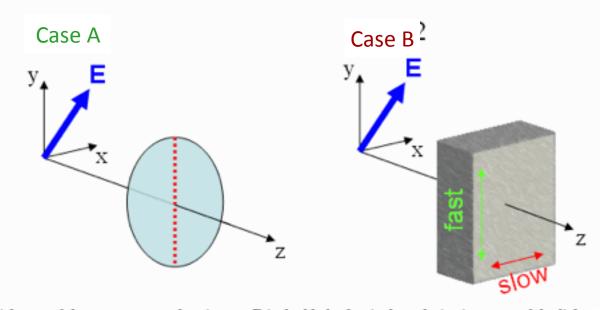




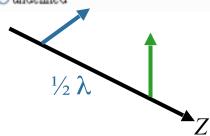
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 - Olinearly polarized
 - oright or left circularly polarized
 - undefined



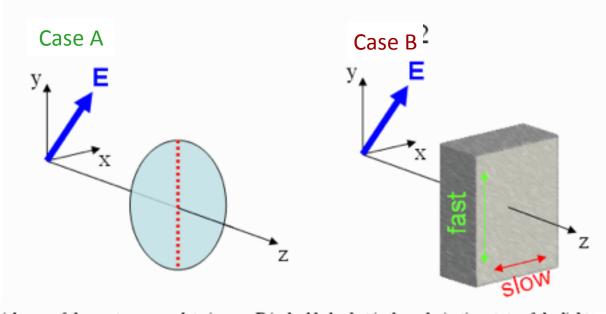




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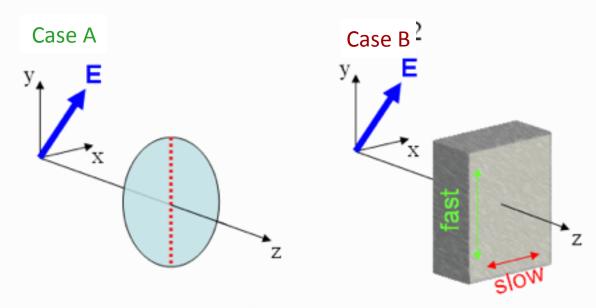


- 10) If the thickness of the quater-wave plate in case B is doubled, what is the polarization state of the light wave after passing through the wave plate?
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 - undefined





Identical linearly polarized light at 45° from the y-axis and propagating along the z-axis is incident on two different objects. In case A the light intercepts a linear polarizer with polarization along the y-axis. In case B the light intercepts a quarter wave plate with fast axis along the y-axis



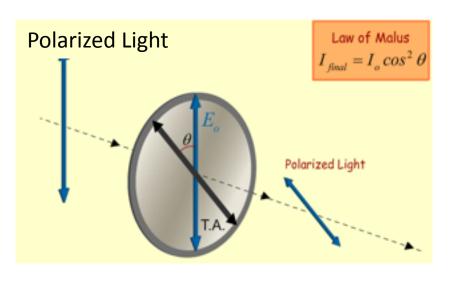
10) If the thickness of the quater-wave plate in case B is doubled, what is the polarization state of the light wave after passing through the wave plate?

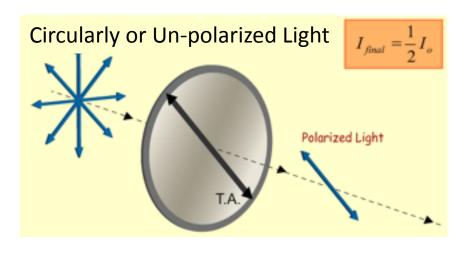
wave after passing through the wave plate?

O linearly polarized
O right or left circularly polarized
O undefined

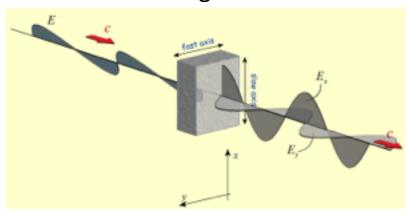
Executive Summary:

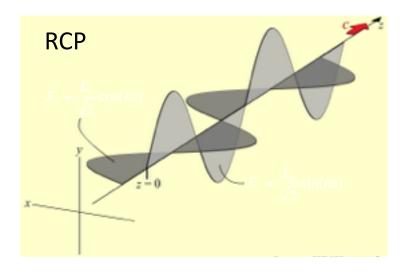
Polarizers & QW Plates:





Birefringence

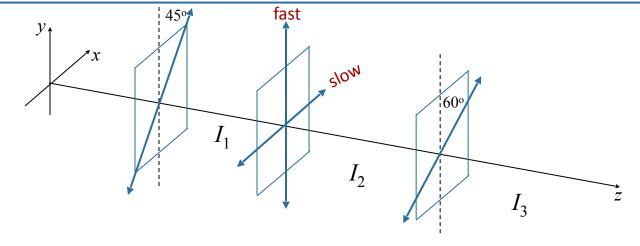




Calculation

Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

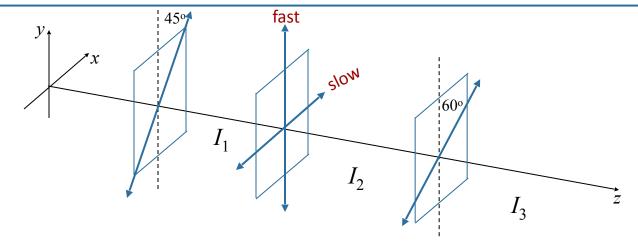
What is the intensity I_3 in terms of I_1 ?



Calculation

Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

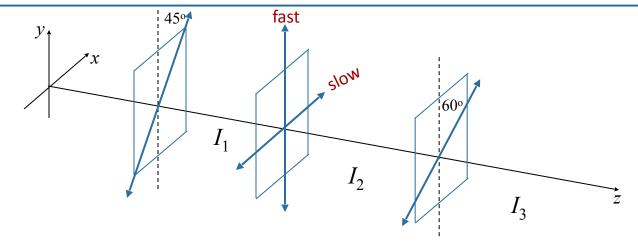
What is the intensity I_3 in terms of I_1 ?



Conceptual Analysis

Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

What is the intensity I_3 in terms of I_1 ?

