Classical Mechanics
Lecture 15

Today's Concepts:

a) Parallel Axis Theorem

b) Torque & Angular Acceleration


UGH...
WHAT HAPPENED?
WHERE AM I?
FWOOOOOOOSH
HELP! SOMEONE
HUH. LOOKS LIKE PHYSICS PROFESSORS DON'T LIKE WORKING IN FRICTIONLESS VACUUMS AFTER ALL.
THEY'RE SUCH LIARS.

Your Comments

idk

TODO, POR FAVOR!!! NO ENTIENDO NADA!!!!!!!!!!!!!!!!!!!!! AYUDA SENOR!!

Your Comments (old)

I do not at ALL like the explanation of the right hand rule. It seems that forces are pointing out of the page in a direction where there is no motion or velocity! I have run into this before, and I think the Right Hand Rule should have stayed with Electricity & Magnetism where it belongs (and makes sense). It seems like nothing more than a useless obfuscation when applied to Torque!

meh right hand rule

Explain the moment of inertia in the different rotational axis. Which one will have the largest, smallest etc...

I hate rotational inertia. It is the bane of my physics existence. Is there any easy way to to find it?

how to approach moment of inertia problems...also in H.S. I wanted to start a band called INERTIA :)

I like physics way more than math.

TODO, POR FAVOR!!! NO ENTIENDO NADA!!!!!!!!!!!!!!!!!!!!! AYUDA SENOR!!

Your Comments

Have you seen my dawg? http://www.tumblr.com/tagged/lost-dawg

Maybe I'm missing something but cross products seem easier to find that dot products. Also, the parallel axis theorem itself was confusing; I had an okay time with torque though.

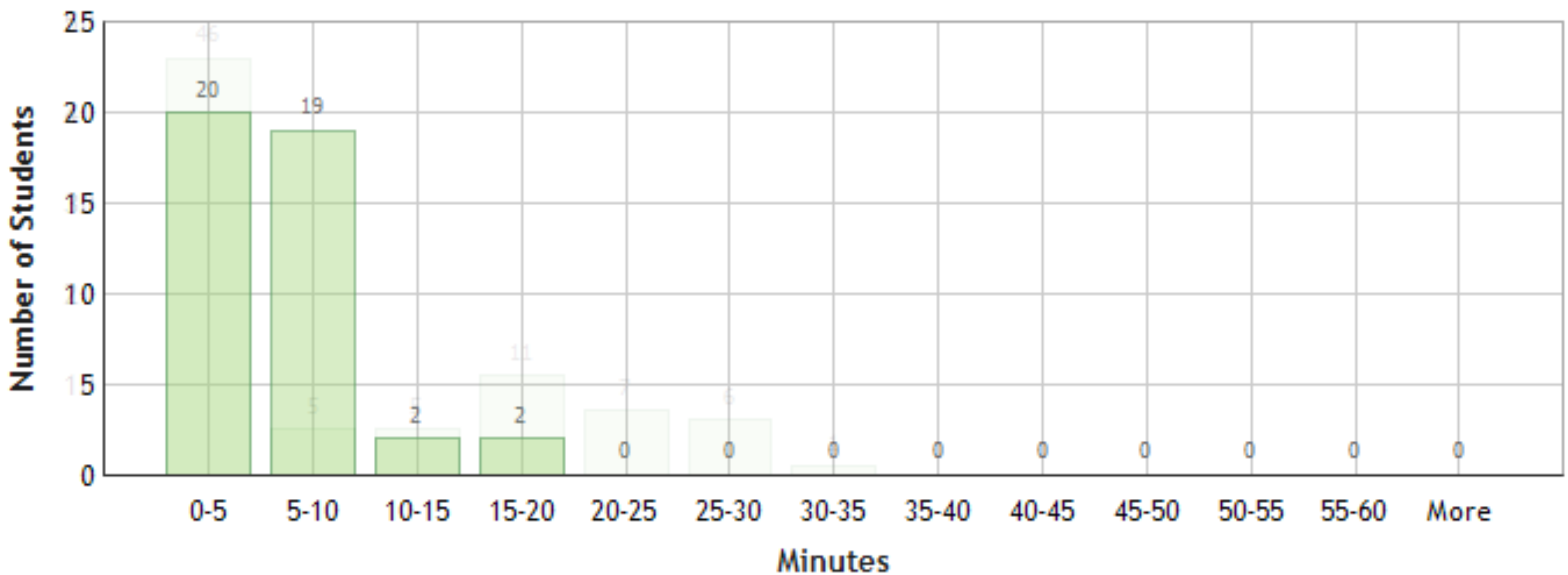
I'm lost in translation, transition,transaction,and transformation. Or simply lost after second midterm.

Thanx God its Friiiiiiidaaaaaayyyyy :D ummmmm ,,, this lecture is a little confusing ,, we need more explanation please

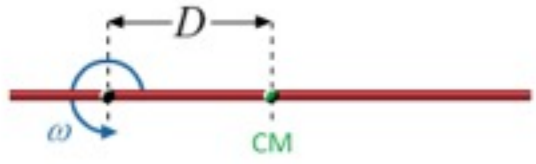
Direction of angular velocity and acceleration, what is the result of the motion because of that.

moment of inertia is the only hard part. torque is all review so no big deal

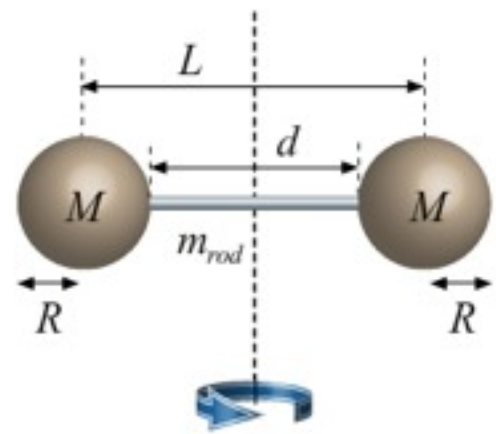
Time Spent Viewing Assignment (N = 43)



