

Symmetries in gravity and LSS

Lam Hui
Columbia University

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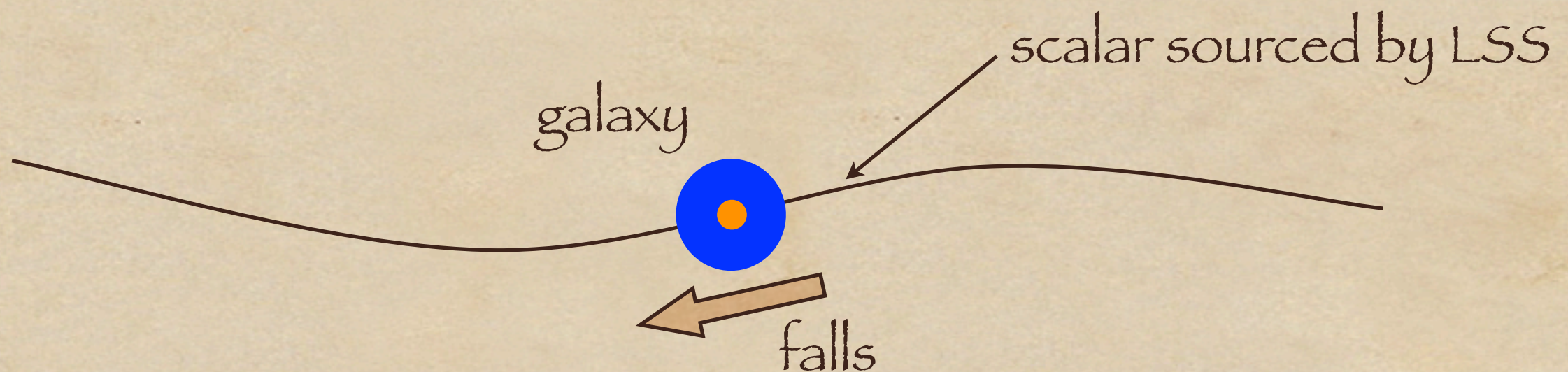
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Outline:

1. Equivalence principle: a generic test of modified gravity
- with Alberto Nicolás.
2. Parity in measurements of large scale structure (LSS)
- with Camille Bonvin & Enrique Gaztanaga.
3. Spontaneously broken symmetry in the theory of LSS
- with Kurt Hinterbichler & Justin Khoury;
Walter Goldberger & Alberto Nicolás;
Cremínnelli, Gleyzes, Simonovic & Vernizzi;
Bart Horn & Xiao Xiao.

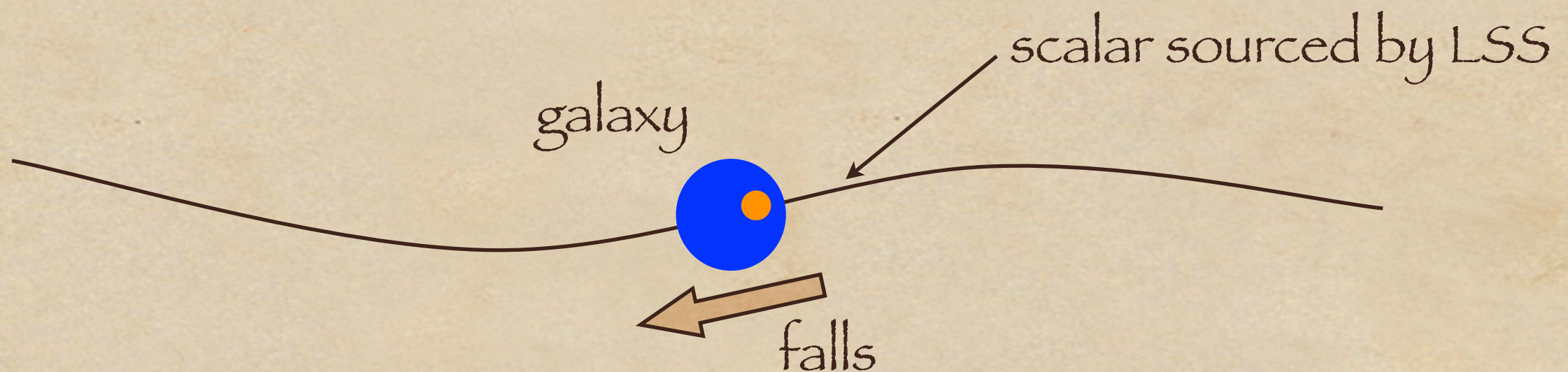
Idea 1: a generic test of scalar-tensor gravity