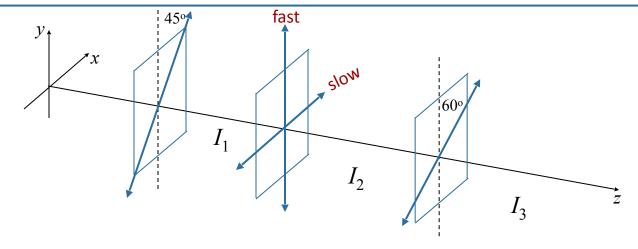


Conceptual Analysis

Linear Polarizers: absorbs E field component perpendicular to TA

Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

What is the intensity I_3 in terms of I_1 ?



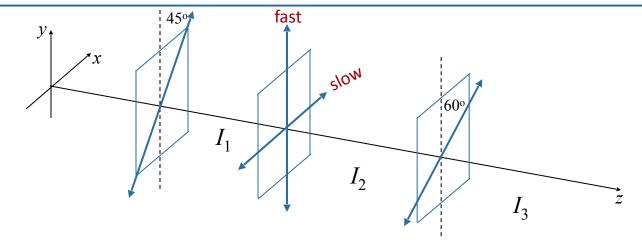
Conceptual Analysis

Linear Polarizers: absorbs E field component perpendicular to TA

Quarter Wave Plates: Shifts phase of E field components in fast-slow directions

Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

What is the intensity I_3 in terms of I_1 ?



Conceptual Analysis

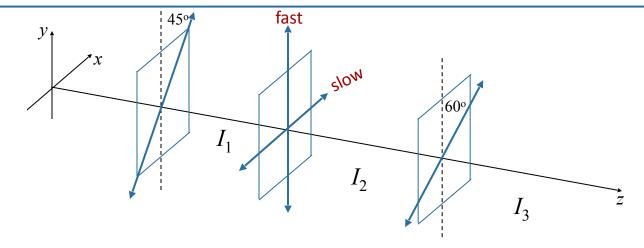
Linear Polarizers: absorbs E field component perpendicular to TA

Quarter Wave Plates: Shifts phase of E field components in fast-slow directions

Strategic Analysis

Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

What is the intensity I_3 in terms of I_1 ?



Conceptual Analysis

Linear Polarizers: absorbs E field component perpendicular to TA

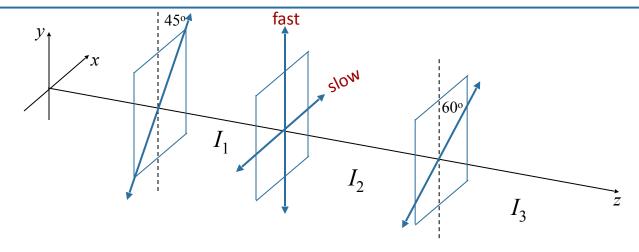
Quarter Wave Plates: Shifts phase of E field components in fast-slow directions

Strategic Analysis

Determine state of polarization and intensity reduction after each object

Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

What is the intensity I_3 in terms of I_1 ?



Conceptual Analysis

Linear Polarizers: absorbs E field component perpendicular to TA

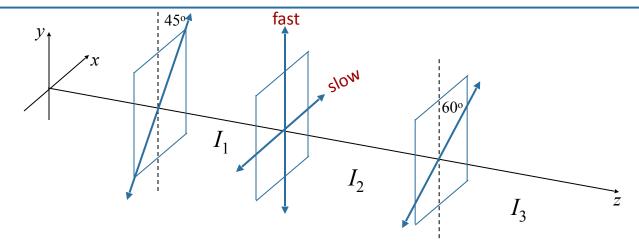
Quarter Wave Plates: Shifts phase of E field components in fast-slow directions

Strategic Analysis

Determine state of polarization and intensity reduction after each object Multiply individual intensity reductions to get final reduction.

Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

What is the intensity I_3 in terms of I_1 ?



Conceptual Analysis

Linear Polarizers: absorbs E field component perpendicular to TA

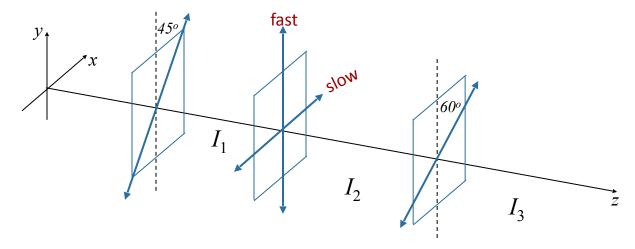
Quarter Wave Plates: Shifts phase of E field components in fast-slow directions

Strategic Analysis

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Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

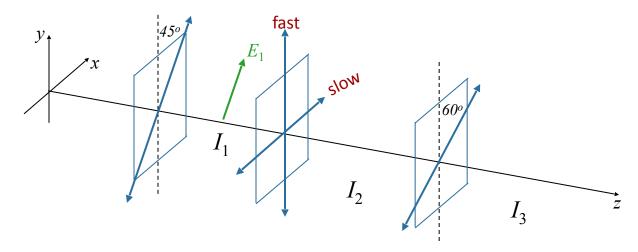


What is the polarization of the light after the QWP?

- B) RCP C) $-\frac{y}{1-x}$ D) $-\frac{y}{1-x}$
- E) un-polarized



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



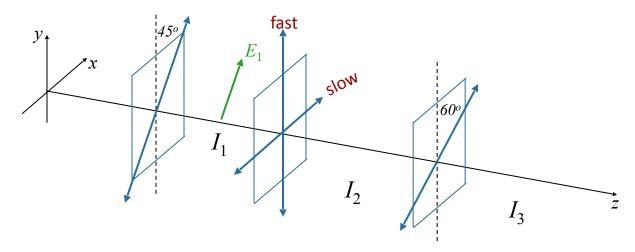
What is the polarization of the light after the QWP?

- B) RCP C) $-\frac{y}{1-x}$ D) $-\frac{y}{1-x}$
- E) un-polarized

Light incident on QWP is linearly polarized at 45° to fast axis



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the QWP?

- A) LCP
- B) RCP
- $C) \xrightarrow{y_{1}} x$
- $D) \longrightarrow x$
- E) un-polarized

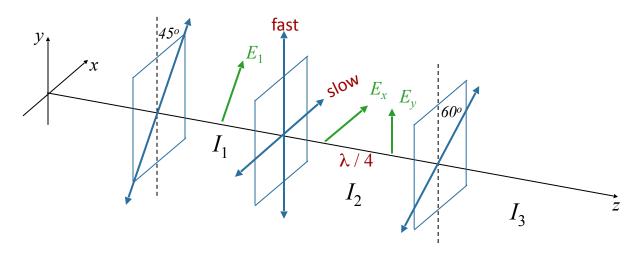
Light incident on QWP is linearly polarized at 45° to fast axis



Light will be circularly polarized after QWP



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the QWP?

