# **Influence of Reaction Conditions on the Synthesis of** Self-Cross-Linked N-Isopropylacrylamide Microgels

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We report systematic investigations of the reaction conditions necessary for the production of selfcross-linked poly(N-isopropylacrylamide) (PNIPAM) microgel particles. Reaction temperatures ( $T_{\text{syn}}$ ) ranging from 40 to 90  $^{\circ}$ C and various monomer ( $C_{\text{NIPAM}}$ ) and initiator ( $C_{\text{KPS}}$ ) concentrations were investigated. Laser light scattering was used to characterize the resultant gel particles at 25 and 40 °C, below and above the phase transition temperature of PNIPAM. By comparing the molar masses measured at these two temperatures, well-defined ranges of  $T_{\text{syn}}$ ,  $C_{\text{NIPAM}}$ , and  $C_{\text{KPS}}$  were found in which the polymer chains were well self-cross-linked and formed gel networks. Variations in the size and solid density as a function of these parameters are also discussed.

#### Introduction

Since the first synthesis of poly(N-isopropylacrylamide)(PNIPAM) microgels in 1986, these particles have become by far the most widely investigated water-based, temperature-sensitive microgels. <sup>2,3</sup> PNIPAM-based microgels are temperature-sensitive because PNIPAM undergoes a volume phase transition at a lower critical solution temperature (LCST) of around 33 °C.4 There is a growing interest in these materials because of potential applications as building blocks for more complicated structures, 5-7 as temperature-sensitive vessels,8 and in permeable membranes9 for controlled drug release.

The standard technique used to form PNIPAM microgels<sup>1,10</sup> is precipitation polymerization. A solution consisting of the N-isopropylacrylamide (NIPAM) monomer and cross-linker is heated to temperatures well above the LCST of PNIPAM, and an initiator is introduced. Because the growing PNIPAM chains are very hydrophobic at these temperatures, they collapse into nano-aggregates mainly stabilized by charged groups originating from an ionic initiator or added ionic surfactant. In most cases of PNIPAM microgel synthesis, a monomer containing two vinyl groups, N,N-methylenebisacrylamide (BIS), is used to cross-link the polymer chains into polymer networks. However, the use of a chemical cross-linker can lead to structural inhomogeneities<sup>11–13</sup> if the reaction rate of the cross-linker is different from that of the monomer, as is known for BIS.14

We recently observed the formation of PNIPAM microgel particles during synthesis under reaction conditions that were normal except for the absence of an added crosslinker. We showed that NIPAM can self-cross-link into microgel particles through tert carbon atoms both during and after the polymerization of the NIPAM monomers. 15 These stable microgels, with radii of several hundred nanometers, molar masses as high as 109 g/mol, and solid densities as low as 0.013 g/cm<sup>3</sup> at 25 °C in water, resemble normal BIS-cross-linked PNIPAM microgels in every aspect, including the formation of a colloidal crystalline structure at suitable volume fractions. The kinetics of selfcross-linking and exclusion of pure hyperbranching as a source of formation of PNIPAM particles were also presented in our previous paper. 15

In this work, we describe the systematic synthesis of PNIPAM microgels without the use of an added crosslinker carried out under different reaction conditions. By using laser light scattering to characterize the sizes and molar masses of the resultant gel nanoparticles, suitable conditions were found for effective self-cross-linking. In general, the aggregates have to reach a sufficiently high solid density to ensure that interchain cross-linking can occur. The extent of intrinsic self-cross-linking was also estimated by comparing the density of these particles with that of particles made with an added cross-linker. These studies of the influence of the reaction temperature and initial monomer and initiator concentrations on the resultant particle sizes, molar masses, and densities also provide insight into BIS-cross-linked NIPAM microgel synthesis.

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#### **Materials and Method**

Synthesis of Gel Nanospheres. NIPAM from Acros Organics (Geel, Belgium) was recrystallized from hexane/acetone solutions. BIS and potassium persulfate (KPS) from Aldrich were used as

<sup>(1)</sup> Pelton, R. H.; Chibante, P. Colloids Surf. 1986, 20, 247.

<sup>(2)</sup> Saunders, B. R.; Vincent, B. Adv. Colloid Interface Sci. 1999, 80,

<sup>(3)</sup> Pelton, R. H. Adv. Colloid Interface Sci. 2000, 85, 1. (4) Hirokawa, Y.; Tanaka, T. J. Chem. Phys. 1984, 81, 6379.