- Modifying gravity necessarily introduces new d.o.f. such as a scalar, i.e. a long range scalar force in addition to usual gravitational force (Weinberg/Deser thm.).
- Assume black holes have no scalar hair. More generally, compact objects have Q/M (scalar-charge/mass ratio) $\rightarrow 0$. Normal stars like the Sun have $Q/M \approx 1$. Thus, in the same environment a black hole and a star fall differently (Nordvedt).
- For Brans-Dicke, this is hopeless to see. Recent theories resurrect the idea.



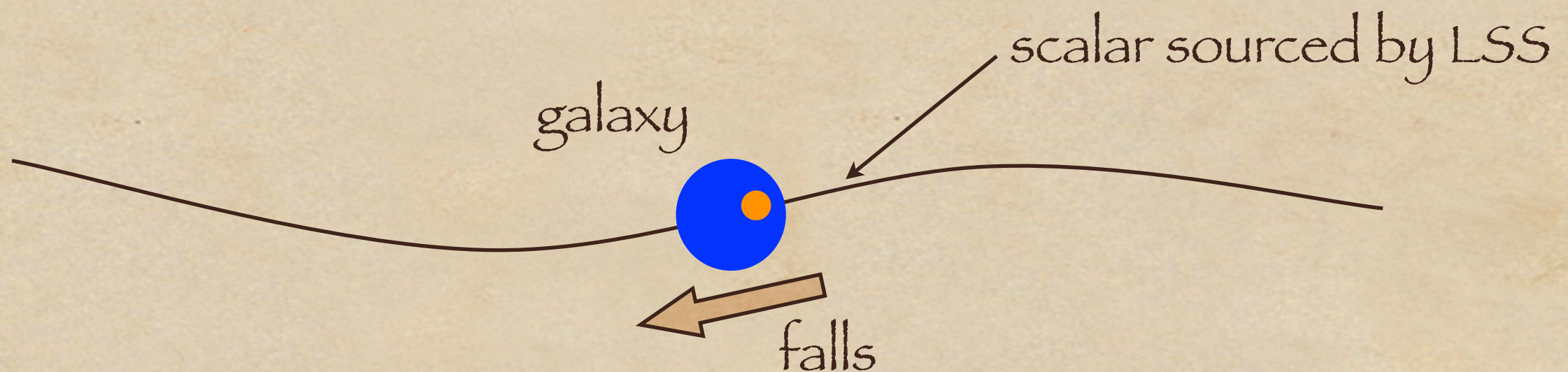
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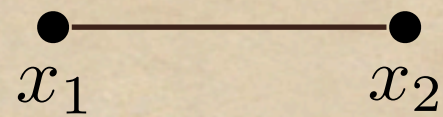
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- Black hole offset up to 100 pc (use local, small Seyfert galaxies).
Known offset: 7 pc for M87; Batcheldor et al. 2010 - beware astrophys. effects.