A) LCP

B) RCP

C) ----

D) ---

E) un-polarized

Light incident on QWP is linearly polarized at 45° to fast axis



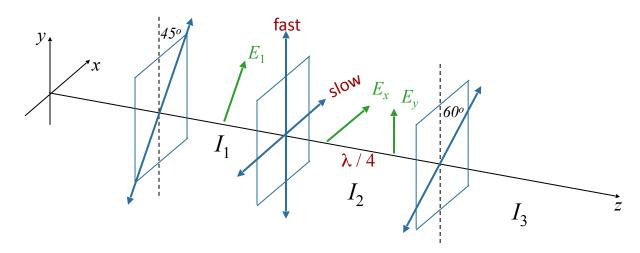
Light will be circularly polarized after QWP

LCP or RCP? Easiest way: Right

Hand Rule:



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the QWP?

A) LCP

B) RCP

y

E) un-polarized

Light incident on QWP is linearly polarized at 45° to fast axis



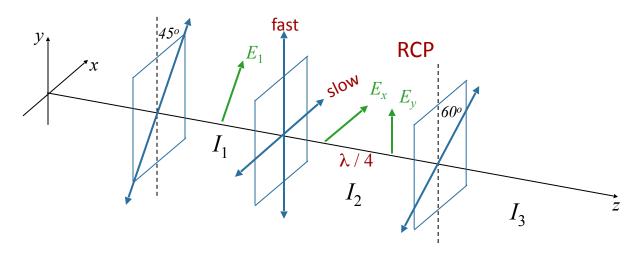
Light will be circularly polarized after QWP

LCP or RCP? Easiest way: Right Hand Rule:

Curl fingers of RH back to front Thumb points in dir of propagation if right hand polarized.



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the QWP?

A) LCP

B) RCP

C)



D)



E) un-polarized

Light incident on QWP is linearly polarized at 45° to fast axis

Light will be circularly polarized after QWP

LCP or RCP? Easiest way: Right Hand Rule:

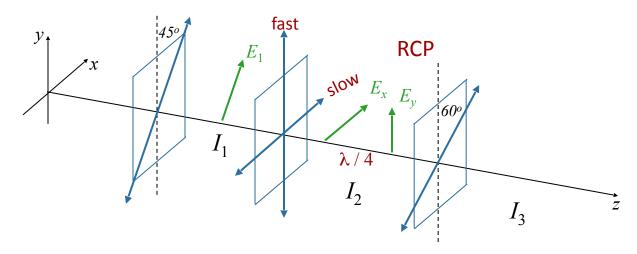
Curl fingers of RH back to front Thumb points in dir of propagation if right hand polarized.



RCP



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the QWP?

A) LCP

B) RCP

C)



D)



E) un-polarized

Light incident on QWP is linearly polarized at 45° to fast axis

Light will be circularly polarized after QWP

LCP or RCP? Easiest way: Right Hand Rule:

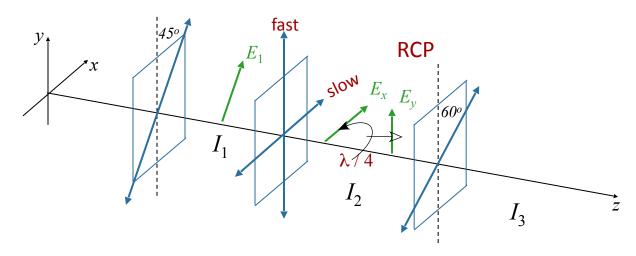
Curl fingers of RH back to front Thumb points in dir of propagation if right hand polarized.



RCP



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the QWP?

A) LCP

B) RCP

C)



D)



E) un-polarized

Light incident on QWP is linearly polarized at 45° to fast axis

Light will be circularly polarized after QWP

LCP or RCP? Easiest way: Right Hand Rule:

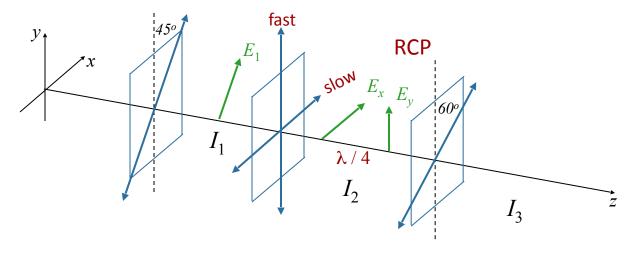
Curl fingers of RH back to front Thumb points in dir of propagation if right hand polarized.



RCP



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_2 of the light after the QWP?

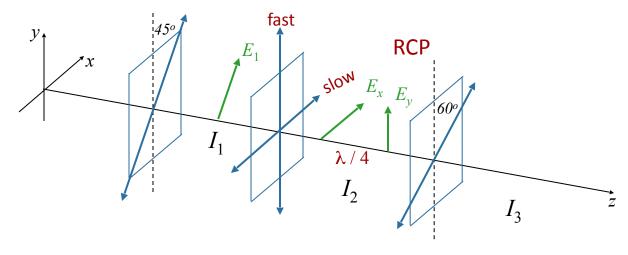
A)
$$I_2 = I_1$$

B)
$$I_2 = \frac{1}{2} I_1$$

C)
$$I_2 = \frac{1}{4} I_1$$



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_2 of the light after the QWP?

A)
$$I_2 = I_1$$

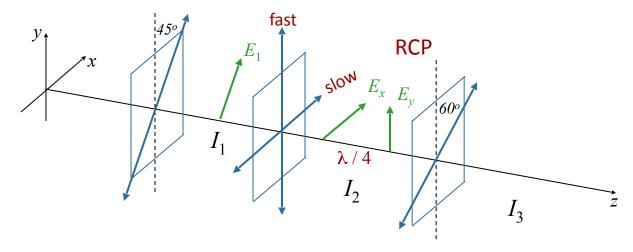
A)
$$I_2 = I_1$$
 B) $I_2 = \frac{1}{2} I_1$

C)
$$I_2 = \frac{1}{4} I_1$$

No absorption: Just a phase change!



