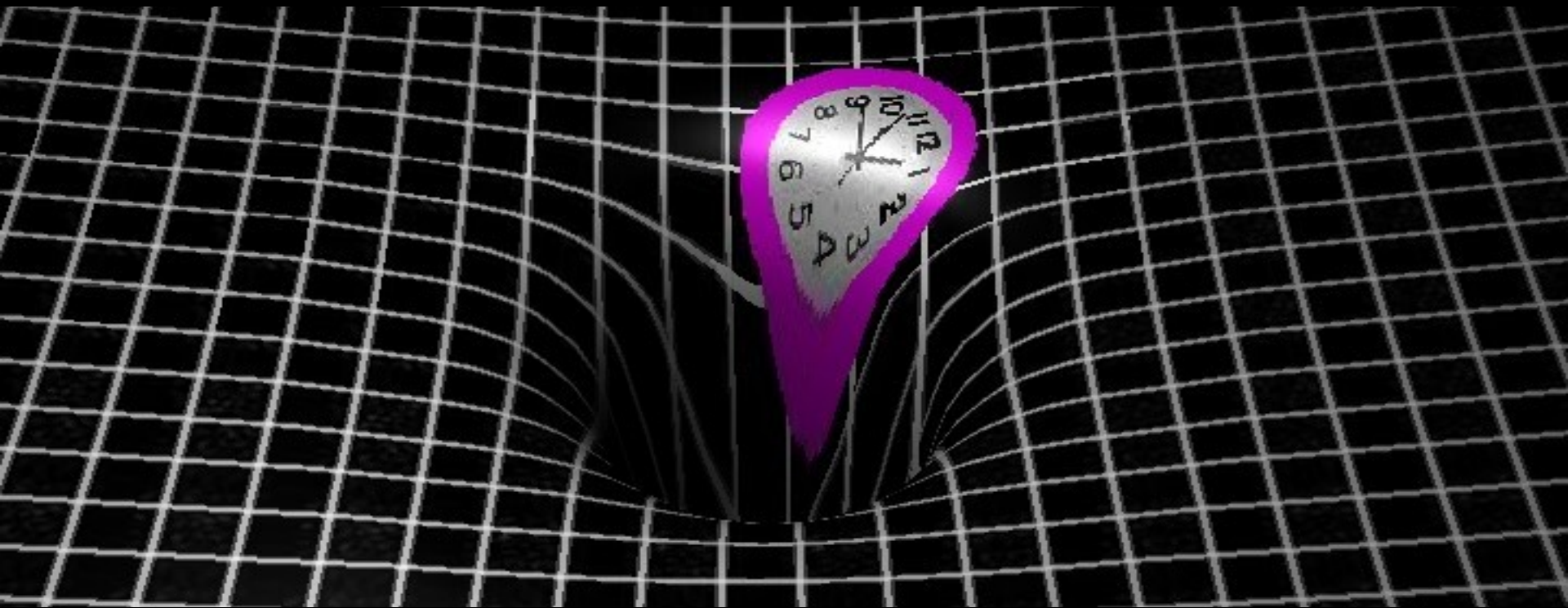


Searches for Local Lorentz Violation



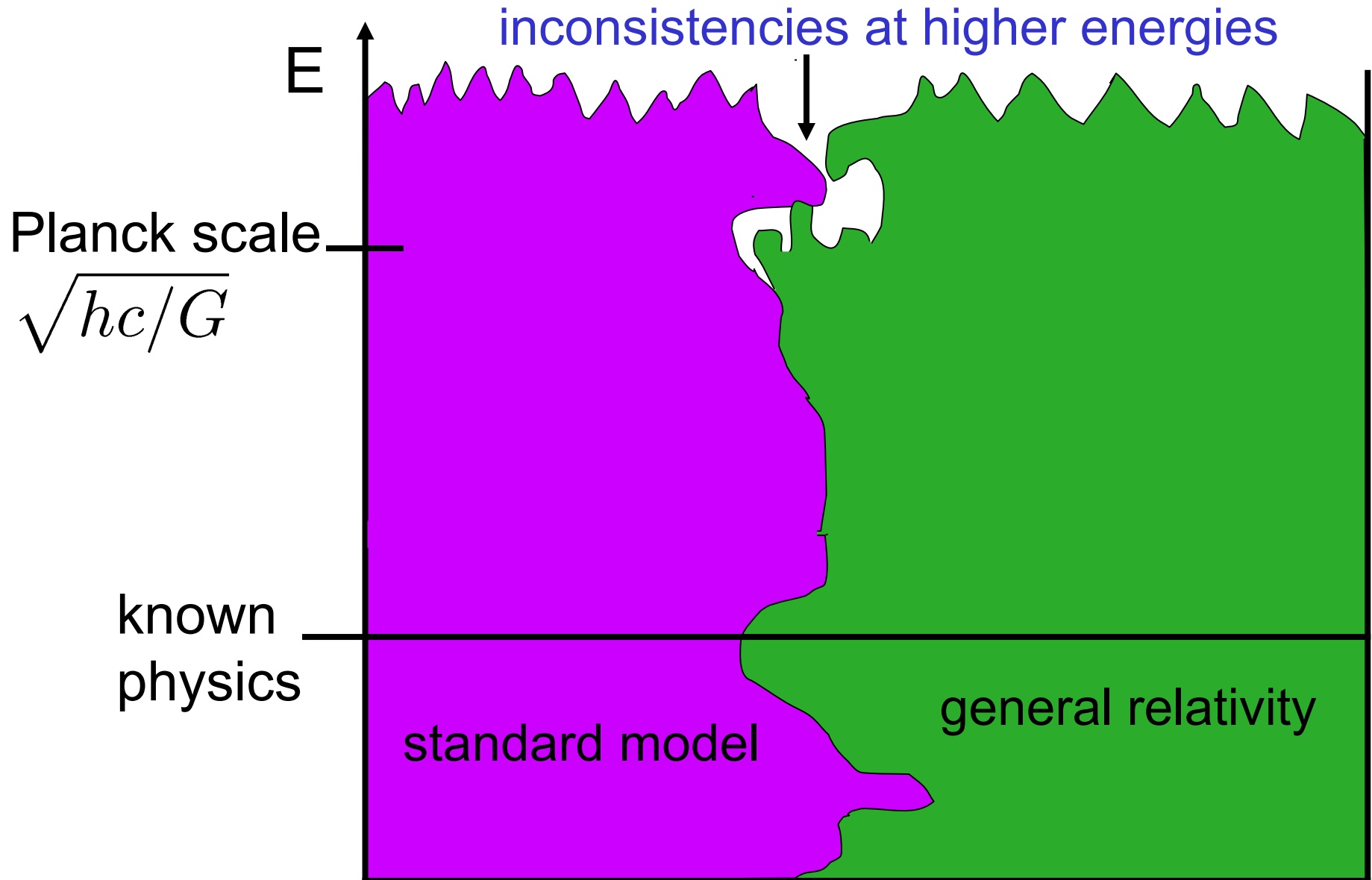
Jay D. Tasson

St. Olaf College

outline

- background
 - motivation
 - SME
- gravity theory
 - pure-gravity sector
 - matter-gravity couplings
- experiments & observations