Parallel Axis Theorem



$$I_{Total} = MD^2 + I_{CM}$$



$$I_{Dumbbell} = \frac{1}{12} m_{rod} d^2 + 2\left[\frac{2}{5}MR^2 + M\left(\frac{L}{2}\right)^2\right]$$

Smallest when $D = 0$

I honestly don't see the significance or use of the parallel axis theorem. im sure its great and important but maybe you can convince of its greatness. i feel this way because i feel like i can just calculate the moment of inertia in the same way we learned on tuesday

Clicker Question

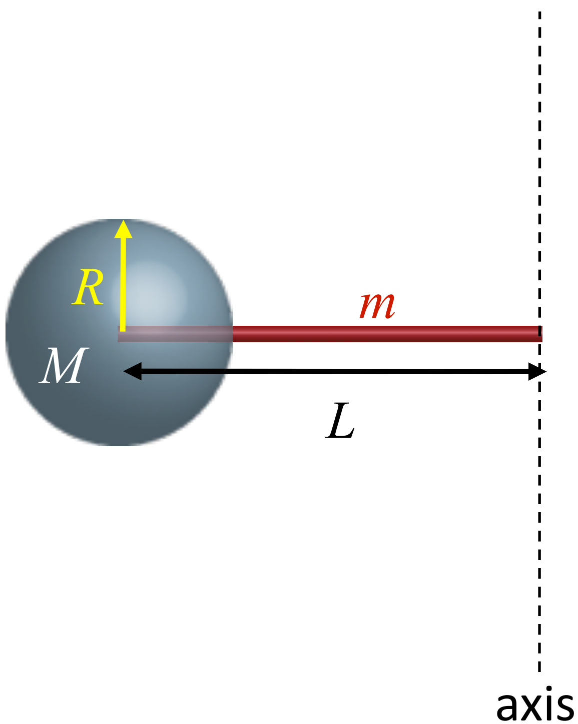
A solid ball of mass M and radius is connected to a rod of mass m and length L as shown. What is the moment of inertia of this system about an axis perpendicular to the other end of the rod?

A) $I = \frac{2}{5}MR^2 + ML^2 + \frac{1}{3}mL^2$

B) $I = \frac{2}{5}MR^2 + mL^2 + \frac{1}{3}ML^2$

C) $I = \frac{2}{5}MR^2 + \frac{1}{3}mL^2$

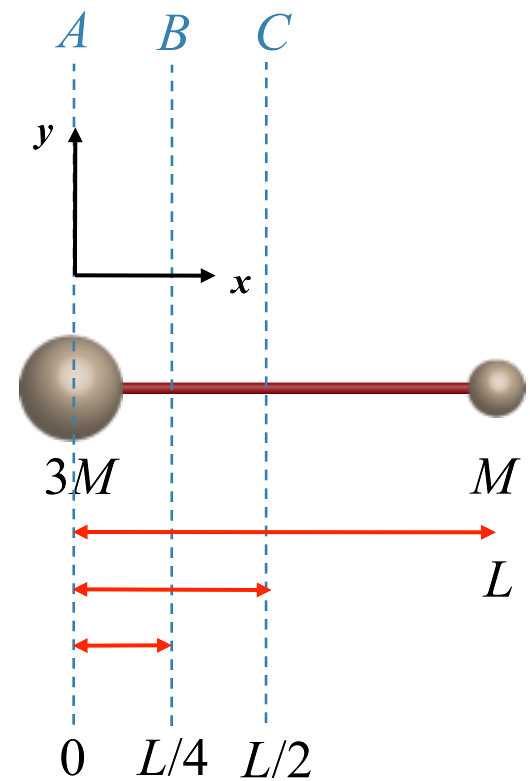
D) $I = ML^2 + \frac{1}{3}mL^2$



CheckPoint

A ball of mass $3M$ at $x = 0$ is connected to a ball of mass M at $x = L$ by a massless rod. Consider the three rotation axes A, B, and C as shown, all parallel to the y axis.

For which rotation axis is the moment of inertia of the object smallest? (It may help you to figure out where the center of mass of the object is.)



75% got this right

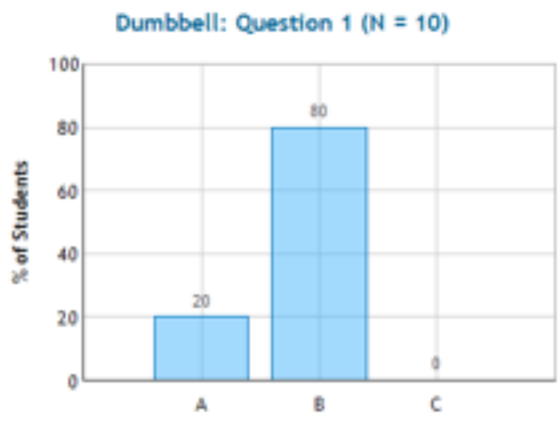
CheckPoint

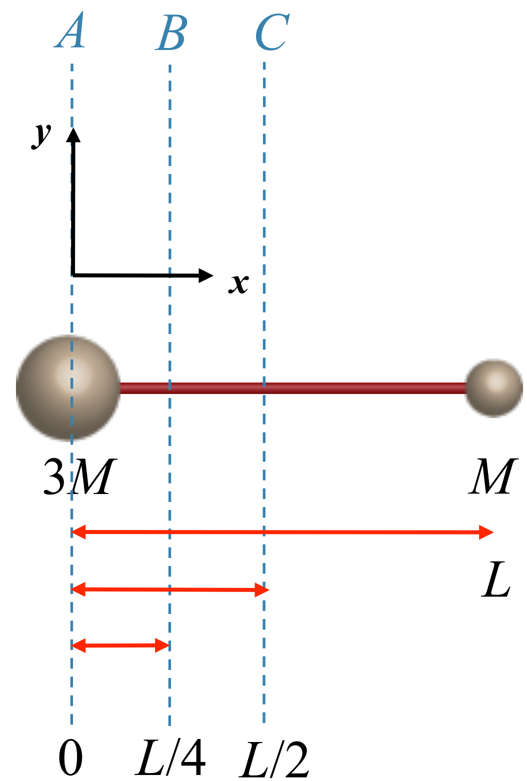
For which rotation axis is the moment of inertia of the object smallest?