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_2 of the light after the QWP?

A)
$$I_2 = I_1$$

B)
$$I_2 = \frac{1}{2} I_1$$

C)
$$I_2 = \frac{1}{4} I_1$$

Before:

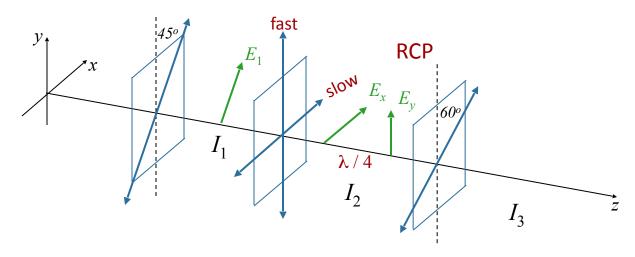
No absorption: Just a phase change!

$$E_x = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_2 of the light after the QWP?

A)
$$I_2 = I_1$$

B)
$$I_2 = \frac{1}{2} I_1$$

C)
$$I_2 = \frac{1}{4} I_1$$

Before:

$$E_x = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$

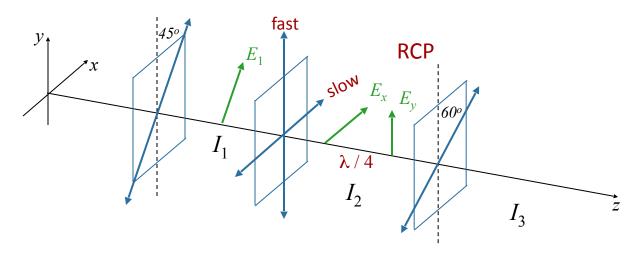
No absorption: Just a phase change!

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_2 of the light after the QWP?

A)
$$I_2 = I_1$$

B)
$$I_2 = \frac{1}{2} I_1$$

C)
$$I_2 = \frac{1}{4} I_1$$

Before:

$$E_x = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$

No absorption: Just a phase change!

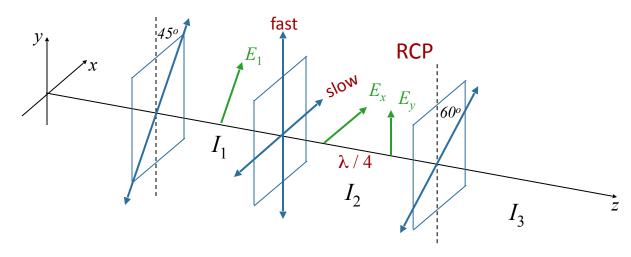
$$I = \epsilon_0 c \left[\langle E_x^2 \rangle + \langle E_y^2 \rangle \right]$$

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_2 of the light after the QWP?

A)
$$I_2 = I_1$$

B)
$$I_2 = \frac{1}{2} I_1$$

C)
$$I_2 = \frac{1}{4} I_1$$

Before:

$$E_x = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$

No absorption: Just a phase change!

$$I = \epsilon_0 c \left[\langle E_x^2 \rangle + \langle E_y^2 \rangle \right]$$

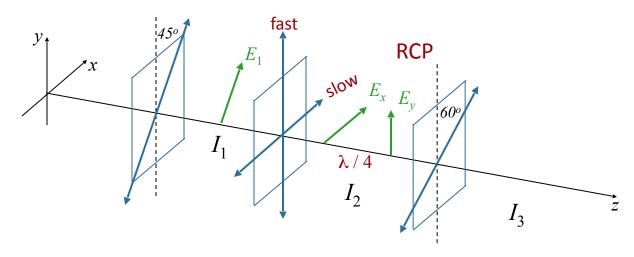
Same before & after!

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_2 of the light after the QWP?

A)
$$I_2 = I_1$$

B)
$$I_2 = \frac{1}{2} I_1$$

C)
$$I_2 = \frac{1}{4} I_1$$

Before:

$$E_x = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$

No absorption: Just a phase change!

$$I = \epsilon_0 c \left[\langle E_x^2 \rangle + \langle E_y^2 \rangle \right]$$

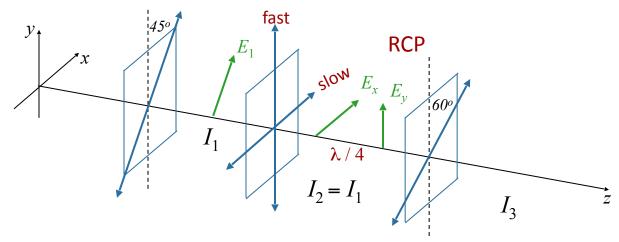
Same before & after!

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

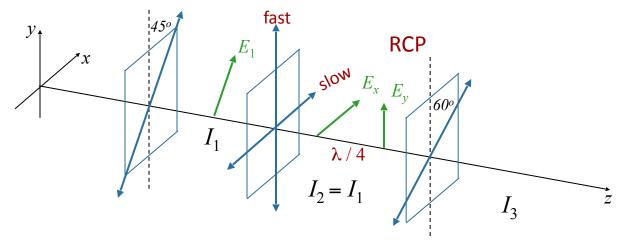


What is the polarization of the light after the 60° polarizer?

- A) LCP
- B) RCP



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the $60^{\rm o}$ polarizer?

A) LCP

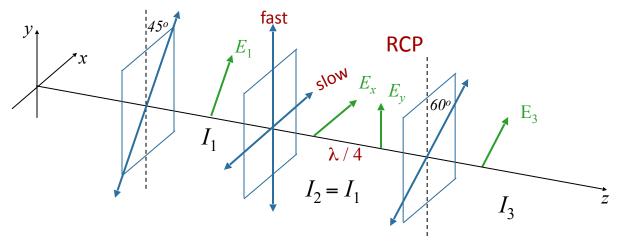
B) RCP

 $C) \xrightarrow{1600} X$

E) un-polarized



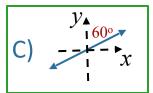
Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the $60^{\rm o}$ polarizer?