motivation



underlying theory at Planck scale

options for probing experimentally

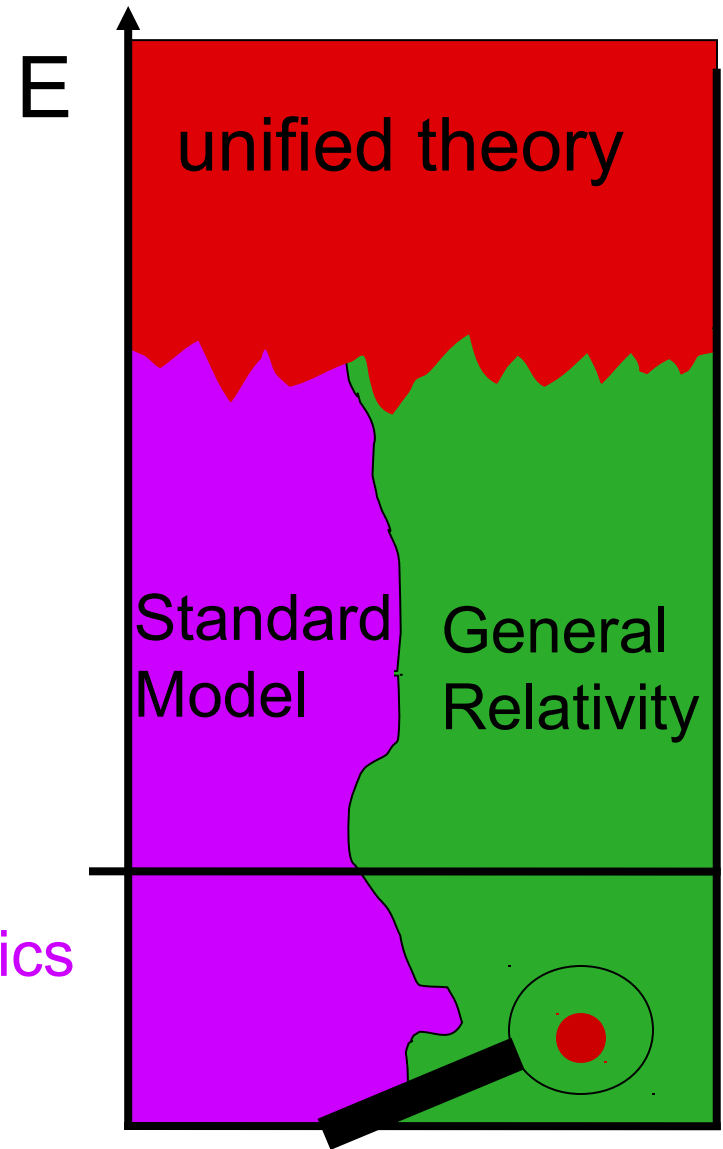
- galaxy-sized accelerator



- suppressed effects in sensitive experiments

local Lorentz violation

- can arise in theories of new physics
- difficult to mimic with conventional effects



Standard-Model Extension (SME)

test framework based on effective field theory which contains:

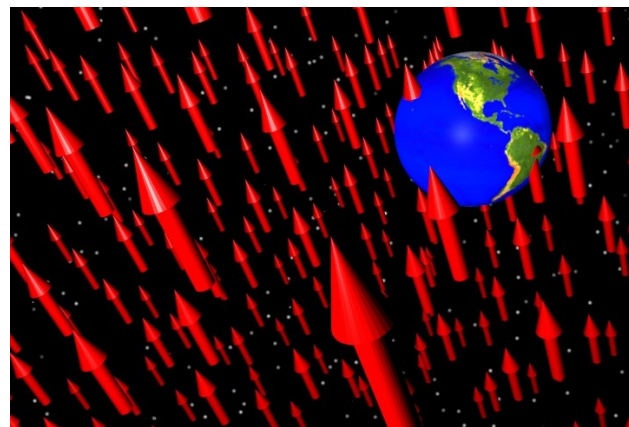
- General Relativity (GR)
- Standard Model (SM)
- arbitrary coordinate-independent Lorentz violation

$$L_{\text{SME}} = L_{\text{GR}} + L_{\text{SM}} + L_{\text{LV}}$$

Lorentz-violating terms

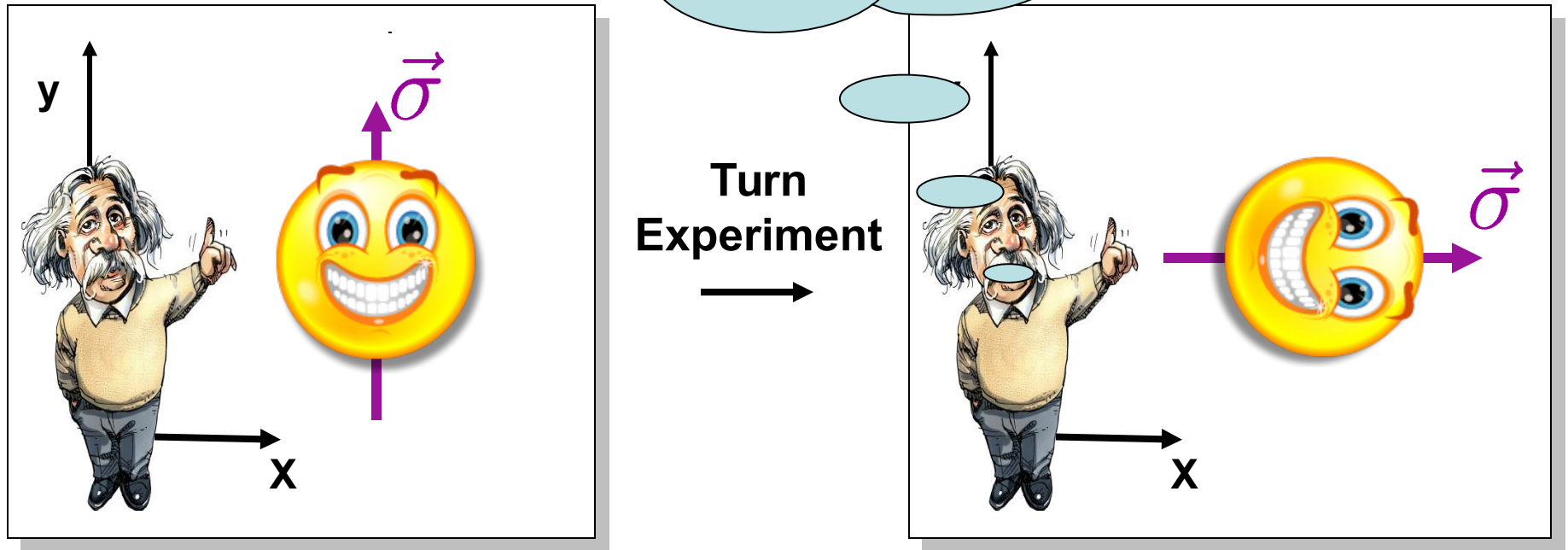
- constructed from GR and SM fields
- parameterized
by coefficients for Lorentz violation
- samples