Idea 2: ~~parity~~ in the measurement of LSS

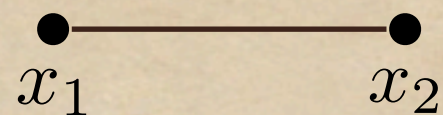
- It is generally assumed parity is respected in measurements of LSS, for good reason:



$$\langle \delta(x_1) \delta(x_2) \rangle$$

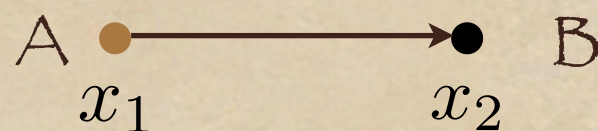
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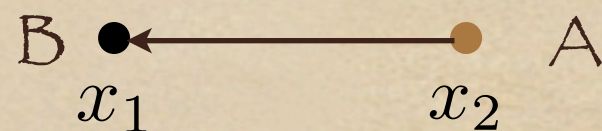
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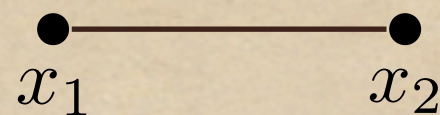
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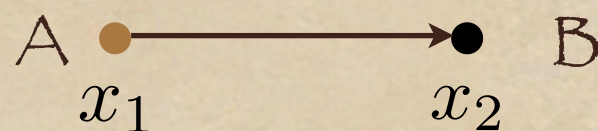
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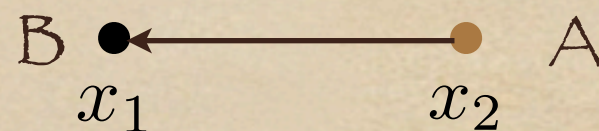
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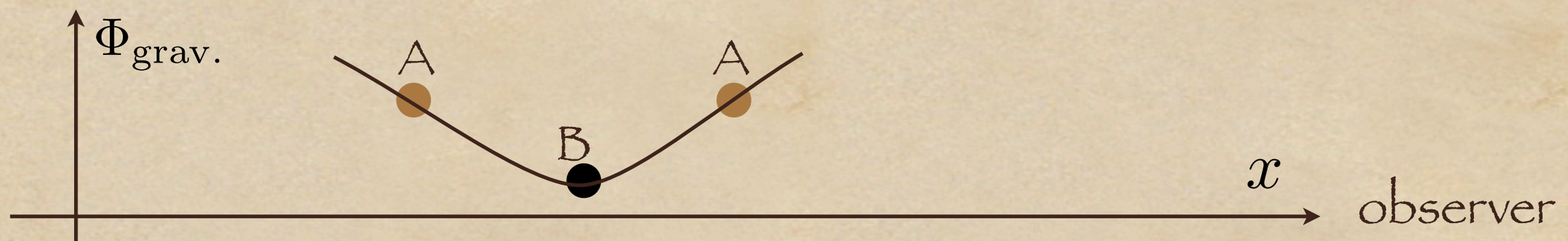
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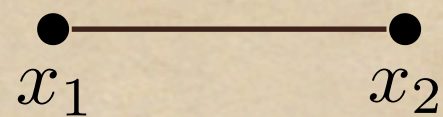