A) LCP

B) RCP

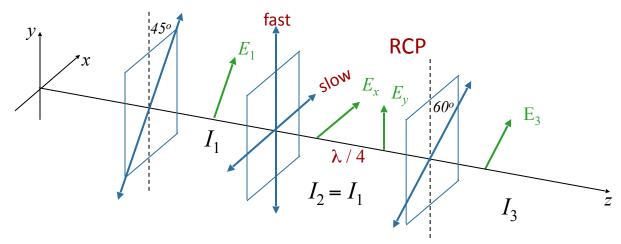


) ----x

E) un-polarized



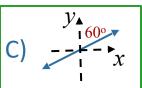
Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



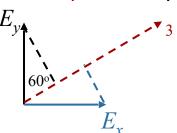
What is the polarization of the light after the $60^{\rm o}$ polarizer?

A) LCP

B) RCP

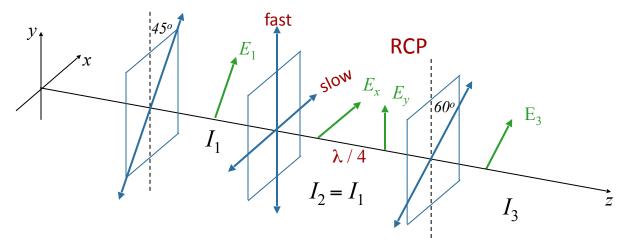


E) un-polarized



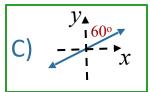


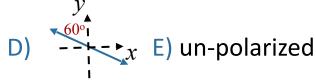
Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

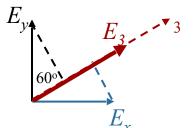


What is the polarization of the light after the $60^{\rm o}$ polarizer?

- A) LCP
- B) RCP



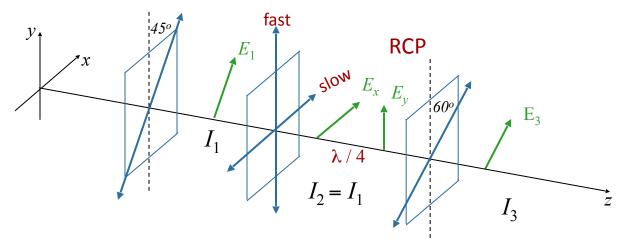




$$E_3 = E_x \sin\theta + E_y \cos\theta$$



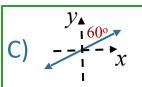
Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the $60^{\rm o}$ polarizer?

A) LCP

B) RCP



D)
$$-\frac{y}{1}$$
 E) un-polarize

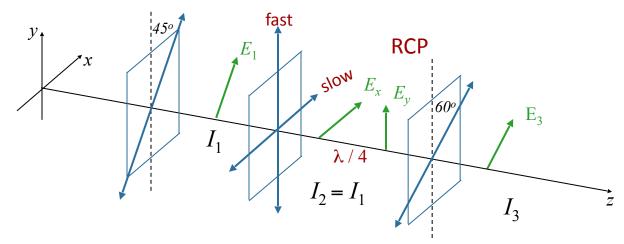
$$E_y$$
 E_3
 E_3
 E_3

$$E_3 = E_x \sin\theta + E_y \cos\theta$$

$$E_{x} = \frac{E_{1}}{\sqrt{2}} \left(\cos(kz - \omega t) \sin\theta + \sin(kz - \omega t) \cos\theta \right)$$

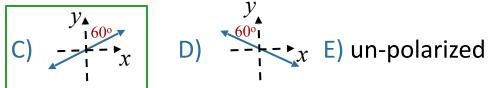


Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the 60° polarizer?

A) LCP



$$) \qquad \begin{array}{c} 60^{\circ} \\ - \\ \end{array}$$

$$E_y$$
 E_3
 E_3
 E_3

$$E_3 = E_x \sin\theta + E_y \cos\theta$$

$$E_3 = \frac{E_1}{\sqrt{2}} \left(\sin(kz - \omega t + \theta) \right)$$

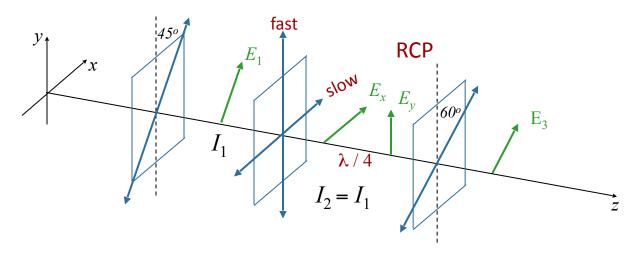
$$E_{3} = E_{x} \sin \theta + E_{y} \cos \theta$$

$$E_{3} = \frac{E_{1}}{\sqrt{2}} \left(\cos(kz - \omega t) \sin \theta + \sin(kz - \omega t) \cos \theta \right)$$





Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

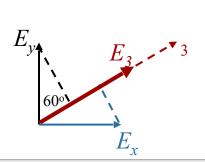


What is the intensity I_3 of the light after the $60^{\rm o}$ polarizer?

A)
$$I_3 = I_1$$

A)
$$I_3 = I_1$$
 B) $I_3 = \frac{1}{2} I_1$

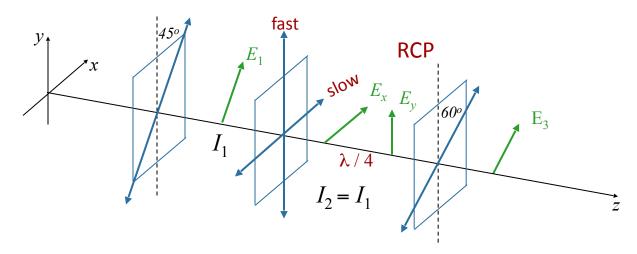
C)
$$I_3 = \frac{1}{4} I_1$$



$$E_3 = \frac{E_1}{\sqrt{2}}$$



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

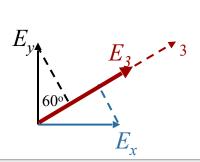


What is the intensity I_3 of the light after the 60° polarizer?

A)
$$I_3 = I_1$$

B)
$$I_3 = \frac{1}{2} I_1$$

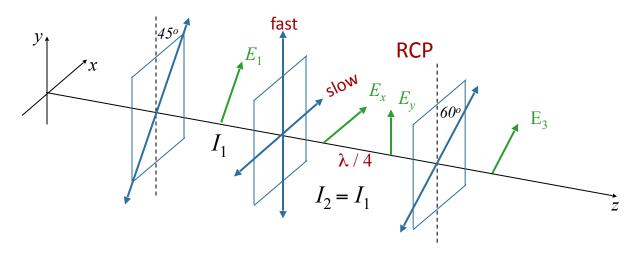
A)
$$I_3 = I_1$$
 B) $I_3 = \frac{1}{2} I_1$ C) $I_3 = \frac{1}{4} I_1$



$$E_3 = \frac{E_1}{\sqrt{2}} \qquad I \propto E^2$$



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

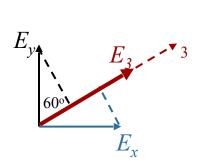


What is the intensity I_3 of the light after the 60° polarizer?