A) Less mass is rotating at point a.

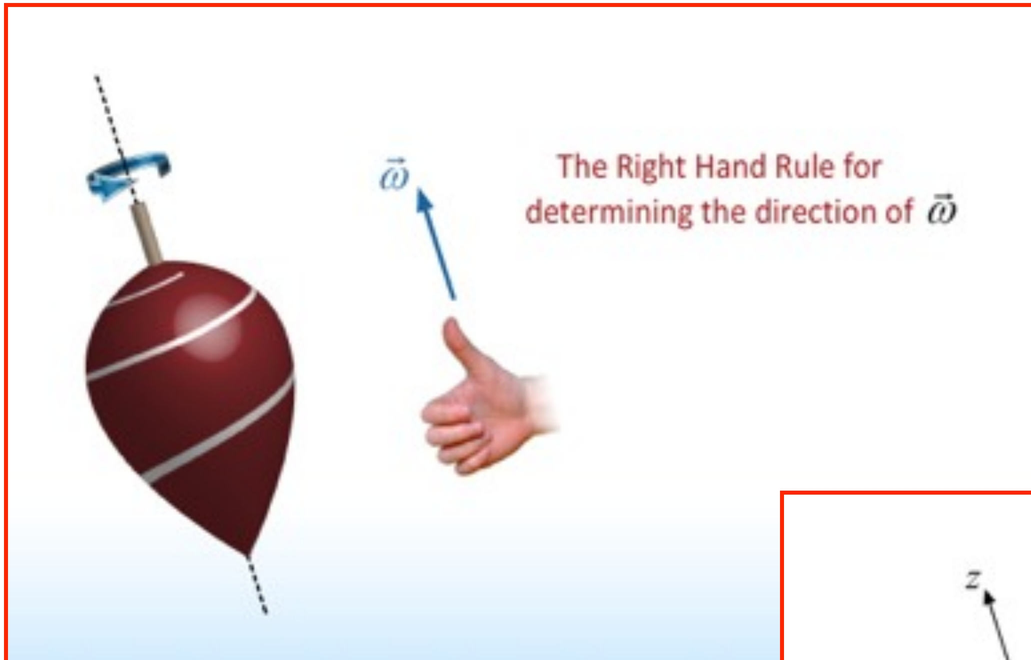
B) The smallest moment of inertia is at the centre of mass which is closest to the most massive ball (3M).

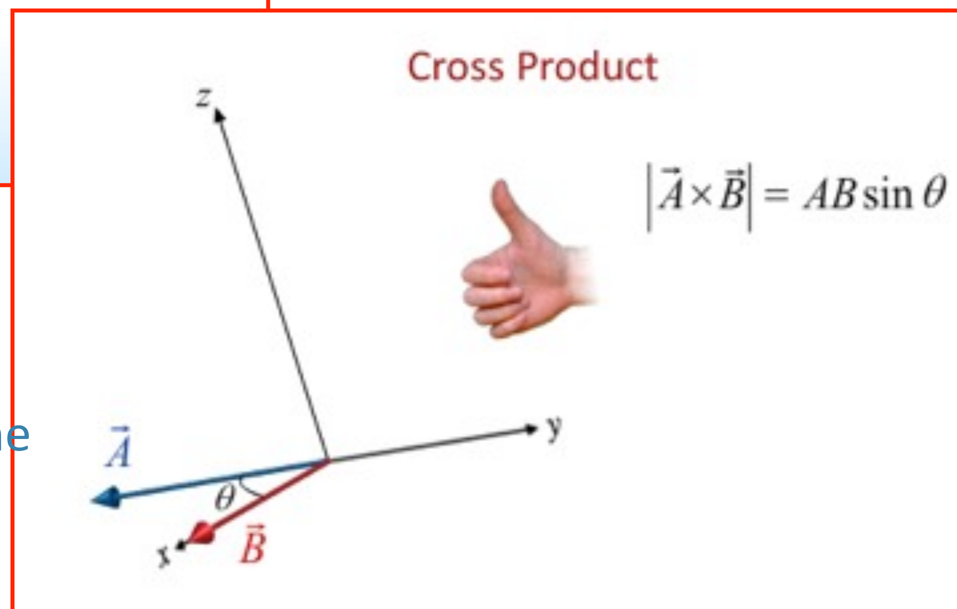
C) I did the equation on paper. This one was actually kind of tricky.





Right Hand Rule for finding Directions





Why do the angular velocity and acceleration point perpendicular to the plane of rotation?

Clicker Question

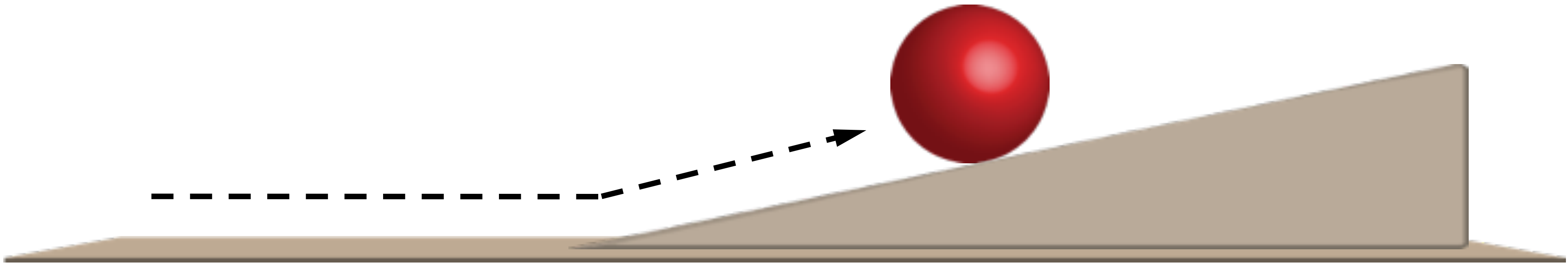
A ball rolls across the floor, and then starts up a ramp as shown below. In what direction does the angular velocity vector point when the ball is rolling up the ramp?