$$s^{\mu\nu} R_{\mu\nu} \quad \bar{\psi} a_{\mu} \gamma^{\mu} \psi$$



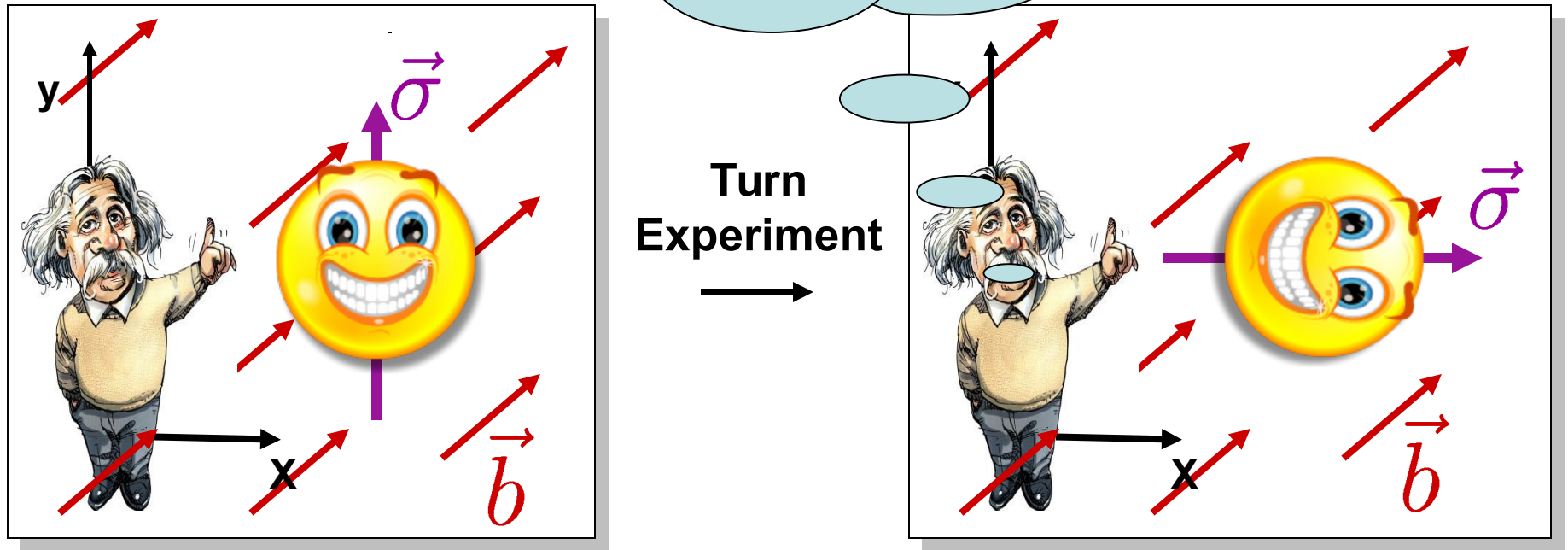
What is Lorentz (rotation) violation?

If I turn my head, it's clear that nothing has changed and relativity is preserved.



What is Lorentz (rotation) violation?

I can't fix this by rotating my coordinates. Relativity is violated



$$\vec{\tau} = \vec{\sigma} \times \vec{b}$$

Standard-Model Extension (SME)

test framework based on effective field theory which contains:

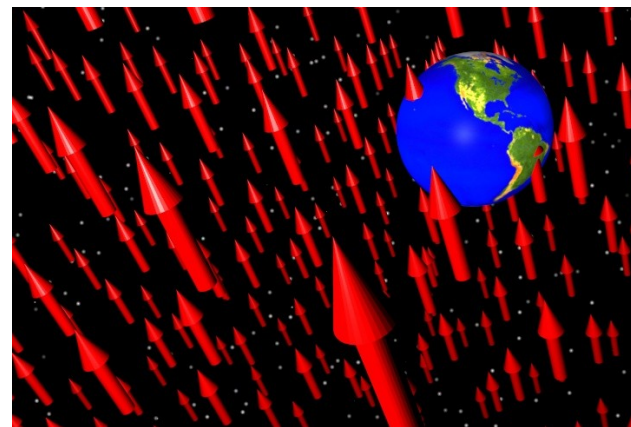
- General Relativity (GR)
- Standard Model (SM)
- arbitrary coordinate-independent Lorentz violation

$$L_{\text{SME}} = L_{\text{GR}} + L_{\text{SM}} + L_{\text{LV}}$$

Lorentz-violating terms

- constructed from GR and SM fields
- parameterized by coefficients for Lorentz violation
- sampled by experiments

$$S \supset R_{\mu\nu} \bar{\psi} a_{\mu} \gamma^{\mu} \psi$$



PPN vs. SME

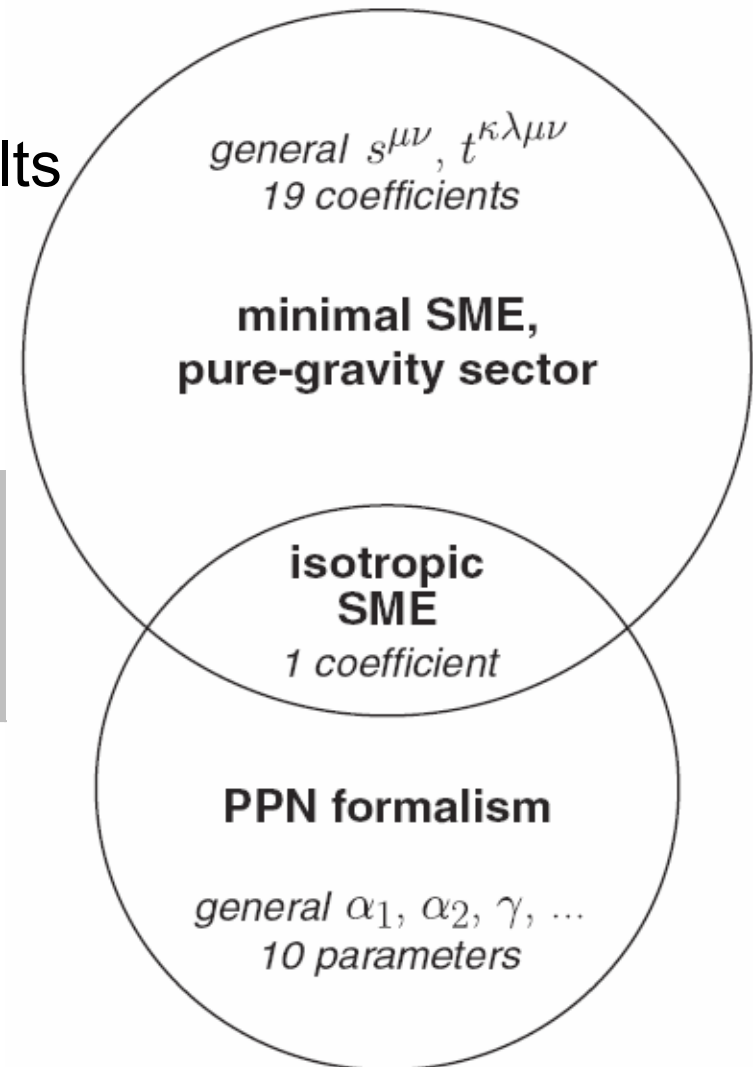
framework	PPN	SME
parameterizes deviations from:	General Relativity (including some LLV)	exact LLI (including some corrections to GR)
expansion about:	GR metric	GR + standard model lagrangian
GR corrections?	Yes	Yes, different ones!
matter sector /standard model corrections?	No	Yes
Lorentz invariant corrections?	Yes	(not primary interest)

parameterized deviations from GR are different!