A)
$$I_3 = I_1$$

B)
$$I_3 = \frac{1}{2} I_1$$

A)
$$I_3 = I_1$$
 B) $I_3 = \frac{1}{2} I_1$ C) $I_3 = \frac{1}{4} I_1$



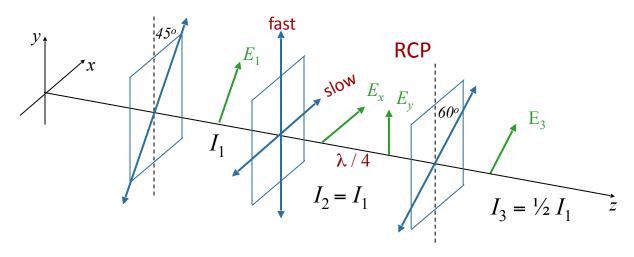
$$E_3 = \frac{E_1}{\sqrt{2}}$$

$$I \propto E^2$$

$$E_3 = \frac{E_1}{\sqrt{2}} \qquad I \propto E^2 \qquad \blacksquare \qquad I_3 = \frac{1}{2}I_1$$



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_3 of the light after the 60° polarizer?

A)
$$I_3 = I_1$$

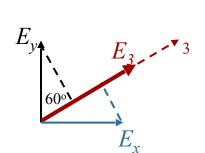
B)
$$I_3 = \frac{1}{2} I_1$$

C)
$$I_3 = \frac{1}{4} I_1$$

$$E_3 = \frac{E_1}{\sqrt{2}}$$

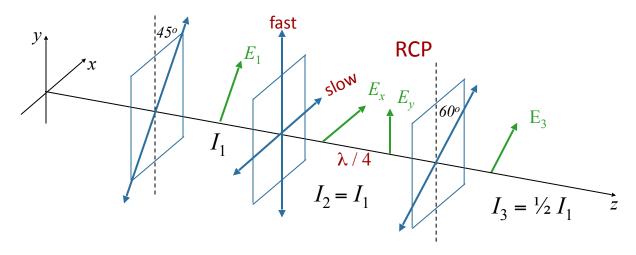
$$I \propto E^2$$

$$E_3 = \frac{E_1}{\sqrt{2}}$$
 $I \propto E^2$ $I_3 = \frac{1}{2}I_1$





Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_3 of the light after the 60° polarizer?

A)
$$I_3 = I_1$$

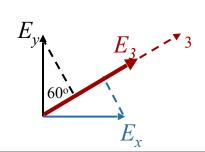
B)
$$I_3 = \frac{1}{2} I_1$$

C)
$$I_3 = \frac{1}{4} I_1$$

$$E_3 = \frac{E_1}{\sqrt{2}}$$

$$I \propto E^2$$

$$E_3 = \frac{E_1}{\sqrt{2}}$$
 $I \propto E^2$ $I_3 = \frac{1}{2}I_1$

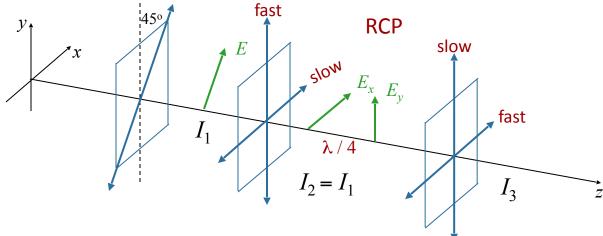


NOTE: This does not depend on θ !

Follow-Up 1



Replace the 60° polarizer with another QWP as shown.



What is the polarization of the light after the last QWP?

A) LCP

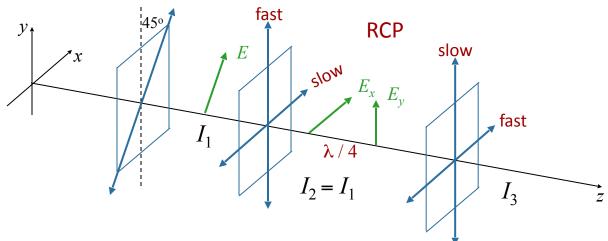
B) RCP

- E) un-polarized

Follow-Up 1



Replace the 60° polarizer with another QWP as shown.



What is the polarization of the light after the last QWP?

A) LCP

B) RCP

- C) ---
- E) un-polarized

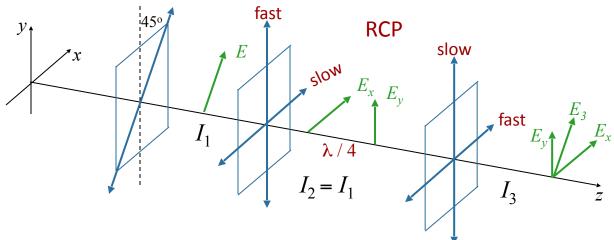
Easiest way:

 $E_{\it fast}$ is λ / 4 ahead of $E_{\it slow}$

Follow-Up 1



Replace the 60° polarizer with another QWP as shown.



What is the polarization of the light after the last QWP?

A) LCP

B) RCP

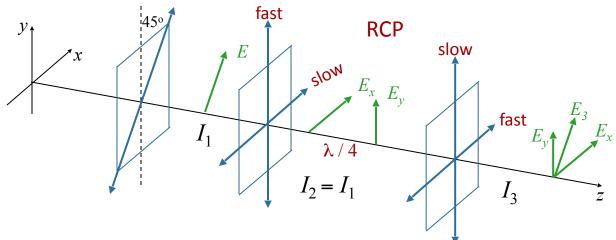
- E) un-polarized

Easiest way:

 E_{fast} is λ / 4 ahead of E_{slow}



Replace the 60° polarizer with another QWP as shown.



What is the polarization of the light after the last QWP?