A) Into the page

B) Out of the page

C) Up

D) Down

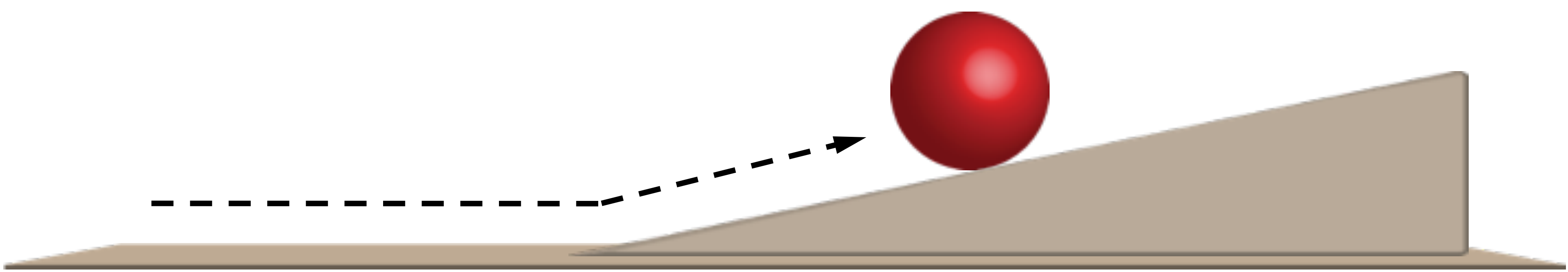


Clicker Question

A ball rolls across the floor, and then starts up a ramp as shown below. In what direction does the angular acceleration vector point when the ball is rolling up the ramp?

A) Into the page

B) Out of the page

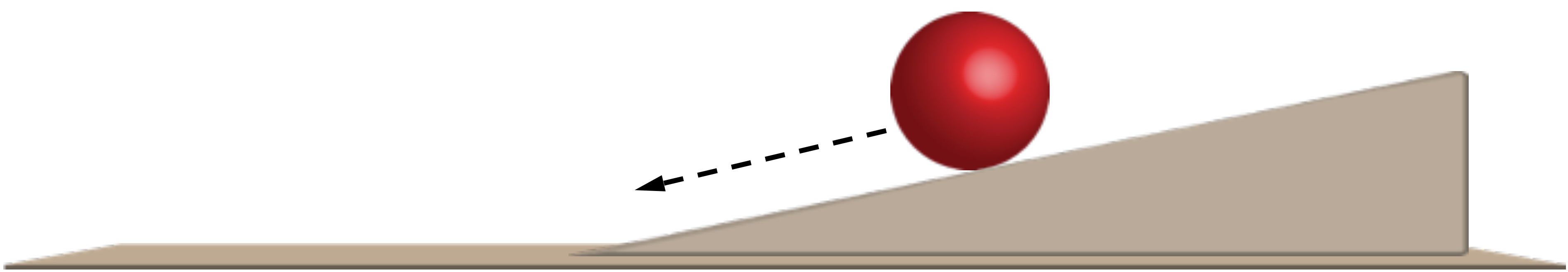


Clicker Question

A ball rolls across the floor, and then starts up a ramp as shown below. In what direction does the angular acceleration vector point when the ball is rolling back down the ramp?