Example: pure-gravity sector of minimal SME vs. PPN

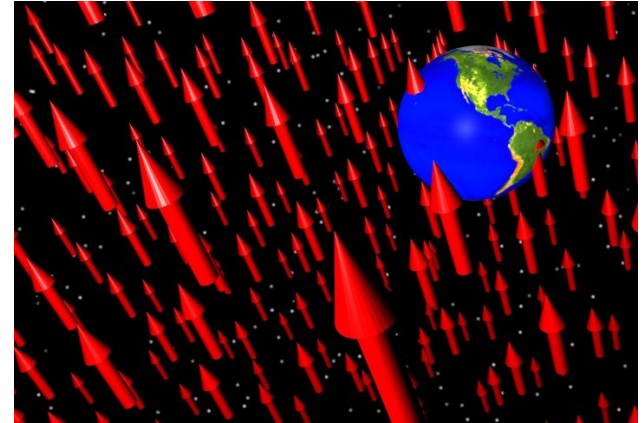
- different coefficients
- can lead to qualitatively different results

If you currently investigate the PPN, you may be able to test additional physics using the SME!



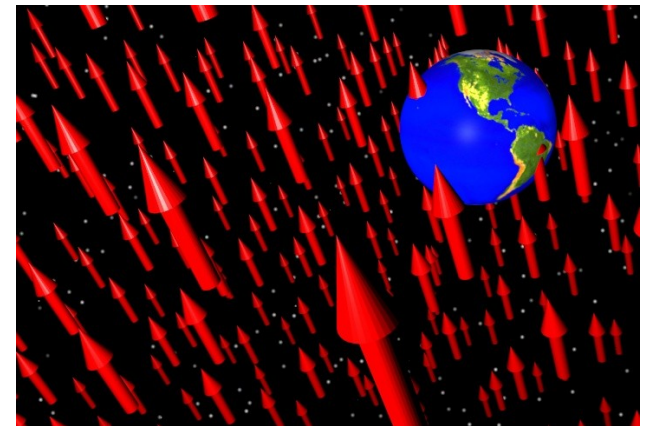
background vectors and tensors are cute, but where could they come from?

- explicit Lorentz violation
 - the universe just looks that way
 - consistency problems with Riemann geometry can arise¹
- spontaneous Lorentz violation
 - a vector or tensor field gets a vacuum-expectation value
 - nonzero VEV observed for a scalar particle, the Higgs (no Lorentz violation)
 - VEV for vector or tensor would be my red arrows
 - consistent with Riemann geometry



tests

- compare experiments pointing in different directions
- compare experiments at different velocities
- compare particles and antiparticles
- SME
 - predictive
 - quantitative comparisons
- observe:
 - Lorentz violation
 - ‘conventional’ field associated with larger-scale source eg. spacetime torsion¹, gravitomagnetism²



1 Kostelecký Russell JT PRL '08

2 JT PRD '12

SME experimental and observational searches

- atom-interferometer tests (Mueller, Chiow, Herrmann, Chu, Chung)
- lunar laser ranging (Battat, Chandler, Stubbs)
- pulsar-timing observations (Shao)
- short-range gravity tests (Speake, Long,...)
- trapped particle tests (Dehmelt, Gabrielse, ...)
- spin-polarized matter tests (Adelberger, Heckel, Hou, ...)
- clock-comparison tests (Gibble, Hunter, Romalis, Walsworth, ...)
- tests with resonant cavities (Lipa, Mueller, Peters, Schiller, Wolf, ...)
- neutrino oscillations (LSND, Minos, Super K, ...)
- muon tests (Hughes, BNL g-2)
- meson oscillations (BABAR, BELLE, DELPHI, FOCUS, KTeV, OPAL, ...)
- astrophysical photon decay
- cosmological birefringence
- CMB analysis
-

SME experimental and observational searches

- atom-
- lunar
- pulsar
- short-
- trapped
- spin-p
- clock-
- tests v
- neutrino
- muon
- meson
- astroph
- cosmological
- CMB anisotropy
-



Cornell University
Library

arXiv.org > hep-ph > arXiv:0801.0287

Search on

High Energy Physics - Phenomenology

Data Tables for Lorentz and CPT Violation

Alan Kostelecky, Neil Russell

(Submitted on 1 Jan 2008 (v1), last revised 23 Jan 2014 (this version, v7))

This work tabulates measured and derived values of coefficients for Lorentz and CPT violation in the Standard-Model Extension. Summary tables are extracted listing maximal attained sensitivities in the matter, photon, neutrino, and gravity sectors. Tables presenting definitions and properties are also compiled.

Comments: 67 pages, January 2014 edition

Subjects: **High Energy Physics - Phenomenology (hep-ph)**; Astrophysics (astro-ph); General Relativity and Quantum Cosmology (gr-qc); High Energy Physics - Experiment (hep-ex); High Energy Physics - Theory (hep-th)

Journal reference: Rev.Mod.Phys.83:11,2011

DOI: [10.1103/RevModPhys.83.11](https://doi.org/10.1103/RevModPhys.83.11)

Report number: IUHET 584, January 2014

Cite as: [arXiv:0801.0287](https://arxiv.org/abs/0801.0287) [hep-ph]

(or [arXiv:0801.0287v7](https://arxiv.org/abs/0801.0287v7) [hep-ph] for this version)

Chung)

...)

Volf, ...)

AL, ...)

SME experimental and observational searches

- atom-
- lunar
- pulsar
- short-
- trapped
- spin-p
- clock-
- tests v
- neutrino
- muon
- meson
- astroph
- cosmological
- CMB anisotropy
-

The screenshot shows the Cornell University Library's arXiv page for the paper 'Data Tables for Lorentz and CPT Violation'. The page header includes the Cornell University Library logo and the arXiv.org URL. The paper title is prominently displayed, followed by the authors' names. A blue box highlights the text 'Over 1000 experimental sensitivities' and 'Yet much remains unexplored'. The bottom section provides the journal reference, DOI, report number, and citation information.

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(or arXiv:0801.0287v7 [hep-ph] for this version)

Chung)

...)