A) LCP

B) RCP

- C) ---
- E) un-polarized

Easiest way:

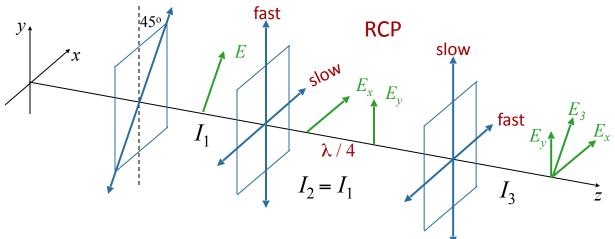
 $E_{\it fast}$ is λ / 4 ahead of $E_{\it slow}$



Brings E_x and E_y back in phase!



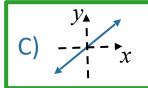
Replace the 60° polarizer with another QWP as shown.

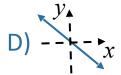


What is the polarization of the light after the last QWP?

A) LCP

B) RCP





E) un-polarized

Easiest way:

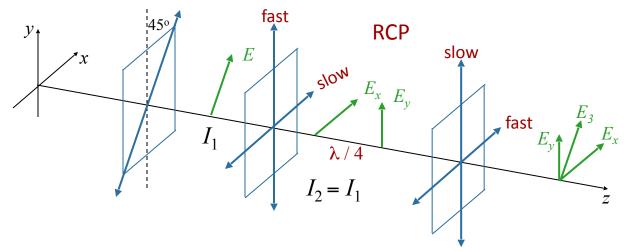
 $E_{\it fast}$ is λ / 4 ahead of $E_{\it slow}$



Brings E_x and E_y back in phase!



Replace the 60° polarizer with another QWP as shown.



What is the intensity I_3 of the light after the last QWP?

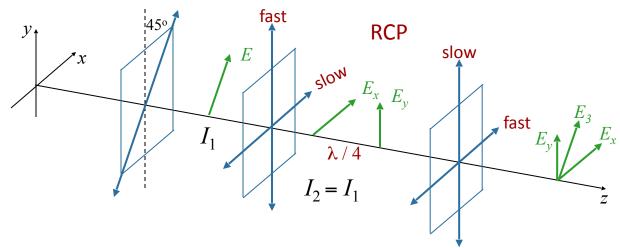
A) I_1

B) $\frac{1}{2}I_1$

C) $\frac{1}{4}I_1$



Replace the 60° polarizer with another QWP as shown.



What is the intensity I_3 of the light after the last QWP?

A)
$$I_1$$

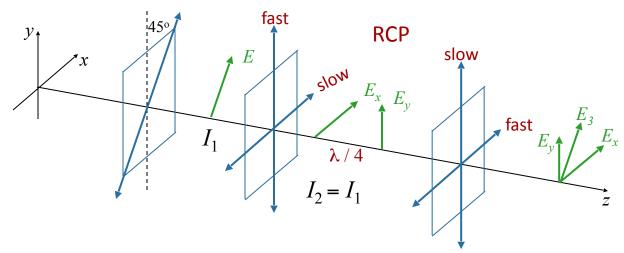
B)
$$\frac{1}{2}I_1$$

C)
$$\frac{1}{4}I_1$$

No absorption: Just a phase change!



Replace the 60° polarizer with another QWP as shown.



What is the intensity I_3 of the light after the last QWP?

A)
$$I_1$$

B)
$$\frac{1}{2}I_1$$

C)
$$\frac{1}{4}I_1$$

Before:

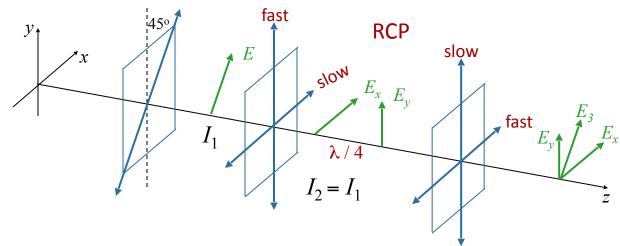
$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

 $E_y = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$

No absorption: Just a phase change!



Replace the 60° polarizer with another QWP as shown.



What is the intensity I_3 of the light after the last QWP?

A)
$$I_1$$

B)
$$\frac{1}{2}I_1$$

C)
$$\frac{1}{4}I_1$$

Before:

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t)$$

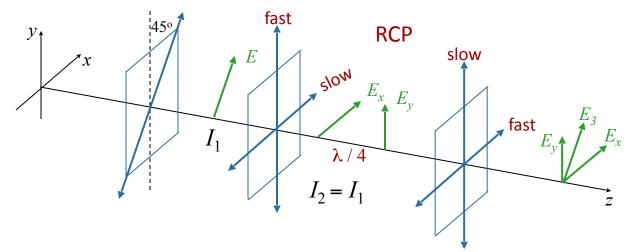
No absorption: Just a phase change!

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_{y} = \frac{E_{1}}{\sqrt{2}}\cos(kz - \omega t)$$



Replace the 60° polarizer with another QWP as shown.



What is the intensity I_3 of the light after the last QWP?

A)
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Before:

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_{y} = \frac{E_{1}}{\sqrt{2}}\sin(kz - \omega t)$$

No absorption: Just a phase change!

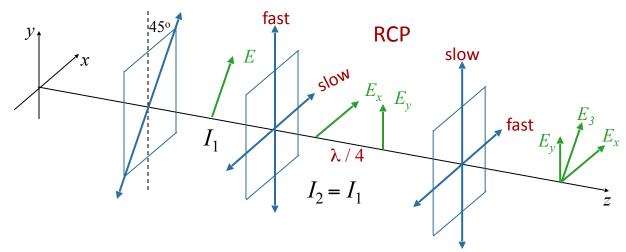
Intensity =
$$\langle E^2 \rangle$$

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$



Replace the 60° polarizer with another QWP as shown.



What is the intensity I_3 of the light after the last QWP?

A)
$$I_1$$

B)
$$\frac{1}{2}I_1$$

C)
$$\frac{1}{4}I_1$$

Before:

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}} \sin(kz - \omega t) \qquad I_{before} = \frac{E_1^2}{2}$$

No absorption: Just a phase change!