A) into the page

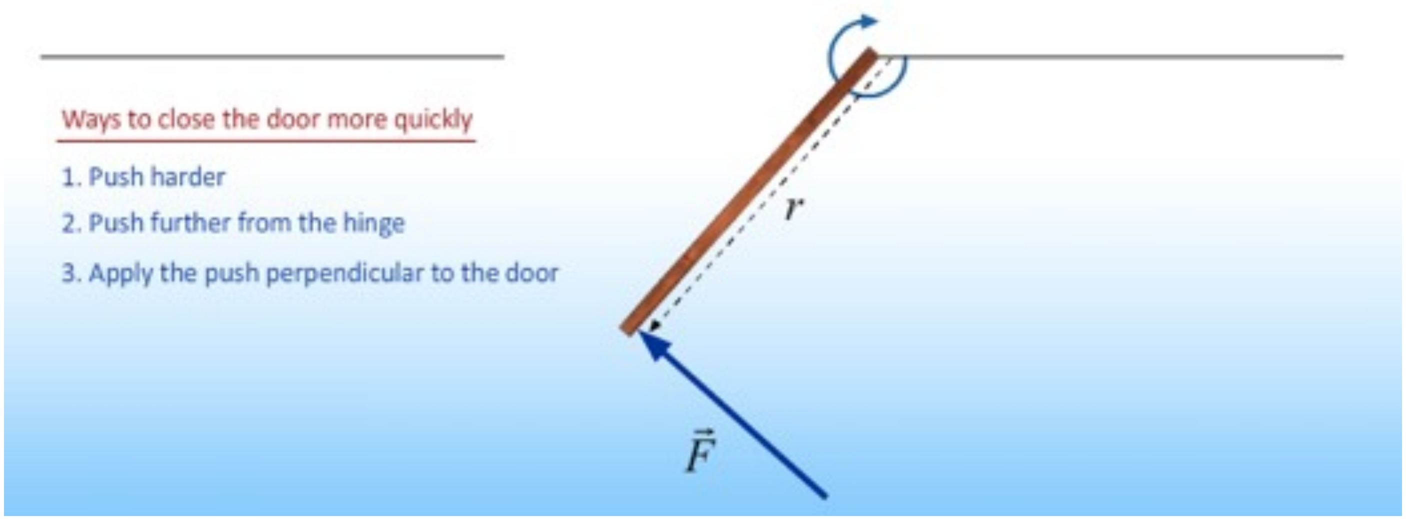
B) out of the page



Torque

$$\tau = rF\sin(\theta\ )$$

Torque $\tau = rF_{\theta} = I\alpha$

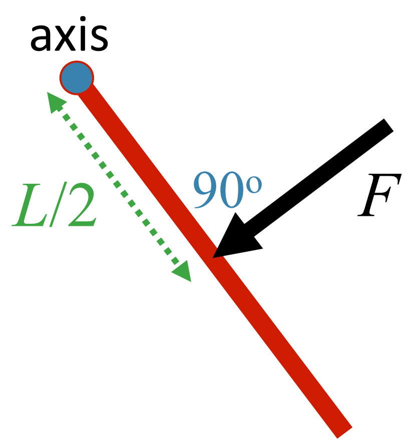


CheckPoint

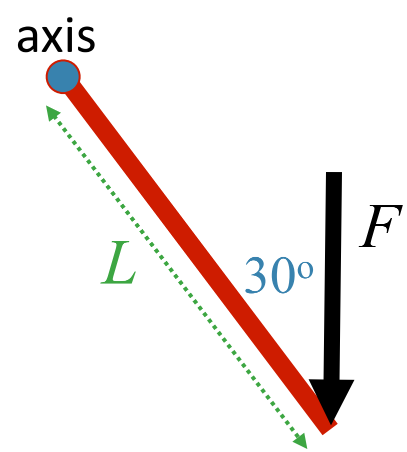
In Case 1, a force F is pushing perpendicular on an object a distance $L/2$ from the rotation axis. In Case 2 the same force is pushing at an angle of 30 degrees a distance L from the axis.

In which case is the torque due to the force about the rotation axis biggest?

A) Case 1 B) Case 2 C) Same



Case 1



Case 2

64% got this right

CheckPoint

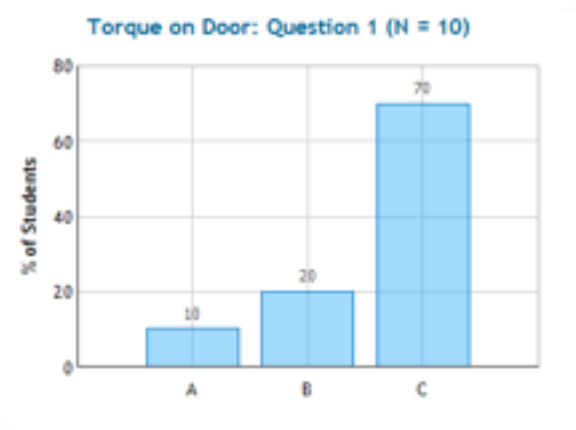
In which case is the torque due to the force about the rotation axis biggest?

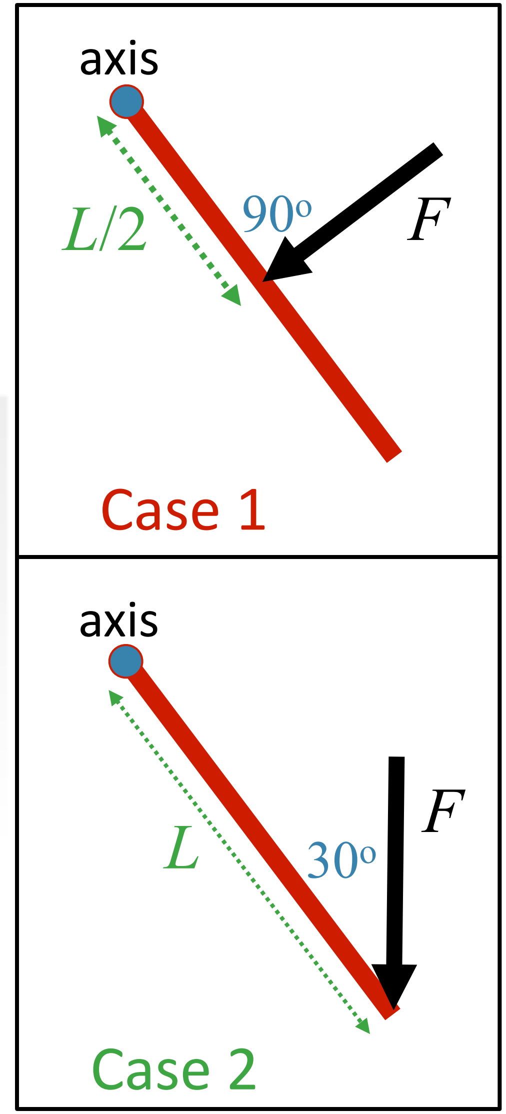
A) Case 1 B) Case 2 C) Same

A) perpendicular force acting miultiplied by perpendicular distance from the axis of rotation is torque

B) More of the force is paralllel

C) For case 1, the magnitude of the torque is F*(L/2). For case 2, the magnitude of the torque is F*sin(30 degrees)*L = F*L/2, which is exactly the same as the one in case 1.





Similarity to 1D motion

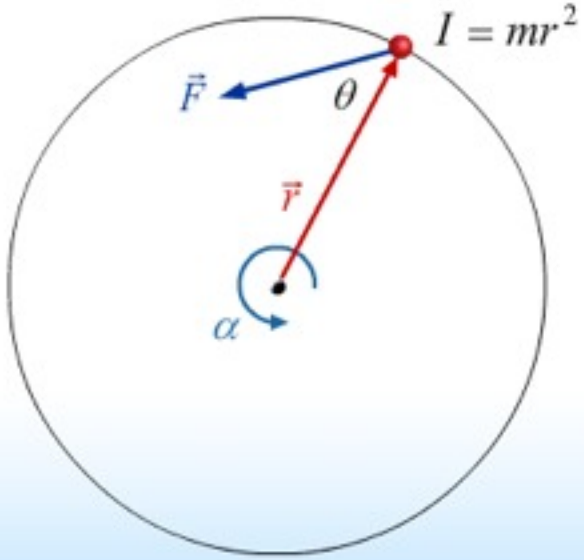
Linear Motion		Rotational Motion
$x = x_o + v_o t + \frac{1}{2} a t^2$	$\longleftrightarrow$	$\theta = \theta_o + \omega_o t + \frac{1}{2} \alpha t^2$
$v = v_o + at$	$\longleftrightarrow$	$\omega = \omega_o + \alpha t$
m	$\longleftrightarrow$	I
$\frac{1}{2} m v^2$	$\longleftrightarrow$	$\frac{1}{2} I \omega^2$
$\vec{F} = m\vec{a}$	$\longleftrightarrow$	$\vec{\tau} = I\vec{\alpha}$