Volf, ...)

AL, ...)

overview of Lorentz violation/SME

- Tasson, Rep. Prog. Phys. 77, 062901 (2014), arXiv:1403.7785

IOP Publishing

Reports on Progress in Physics

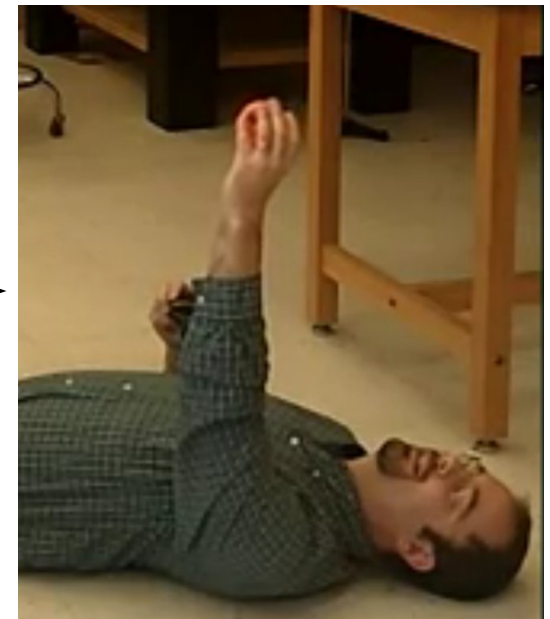
Rep. Prog. Phys. 77 (2014) 062901 (16pp)

doi:10.1088/0034-4885/77/6/062901

Key Issues Review

What do we know about Lorentz invariance?

- simple examples
- general overview
- video abstract



Lorentz violation in gravitational experiments

gravitational sector¹:

- Lorentz violation in the gravitational field
- Einstein-Hilbert + corrections

gravitationally coupled matter sector²:

- Lorentz violation in matter gravity couplings
- species dependent couplings leads to WEP violation

1 Bailey Kostelecký PRD '06, Bailey Kostelecký Xu arXiv:1410.6162

2 JT Kostelecký PRD '11

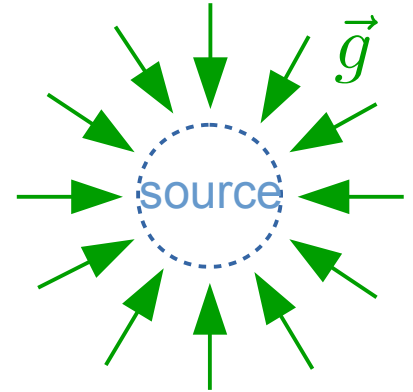
gravity sector

gravity sector: dynamics of gravitational field alone

$$\mathcal{L}_{\text{grav}} = \mathcal{L}_{\text{GR}} + \mathcal{L}_{\text{LV,grav}}$$

conventional
pure-gravity

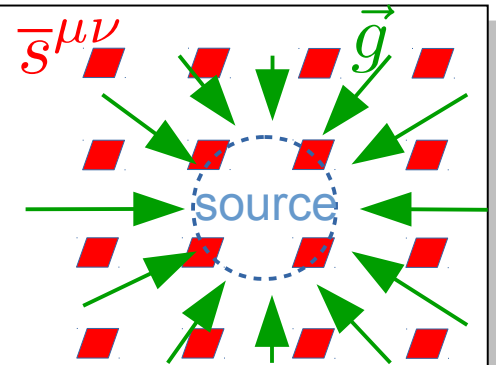
$$\mathcal{L}_{\text{GR}} = eR$$



leading Lorentz
violation

$$\mathcal{L}_{\text{LV,grav}} = e s^{\mu\nu} R_{\mu\nu} \dots$$

$$s^{\mu\nu} = \bar{s}^{\mu\nu} + \tilde{s}^{\mu\nu}$$



- minimal post-Newtonian effects originate from $\bar{s}^{\mu\nu}$
- experiments that involve the gravitational field are relevant

gravity sector

- minimal effects (mass dimension 4 operators) via post Newton metric¹

$$g_{00} = -1 + 2U + 3\bar{s}^{00}U + \bar{s}^{jk}U^{jk} + \dots$$

$$g_{0j} = \bar{s}^{0j}U - \frac{7}{2}V^j + \frac{3}{4}\bar{s}^{jk}V^k + \dots$$

...

- dimension 6 operators²

$$\mathcal{L}_{\text{LV,grav}}^{(6)} = \frac{1}{2}(\bar{k}_1^{(6)})_{\alpha\beta\gamma\delta\kappa\lambda}\{D^\kappa, D^\lambda\}R^{\alpha\beta\lambda\delta} + \dots$$

- dimension 6 effects via modified 1/r behavior

$$U(r) = G_N \int d^3r' \frac{\rho(\vec{r}')}{|\vec{r} - \vec{r}'|} \left(1 + \frac{\bar{k}(\hat{R})}{|\vec{r} - \vec{r}'|^2} \right)$$

anisotropic combination
of dim 6 coefficients

1 Bailey Kostelecký PRD '06

2 Bailey Kostelecký Xu arXiv:1410.6162

gravitationally coupled matter sector

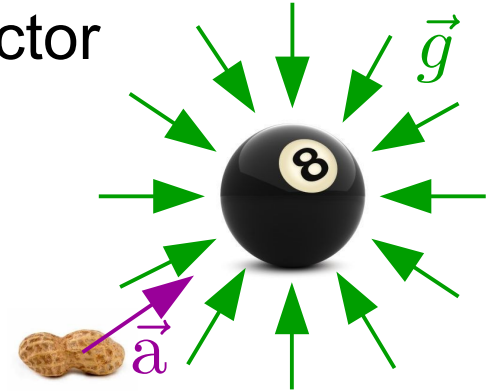
matter sector: kinematics and interactions of particles

$$\mathcal{L}_{\text{matter}} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{LV,SM}}$$

conventional gravitationally coupled matter sector

$$\mathcal{L}_{\text{SM}} = \frac{1}{2} i e^\mu_a \bar{\psi} \gamma^a \overleftrightarrow{D}_\mu \psi - \bar{\psi} m \psi$$

$$L_{\text{SM}} = -m \sqrt{-g_{\mu\nu} u^\mu u^\nu} \\ \approx \frac{1}{2} m \dot{x}^2 - U$$