Intensity =
$$\langle E^2 \rangle$$

$$I_{before} = \frac{E_1^2}{2}$$

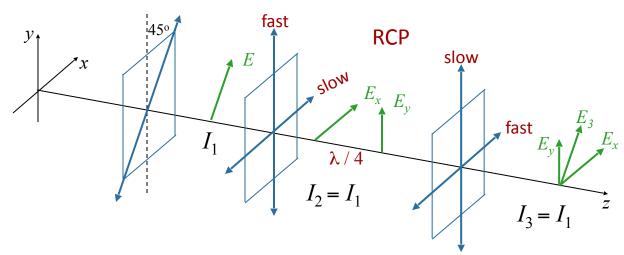
$$I_{after} = \frac{E_1^2}{2}$$

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_y = \frac{E_1}{\sqrt{2}} \cos(kz - \omega t)$$



Replace the 60° polarizer with another QWP as shown.



What is the intensity I_3 of the light after the last QWP?

B)
$$\frac{1}{2}I_1$$

C)
$$\frac{1}{4}I_1$$

Before:

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_{y} = \frac{E_{1}}{\sqrt{2}}\sin(kz - \omega t) \qquad I_{before} = \frac{E_{1}^{2}}{2}$$

No absorption: Just a phase change!

Intensity =
$$\langle E^2 \rangle$$

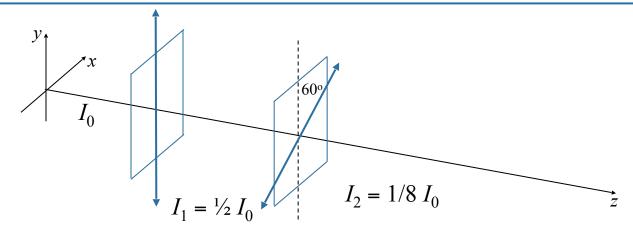
$$I_{after} = \frac{E_1^2}{2}$$

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_{y} = \frac{E_{1}}{\sqrt{2}}\cos(kz - \omega t)$$



Consider light incident on two linear polarizers as shown. Suppose $I_2 = 1/8 I_0$



What is the possible polarization of the input light?

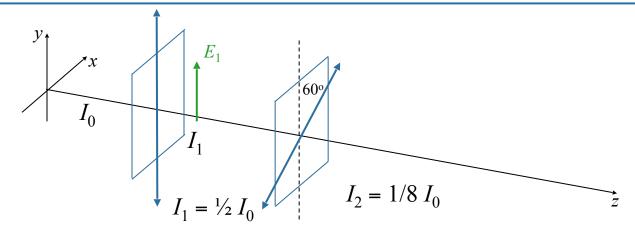
- A) LCP
- C) un-polarized

$$I_2 = 1/8 I_0 \implies I_1 = \frac{1}{2} I_0$$

- D) all of above
- E) none of above



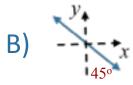
Consider light incident on two linear polarizers as shown. Suppose $I_2 = 1/8 I_0$



What is the possible polarization of the input light?

A) LCP

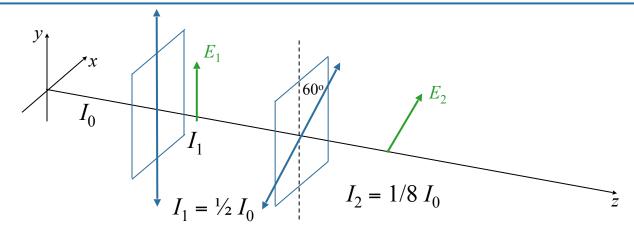
After first polarizer: LP along y-axis with intensity I_1



- C) un-polarized $I_2 = 1/8 I_0 \implies I_1 = \frac{1}{2} I_0$
- D) all of above
- E) none of above



Consider light incident on two linear polarizers as shown. Suppose $I_2 = 1/8 I_0$



What is the possible polarization of the input light?

- A) LCP
- C) un-polarized
- D) all of above
- E) none of above

After first polarizer: LP along y-axis with intensity I_1

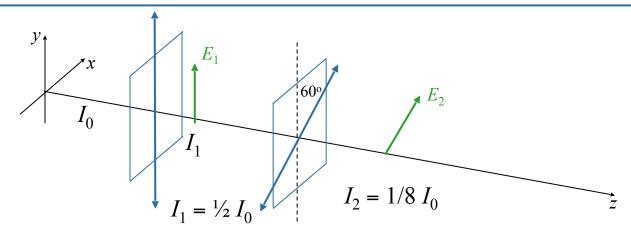
After second polarizer: LP at 60° wrt y-axis

Intensity:
$$I_2 = I_1 \cos^2(60^\circ) = \frac{1}{4} I_1$$

$$I_2 = 1/8 I_0 \implies I_1 = \frac{1}{2} I_0$$



Consider light incident on two linear polarizers as shown. Suppose $I_2 = 1/8 I_0$



What is the possible polarization of the input light?

- A) LCP
- C) un-polarized
- D) all of above
- E) none of above

After first polarizer: LP along y-axis with intensity I_1

After second polarizer: LP at 60° wrt y-axis

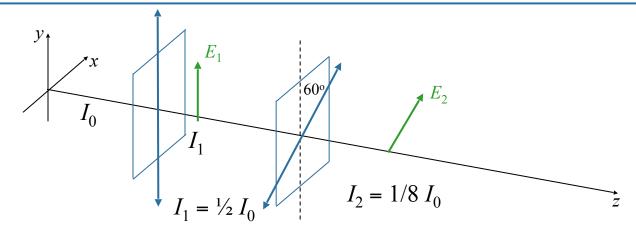
Intensity:
$$I_2 = I_1 \cos^2(60^\circ) = \frac{1}{4} I_1$$

$$I_2 = 1/8 I_0 \implies I_1 = \frac{1}{2} I_0$$

Question is: What kind of light loses ½ of its intensity after passing through vertical polarizer?



Consider light incident on two linear polarizers as shown. Suppose $I_2 = 1/8 I_0$



What is the possible polarization of the input light?

- A) LCP
- B) -- x
- C) un-polarized
- D) all of above
- E) none of above

After first polarizer: LP along y-axis with intensity I_1

After second polarizer: LP at 60° wrt y-axis

Intensity:
$$I_2 = I_1 \cos^2(60^\circ) = \frac{1}{4} I_1$$

$$I_2 = 1/8 I_0 \implies I_1 = \frac{1}{2} I_0$$

Question is: What kind of light loses ½ of its intensity after passing through vertical polarizer?

Answer: Everything except LP at θ other than 45°