Torque

$$\vec{\tau} \equiv \vec{r} \times \vec{F}$$

$$|\vec{\tau}| = |\vec{r}||\vec{F}|\sin\theta$$

$$\vec{\tau}_{Net} = I\vec{\alpha}$$



Clicker Question

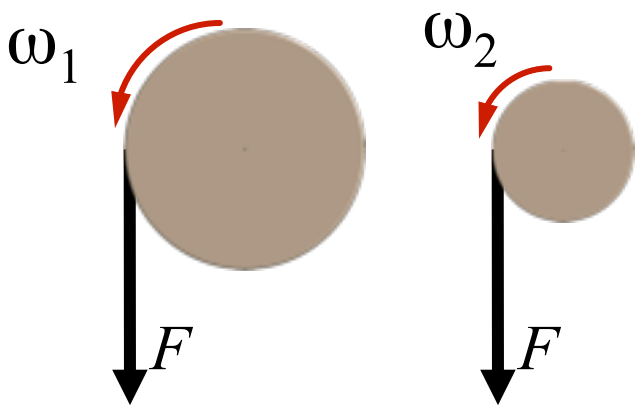
Strings are wrapped around the circumference of two solid disks and pulled with identical forces. Disk 1 has a bigger radius, but both have the same moment of inertia.

Which disk has the biggest angular acceleration?

A) Disk 1

B) Disk 2

C) same



CheckPoint

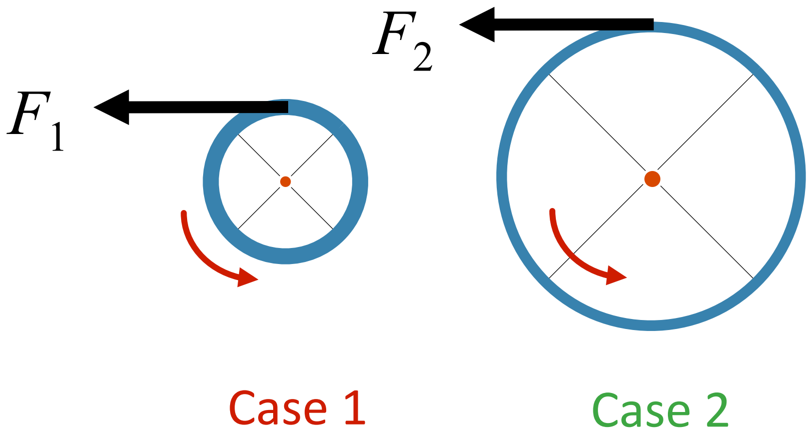
Two hoops can rotate freely about fixed axles through their centers. The hoops have the same mass, but one has twice the radius of the other. Forces F_1 and F_2 are applied as shown.

How are the magnitudes of the two forces related if the angular acceleration of the two hoops is the same?

A) $F_2 = F_1$

B) $F_2 = 2F_1$

C) $F_2 = 4F_1$



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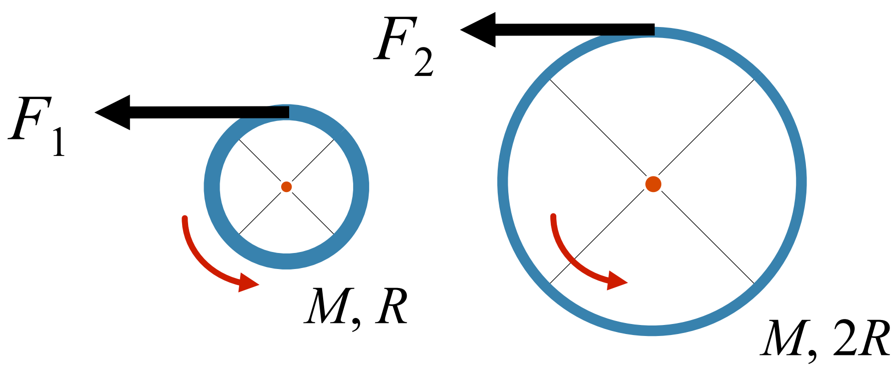
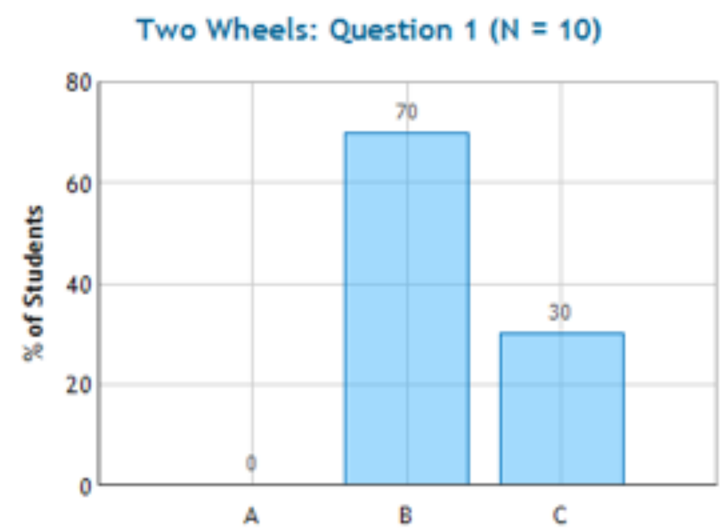


Case 1



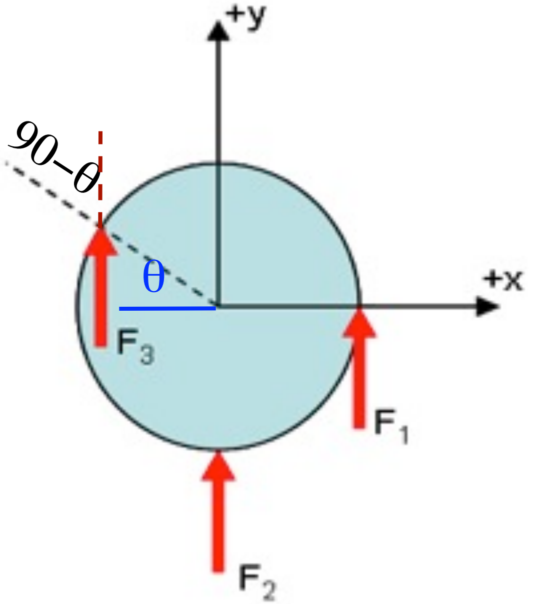
A) eh

B) F = mra. F1 = mra. However, F2 = 2mra. Therefore F2 = 2F1

C) I=mr^2 for F2. And r = 2 squared. That makes F= 4m*alpha.