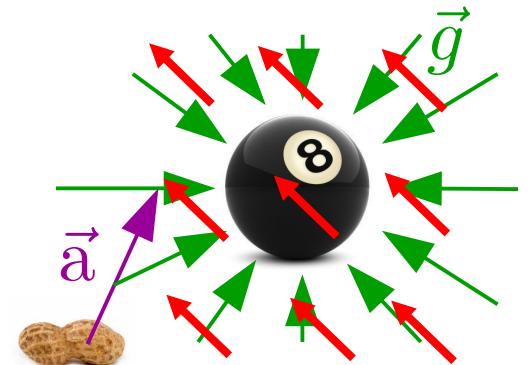
Lorentz violation

$$\mathcal{L}_{\text{LV,SM}} = -\frac{i}{2} e^\mu_a \bar{\psi} (c_{\nu\lambda} e^{\nu a} e^\lambda_b \gamma^b + e_\nu e^{\nu a} \dots) \overleftrightarrow{D}_\mu \psi - \bar{\psi} (a_\mu e^\mu_a \gamma^a \dots) \psi$$

$$L_{\text{LV,SM}} = -m \sqrt{-(g_{\mu\nu} u^\mu + 2c_{\mu\nu}) u^\nu + (a_{\text{eff}})_\mu u^\mu}$$

$$(a_{\text{eff}})_\mu = a_\mu - m e_\mu$$

- source-dependent field distortions
- test-particle dependent responses



countershaded Lorentz violation

- upon investigating spontaneous breaking we find

$$a_\mu = \bar{a}_\mu + \frac{1}{2}\alpha \bar{a}^\nu h_{\mu\nu} - \frac{1}{4}\alpha \bar{a}_\mu h^\nu{}_\nu$$

Minkowski-spacetime coefficients

unobservable shift in fermion phase

observable effects via gravity coupling

- $\bar{a}_\mu$ for matter is unobservable in flat-spacetime tests
- observable $\bar{a}_\mu$ effects are suppressed by the gravitational field
- $\bar{a}_\mu$ could be large ($\sim 1\text{eV}$) relative to existing matter-sector bounds $b_\mu < 10^{-30}$

classical results

$$h_{00} = \frac{2Gm}{r} \left(1 + (\bar{c}^S)_{00} + \frac{2}{m} (\bar{a}_{\text{eff}}^S)_0 \right) + \dots$$

$$\ddot{x}^j = -\frac{1}{2} \partial^j h_{00} + (\bar{c}^T)^j_k \partial^k h_{00} + \frac{1}{m^T} \alpha (\bar{a}_{\text{eff}}^T)_0 \partial^j h_{00} + \dots$$

S and T denote
composite coefficients
for source and test respectively


$$(a_{\text{eff}})_\mu = a_\mu - m e_\mu$$

- modified metric & particle equation of motion
- experimental hooks
 - particle-species dependence
 - time dependence

experiments

- Earth-source lab tests
 - gravimeter
Chung et al. PRD '09
Mueller et al. PRL '08
 - WEP
Hohensee Mueller Waringa PRL '13
Hohensee et al. PRL '11
- space-based WEP
- exotic tests
 - charged matter
 - antimatter
 - higher-generation matter
- solar-system tests
 - laser ranging
Battat Chandler Stubbs PRL '07
 - perihelion precession
- light-travel tests
 - time delay
 - Doppler shift
 - red shift
- clock tests
 - null redshift
 - comagnetometers
- short-range gravity
Long Kostelecký arXiv:1412.6362
Panjwani Carbone Speake in CPT'10
- gravity probe B
Bailey Everett Overduin PRD '13
- pulsar tests
Shao PRL '14
Shao arXiv:1412.2320

experiments

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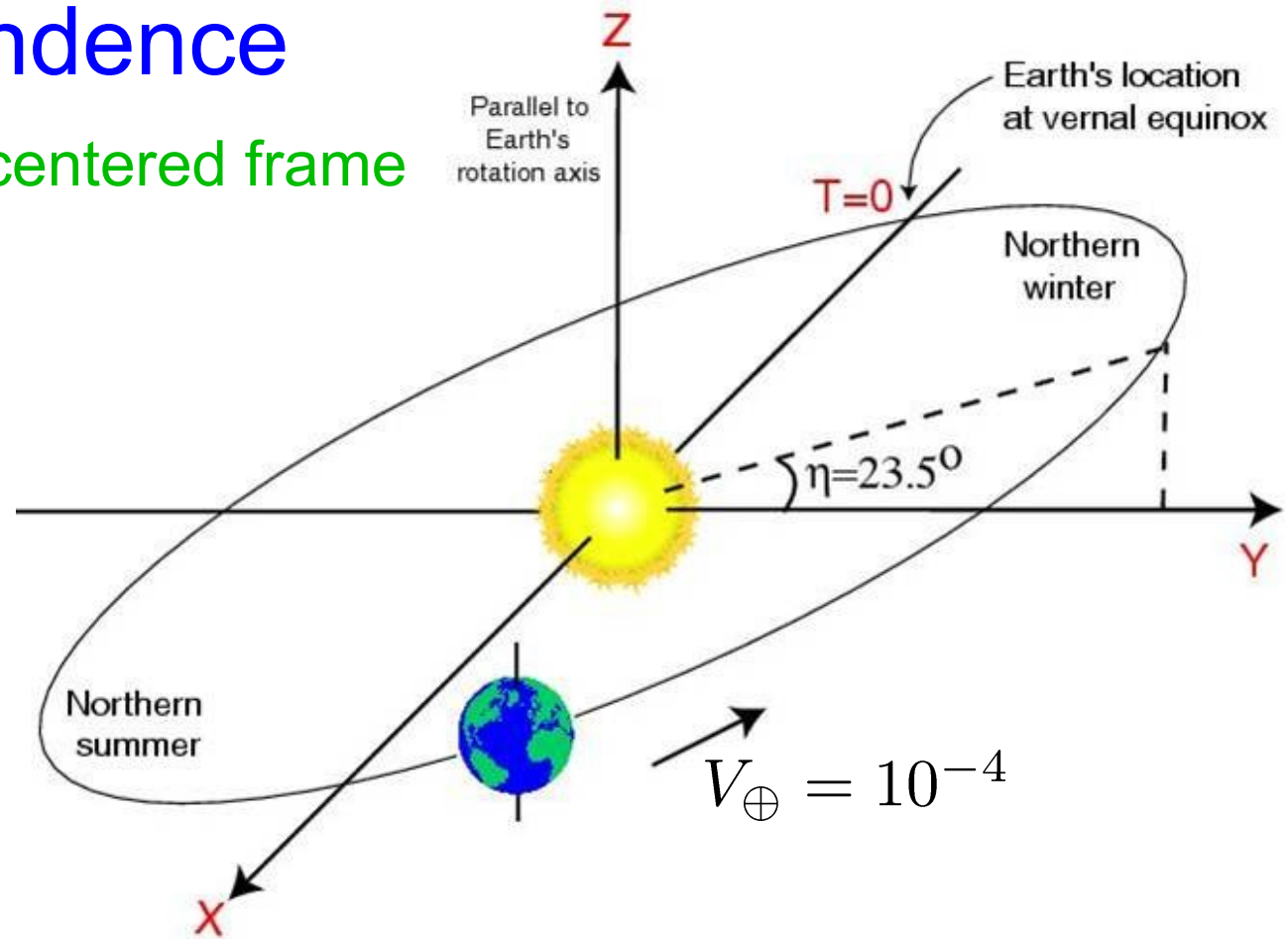
- pulsar tests