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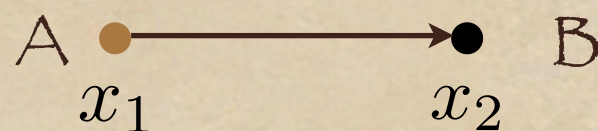
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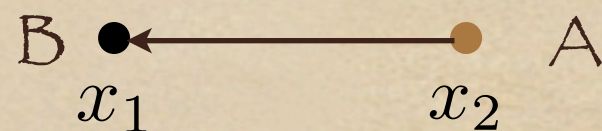
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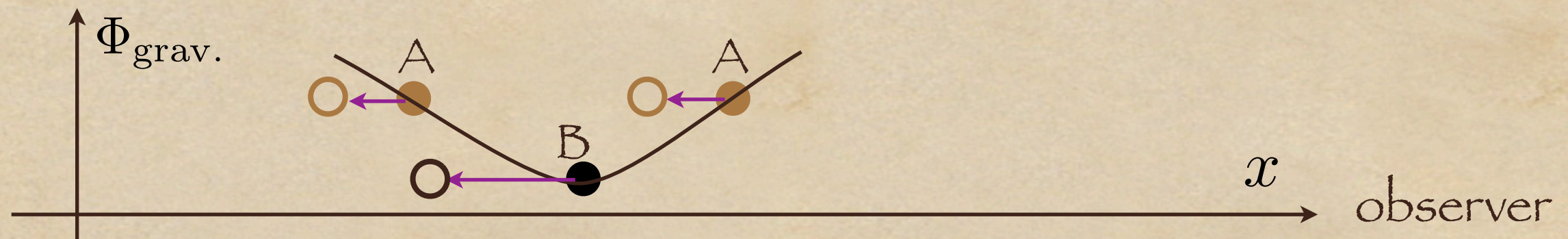
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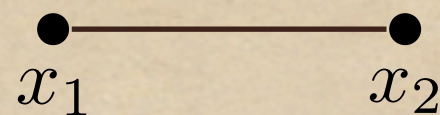
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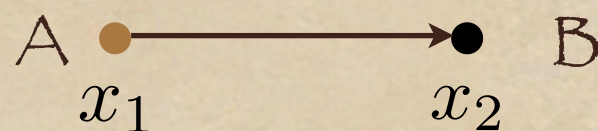
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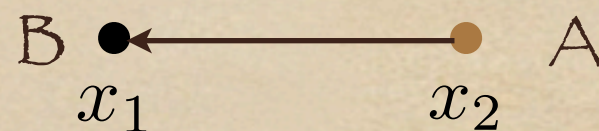
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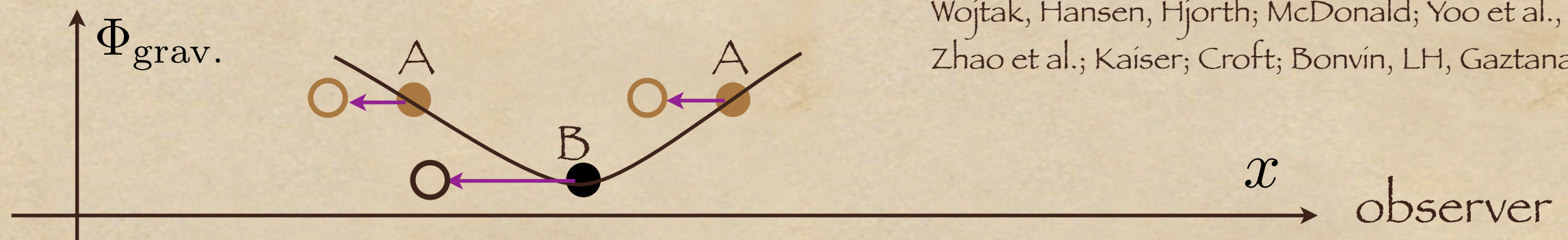
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- Consider the effect of gravitational redshift:



- Several additional (apparent) parity-violating effects. Possible to separate.

Idea 3: non-perturbative consistency relations in LSS

- 1. Consider a familiar example of symmetry: **spatial translation**.

$$x \rightarrow x + \Delta x, \quad \text{where } \Delta x = \text{const.}$$

Its consequence for correlation function is well known:

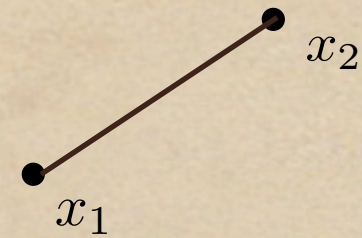
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For small Δx , we have:

$$\langle \phi(x_1 + \Delta x) \phi(x_2 + \Delta x) \phi(x_3 + \Delta x) \rangle \sim \langle \phi(x_1) \phi(x_2) \phi(x_3) \rangle + \Delta x \cdot \partial_1 \langle \phi(x_1) \phi(x_2) \phi(x_3) \rangle + \text{perm.}$$

Thus, alternatively, we say:

$$\langle \phi_1 \phi_2 \phi_3 \rangle \text{ is invariant under } \phi \rightarrow \phi + \Delta x \cdot \partial \phi \quad \text{i.e.} \quad \Delta x \cdot \partial_1 \langle \phi_1 \phi_2 \phi_3 \rangle + \text{perm.} = 0$$



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$$\phi \rightarrow \phi + c, \quad \text{where } c = \text{const.}$$

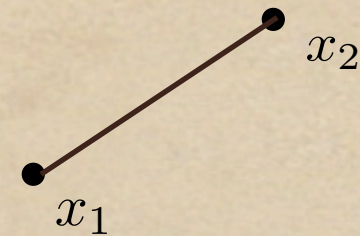
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Thus, saying $\langle \phi_1 \phi_2 \phi_3 \rangle = \langle (\phi_1 + c)(\phi_2 + c)(\phi_3 + c) \rangle$ is equiv. to saying:

$$c(\langle \phi_1 \phi_2 \rangle + \langle \phi_2 \phi_3 \rangle + \langle \phi_1 \phi_3 \rangle) = 0 \longleftarrow \text{clearly false!}$$

Conclude: $\langle \phi_1 \phi_2 \phi_3 \rangle$ is **not** invariant under $\phi \rightarrow \phi + c$



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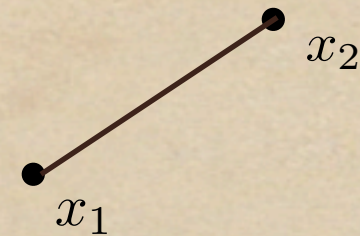
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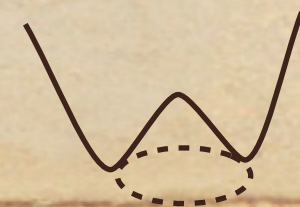
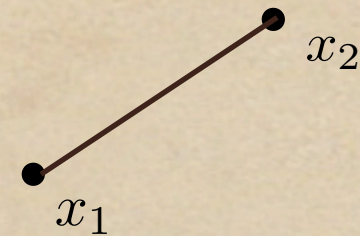
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- What makes the second case so different? We generally choose some expectation value for ϕ e.g. $\langle \phi \rangle = 0$. The choice breaks the shift symmetry i.e. spontaneous symm. breaking.

1. Unbroken symmetries \longrightarrow invariant correlation functions.

2. Spontaneously broken symmetries \longrightarrow consistency relations.

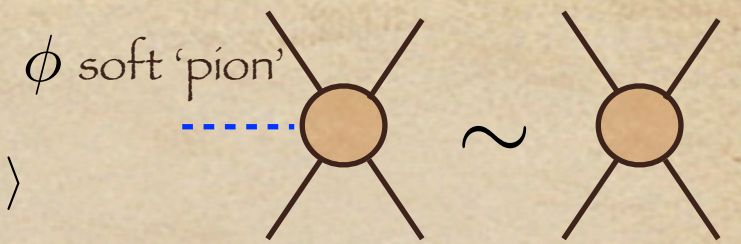


References:

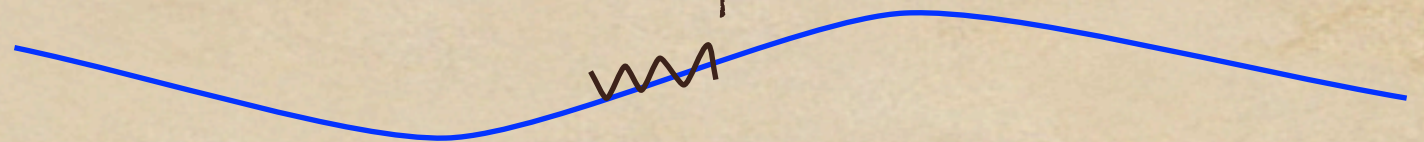
Maldacena; Creminelli & Zaldarriaga; Creminelli, Norena, Simonovic; Assassi, Baumann & Green; Flauger, Green & Porto; Pajer, Schmidt, Zaldarriaga; Kehagias & Riotto; Peloso & Pietronni; Berezhiani & Koury; Pimentel; Creminelli, Norena, Simonovic, Vernizzi; Goldberger, LH, Nicolis; Hinterbichler, LH, Koury; Horn, LH, Xiao.

Consistency relations from SSB

- Schematic form: $\lim_{q \rightarrow 0} \frac{1}{P_\phi(q)} \langle \phi(q) \mathcal{O}(k_1) \dots \mathcal{O}(k_N) \rangle \sim \langle \mathcal{O}(k_1) \dots \mathcal{O}(k_N) \rangle$

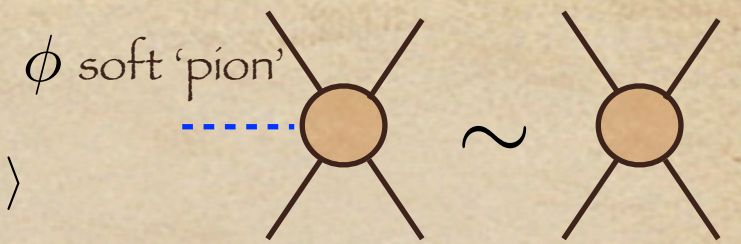


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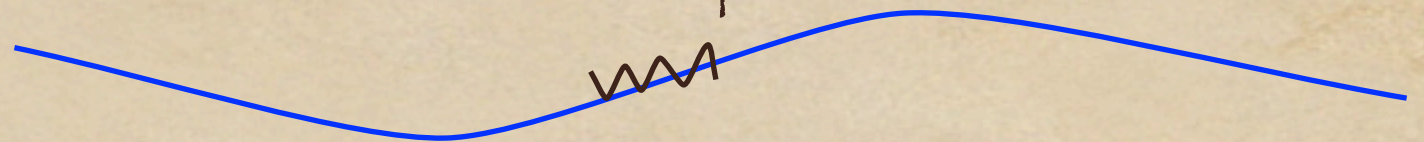
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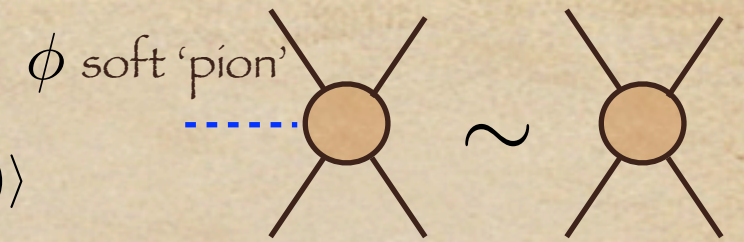
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 1. These are symmetry statements, and are therefore **exact, non-perturbative** i.e. they hold even if the observables \mathcal{O} are highly nonlinear, and even if they involve astrophysically complex objects, such as galaxies. The main input necessary is how they transform under the symmetry of interest (**robust** against galaxy mergers, birth, etc.)
 2. In the fully relativistic context, there is an **infinite** number of consistency relations. Two of them have interesting Newtonian limits (shift and time-dependent translation).
 3. Two assumptions go into these consistency relations, which can be experimentally tested (using highly nonlinear observables!): **Gaussian initial condition** (or more precisely, single-clock initial condition such as provided by inflation), and the **equivalence principle** (that all objects fall at the same rate under gravity). 10^{-4} constraint possible.
 4. Non-trivial constraints on analytic models.

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