- just kus

Torque On Disk



$$\tau = RF\sin\theta$$

A uniform disk with mass m = 8.96 kg and radius R = 1.35 m lies in the x-y plane and centered at the origin. Three forces act in the +y-direction on the disk: 1) a force 337 N at the edge of the disk on the +x-axis, 2) a force 337 N at the edge of the disk on the –y-axis, and 3) a force 337 N acts at the edge of the disk at an angle θ = 36° above the –x-axis.

1) What is the magnitude of the torque on the disk due to F_1?

N-m Submit

$$\theta = 90^0$$

2) What is the magnitude of the torque on the disk due to F_2?

N-m Submit

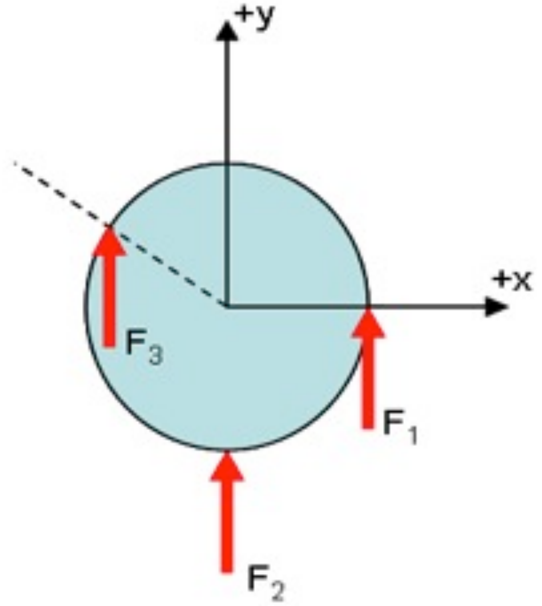
$$\theta = 0^0$$

3) What is the magnitude of the torque on the disk due to F_3?

N-m Submit

$$\theta = 90 - 36 = 54$$

Torque On Disk



$$\tau = RF\sin\theta$$

Direction is perpendicular to both *R* and *F*, given by the *right hand rule*

A uniform disk with mass m = 8.96 kg and radius R = 1.35 m lies in the x-y plane and centered at the origin. Three forces act in the +y-direction on the disk: 1) a force 337 N at the edge of the disk on the +x-axis, 2) a force 337 N at the edge of the disk on the –y-axis, and 3) a force 337 N acts at the edge of the disk at an angle θ = 36° above the –x-axis.

4) What is the x-component of the net torque on the disk?

N-m Submit

$$\tau_x = 0$$

5) What is the y-component of the net torque on the disk?

N-m Submit

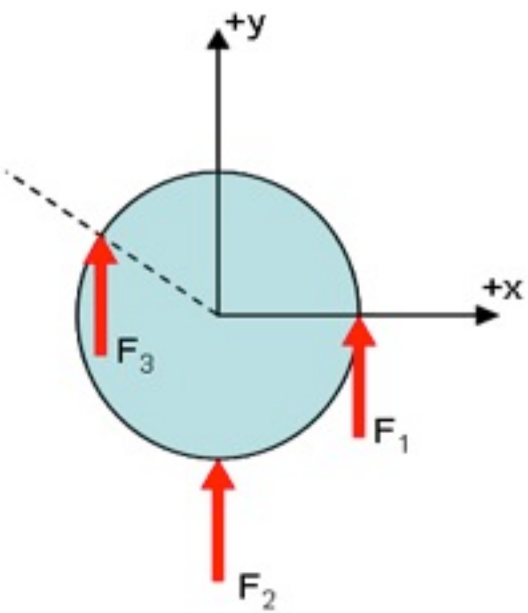
$$\tau_y = 0$$

6) What is the z-component of the net torque on the disk?

N-m Submit

$$\tau_z = \tau_{F_1} + \tau_{F_2} + \tau_{F_3}$$

Torque On Disk



(i) $$I_{DISK} = \frac{1}{2}MR^2$$

(ii) $$\tau = I\alpha$$

(iii) $$K = \frac{1}{2}I\omega^2$$

A uniform disk with mass m = 8.96 kg and radius R = 1.35 m lies in the x-y plane and centered at the origin. Three forces act in the +y-direction on the disk: 1) a force 337 N at the edge of the disk on the +x-axis, 2) a force 337 N at the edge of the disk on the –y-axis, and 3) a force 337 N acts at the edge of the disk at an angle θ = 36° above the –x-axis.

7) What is the magnitude of the angular acceleration of the disk?