Shao PRL '14

Shao arXiv:1412.2320

time dependence

- standard Sun-centered frame



- boost and rotation of test $\longrightarrow$ annual & sidereal variations

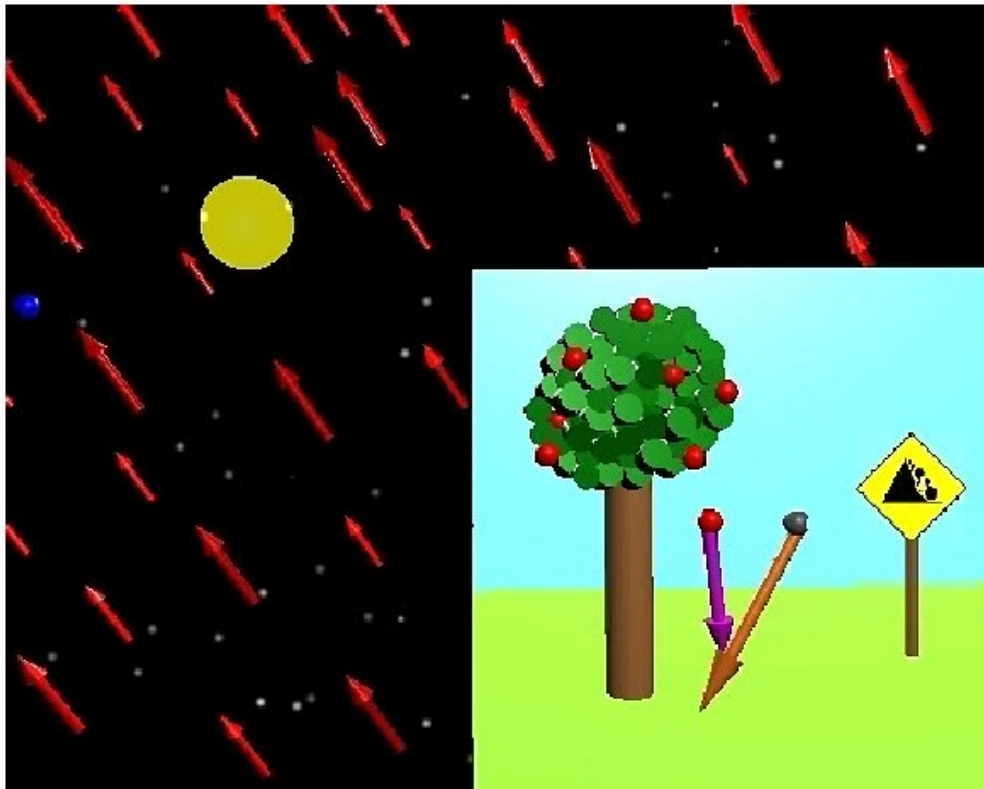
$$\ddot{\vec{x}} \supset -2g \alpha \bar{a}_T \hat{z} - 2g V_\oplus \alpha \bar{a}_X \sin(\Omega T) \hat{z} - \frac{2}{5} g V_L \alpha \bar{a}_X \sin(\omega T + \psi) \hat{y}$$

lab tests

acceleration of a test particle T

$$\ddot{\vec{x}} \supset -2\frac{1}{m}gV_{\oplus} \alpha(\bar{a}_{\text{eff}}^T)_X \sin(\Omega T) \hat{z} + gV_{\oplus}(\bar{c}^T)_{TX} \sin 2\chi \sin(\Omega T) \hat{x}$$

annual variations



- monitor acceleration of one particle over time → gravimeter
- monitor relative behavior of particles → EP test
- frequency and phase distinguish from other effects

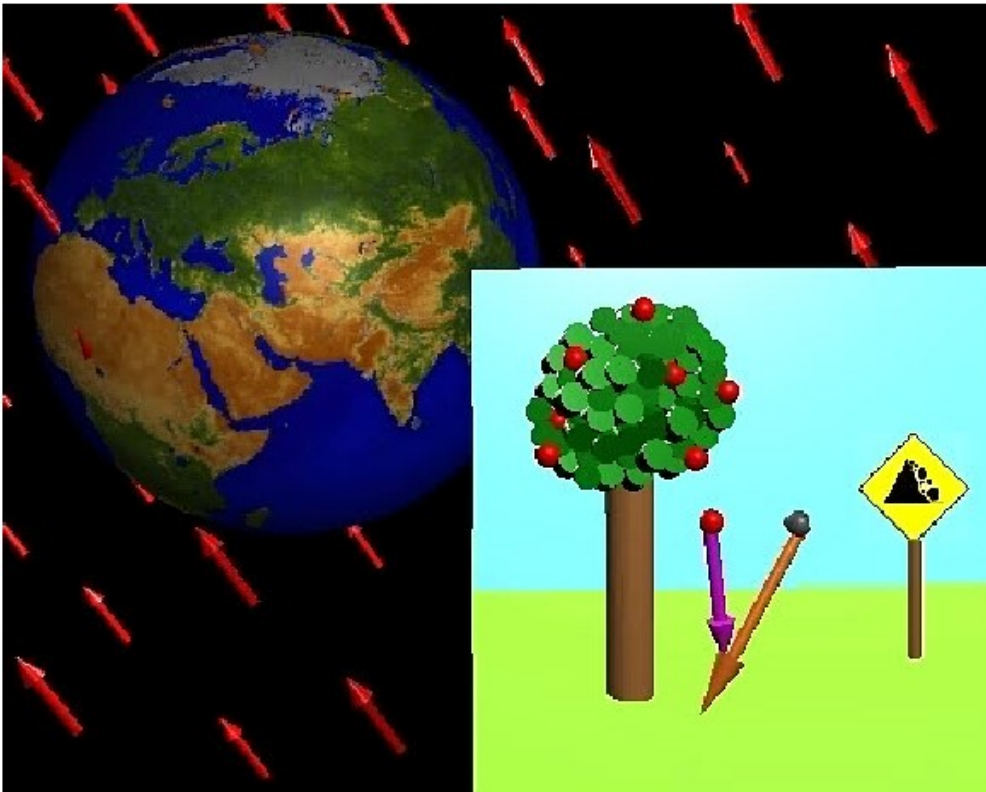
lab tests

acceleration of a test particle T

$$\ddot{\vec{x}} \supset -\frac{2}{5m} g V_L \alpha(\bar{a}_{\text{eff}}^T) x \sin(\omega T + \psi) \hat{y}$$

$$V_L \approx 10^{-2} V_{\oplus}$$

sidereal variations



unsuppressed in
some tests having
horizontal
sensitivity

B. Free-fall gravimeter tests

In this subsection, we consider laboratory tests that monitor the motion of a test body in free fall near the surface of the Earth. The equation of motion for the

B. Free-fall gravimeter tests

In
monit
surfa

$$\begin{aligned}
 a_{\hat{z}} = & -g + \omega^2 R_{\oplus} \sin^2 \chi \\
 & + \sum_{n,w} g \left[\left(\frac{N^w}{m^T} E_n^w + \frac{N_{\oplus}^w}{m^S} E_n'^w + \frac{1}{3} E_n \right) \cos(\omega_n T + \psi_n) \right. \\
 & \left. + \left(\frac{N^w}{m^T} F_n^w + \frac{N_{\oplus}^w}{m^S} F_n'^w + \frac{1}{3} F_n \right) \sin(\omega_n T + \psi_n) \right].
 \end{aligned}
 \tag{138}$$

B. Free-fall gravimeter tests

In
moni
surfa

$$a_{\hat{z}} = -g + \omega^2 R_{\oplus} \sin^2 \chi + \sum_{n,w} g \left[\left(\frac{N^w}{m^T} E_n^w + \frac{N_{\oplus}^w}{m^S} E_n'^w + \frac{1}{3} E_n \right) \cos(\omega_n T + \psi_n) \right]$$

Table IV. Amplitudes for the acceleration $a_{\hat{z}}$.