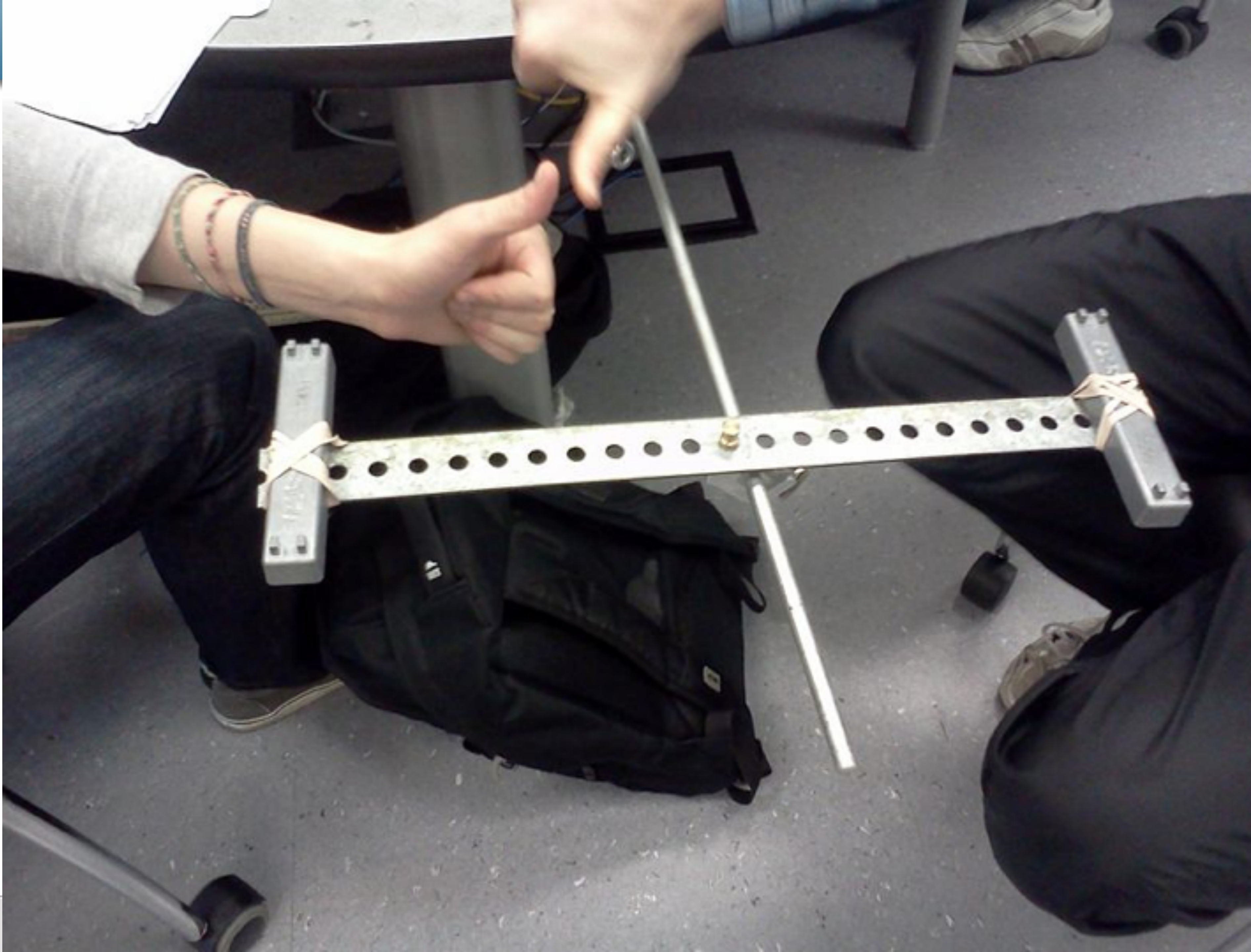
[ ] rad/s^2 Submit

Use (i) & (ii)

8) If the disk starts from rest, what is the rotational energy of the disk after the forces have been applied for t = 1.8 s?

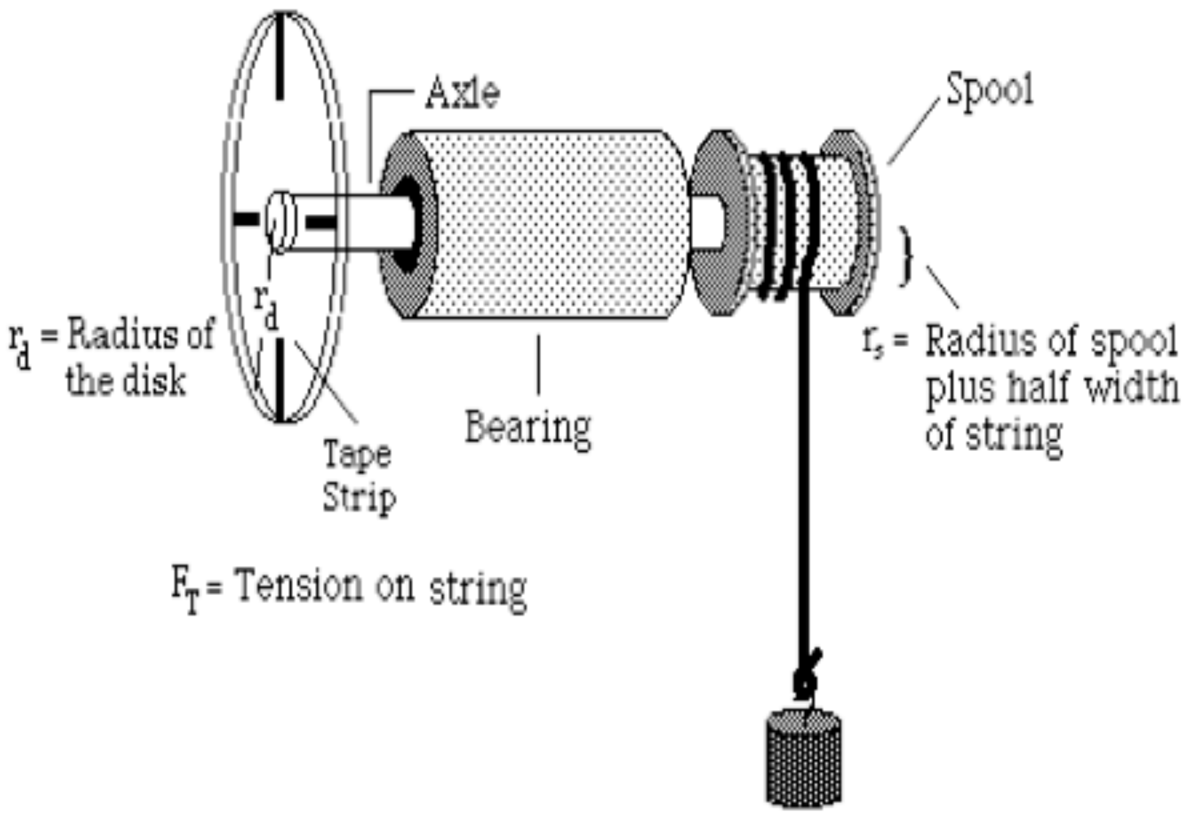
[ ] J Submit

Use (iii)



Must do before Next Time

SP12-4) (20 pts) A small spool of radius r_s and a large Lucite
axle that is free to rotate in an almost frictionless manner insi
gram below.



Deanna and the Machine

Analysis

Predicted a = 2.58 m/s/s