Amplitude	Phase
$E_0^w = -2\alpha(\bar{a}_{\text{eff}}^w)_T + 2m^w(\bar{c}^w)_{ZZ} \cos^2 \chi + m^w((\bar{c}^w)_{XX} + (\bar{c}^w)_{YY}) \sin^2 \chi$	0
$E_0'^w = -2\alpha(\bar{a}_{\text{eff}}^w)_T - m^w(\bar{c}^w)_{TT}$	0
$E_{\omega}^w = 2m^w(\bar{c}^w)_{(XZ)} \sin 2\chi - \frac{4}{5}V_L \alpha(\bar{a}_{\text{eff}}^w)_Y \sin \chi$	ψ
$E_{\omega}'^w = -\frac{4}{5}V_L (3\alpha(\bar{a}_{\text{eff}}^w)_Y + m^w(\bar{c}^w)_{(TY)}) \sin \chi$	ψ
$F_{\omega}^w = 2m^w(\bar{c}^w)_{(YZ)} \sin 2\chi + \frac{4}{5}V_L \alpha(\bar{a}_{\text{eff}}^w)_X \sin \chi$	ψ
$F_{\omega}'^w = \frac{4}{5}V_L (3\alpha(\bar{a}_{\text{eff}}^w)_X + m^w(\bar{c}^w)_{(TX)}) \sin \chi$	ψ

B. Free-fall gravimeter tests

In
monitored
surface

$$a_{\hat{z}} = -g + \omega^2 R_{\oplus} \sin^2 \chi + \sum_{n,w} g \left[\left(\frac{N^w}{m^T} E_n^w + \frac{N_{\oplus}^w}{m^S} E_n'^w + \frac{1}{3} E_n \right) \cos(\omega_n T + \psi_n) \right]$$

Table IV. Amplitudes for the acceleration $a_{\hat{z}}$.

Amplitude	Phase
-----------	-------

$$E_n^w = -2\alpha(\bar{a}_{\text{eff}}^w)_X + 2m^w(\bar{c}^w)_{(TX)} \cos^2 \chi$$

improvement potential via atom interferometry:

- max reach 4 to 6 orders of magnitude improvement
- special linear combinations 10 orders of magnitude improvement

Dimopoulos et al. PRD 2008

$$F_{\omega}^{'w} = \frac{4}{5} V_L \left(3\alpha(\bar{a}_{\text{eff}}^w)_X + m^w(\bar{c}^w)_{(TX)} \right) \sin \chi \quad \psi$$

D. Free-fall WEP tests

E. Force-comparison WEP tests

In this
signals for
the relat

Typical force-comparison WEP tests can be viewed as comparing the motion of two or more bodies joined through electromagnetic forces with that predicted by

signals are qualitatively distinct from other sources of WEP violation due to characteristic periodicity

improvement potential:

- max reach 4 to 6 orders
- special combinations 10 orders

WEP tests considered

atom interferometry

torsion pendulum

drop tower

balloon drop

tossed masses

...and any WEP test can be used

experiments

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 - gravimeter
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Long Kostelecký arXiv:1412.6362
Panjwani Carbone Speake in CPT'10
- gravity probe B
Bailey Everett Overduin PRD '13
- pulsar tests
Shao PRL '14
Shao arXiv:1412.2320

exotic tests

- variations of above tests involving experimentally challenging matter
- charged matter
 - separate proton and electron coefficients
 - theoretically interesting -- bumblebee electrodynamics

improvement potential:

sensitivity to remaining 4 unconstrained $(\bar{a}_{\text{eff}})_{\mu}$ coefficients

- higher-generation matter

improvement potential:

first sensitivity to $(\bar{a}_{\text{eff}})_{\mu}$ for muons, for example

- antimatter
 - separate CPT even and odd coefficients
 - differing gravitational response for matter and antimatter

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Long Kostelecký arXiv:1412.6362
Panjwani Carbone Speake in CPT'10
- gravity probe B
Bailey Everett Overduin PRD '13
- pulsar tests
Shao PRL '14
Shao arXiv:1412.2320

short range

$$U(r) = G_N \int d^3 r' \frac{\rho(\vec{r}')}{|\vec{r} - \vec{r}'|} \left(1 + \frac{\bar{k}(\hat{R})}{|\vec{r} - \vec{r}'|^2} \right)$$

anisotropic combination
of dim 6 coefficients

Time & orientation dependence $\Rightarrow$

- qualitatively different from other $1/r$ deviations
- sensitivities require data analysis
- crude estimate of reach for given experiment

$$U_{\text{Yukawa}} = G_N M (1 + \alpha e^{-r/\lambda})/r \Rightarrow |\bar{k}(\hat{r}, T)| \approx \alpha \lambda^2 / e$$

improvement:

- first dimension 6 sensitivities via Indiana cantilever experiment
 10^{-9} m^2 Long Kostelecký arXiv:1412:6362
- additional experiments offer improved sensitivity & additional coefficients

experiments

- Earth-source lab tests
 - gravimeter
Chung et al. PRD '09
Mueller et al. PRL '08
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- short-range gravity
Long Kostelecký arXiv:1412.6362
Panjwani Carbone Speake in CPT'10
- gravity probe B
Bailey Everett Overduin PRD '13
- **pulsar tests**
Shao PRL '14
Shao arXiv:1412.2320

pulsars

- minimal gravity sector implies $\overline{s}^{\mu\nu}$ effects on orbits and timing¹
- constraints on $\overline{s}^{\mu\nu}$ coefficients achieved using observations of²:
B1937+21, J1744-1134, B1913+16, B1534+12, J0737-3039A, B2127+11C,
J1738+0333, J1012+5307, J0348+0432, J1802-2124, J0437-4715, B1855+09,
J1909-3744
- “The null detection of any beyond-GR effects in binary pulsars constrains LV orbital dynamics.”

improvement:

- first consideration of strong gravity
- several orders of magnitude improvement
- further improvement via direct fit to SME, observation improvements, & additional SME phenomenology

Summary

- Lorentz violation searches have potential to detect Planck-scale physics with existing technology
- The SME provides a field-theory based test framework
- Lorentz violation introduces qualitatively new signals in experiments
- Much work has been done but much remains unexplored