<sup>(4)</sup> Hirokawa, Y.; Tanaka, T. J. Chem. Phys. 1984, 81, 6379.
(5) Hu, Z.; Lu, X.; Gao, J.; Wang, C. Adv. Mater. 2000, 12, 1173. Hu,
Z.; Lu, X.; Gao, J. Adv. Mater. 2001, 13, 1708.
(6) Jones, C. D.; Lyon, L. A. Macromolecules 2000, 33, 8301.
(7) Zha, L.; Zhang, Y.; Yang, W.; Fu, S. Adv. Mater. 2002, 14, 1090.
(8) Leobandung, W.; Ichikawa, H.; Fukumori, Y.; Peppas, N. A. J. Controlled Release 2002, 80, 357.
(9) Zhang, K.; Wu, X. Y. J. Controlled Release 2002, 80, 169.
(10) McPhee, W.; Tam, K. C.; Pelton, R. H. J. Colloid Interface Sci.
1003, 156, 24

**<sup>1993</sup>**. 156, 24.

<sup>(11)</sup> Norisuye, T.; Masui, N.; Kida, Y.; Ikuta, D.; Kokufuta, E.; Ito,

S.; Panyukov, S.; Shibayama, M. *Polymer* **2002**, *43*, 5289. (12) Guillermo, A.; Cohen Addad, J. P.; Bazile, J. P.; Duracher, D.; Elaissari, A.; Pichot, C. J. Polym. Sci., Part B: Polym. Phys. 2000, 38,

<sup>(13)</sup> Fernandez-Barbero, A.; Fernandez-Nieves, A.; Grillo, I.; Lopez-

Cabarcos, E. *Phys. Rev. E* **2002**, *66*, 051803.
(14) Wu, X.; Pelton, R. H.; Hamielec, A. E.; Woods, D. H.; McPhee, W. *Colloid Polym. Sci.* **1994**, *272*, 467.

<sup>(15)</sup> Gao, J.; Frisken, B. J. Langmuir 2003, 19, 5212.

Table 1. Recipes for the Synthesis of Self-Cross-Linked **NIPAM Gel Microspheres in Water** 

	synthesis		concentration (in 100 g of solution)		
batch no.	T (°C)	(h)	$W_{\text{NIPAM}} + W_{\text{BIS}}$ (g)	KPS (mg)	n <sub>BIS</sub> /n <sub>NIPAM</sub> (%)
062 055 054 053 040 009	$39 \pm 0.5$ $42.5 \pm 0.5$ $48.5 \pm 0.5$ $53.5 \pm 1.5$ $61.5 \pm 1.5$ $70 \pm 1$ $76.5 \pm 1.5$	15 15 15 5.5 6.0 4.0 2.5	1.00 1.00 1.00 1.00 1.00 1.00	40 40 40 40 40 40 40	0 0 0 0 0
045 051 034	$80.5 \pm 0.5$ $89 \pm 1$ $70 \pm 1$	2.5 2.5 4.0	1.00 1.00 0.10	40 40 40	0 0 0
039 009 050	$70 \pm 1$ $70 \pm 1$ $70 \pm 1$	4.0 4.0 4.0	0.50 1.00 1.50	40 40 40	0 0 0
058 047 046 009 048B 035	$70 \pm 1$ $70 \pm 1$ $70 \pm 1$ $70 \pm 1$ $70 \pm 1$ $70 \pm 1$	4.0 4.0 4.0 4.0 4.0 4.0	1.00 1.00 1.00 1.00 1.00 1.00	5 10 20 40 77 160	0 0 0 0 0
009 063 064 049	$70 \pm 1$ $70 \pm 1$ $70 \pm 1$ $70 \pm 1$	4.0 4.0 4.0 4.0	1.00 1.00 1.00 1.00	40 40 40 40	0 1.0 2.0 5.0

received. Fresh deionized water from a Milli-Q Plus water purification system (Millipore, Bedford; 0.2-um filter) was used throughout this work. The NIPAM solution was stirred under a nitrogen atmosphere in a 150-mL reactor for ~30 min and heated to the required temperature using a digital heating plate and water bath covered with a thin layer of paraffin oil. A KPS/ water solution was added to the reactor to initiate polymerization. The reaction system was stirred at the incubation temperature for a time sufficient to ensure that all of the monomer was exhausted. After being cooled to room temperature, the final reaction dispersion was ready for characterization. Table 1 contains the details of the reaction conditions used for the different samples prepared for this study.

Laser Light Scattering. The apparatus used for the light scattering measurements was an ALV-5000 spectrometer/ goniometer equipped with a digital time correlator and a helium-

We used static light scattering to measure the weight-average molar mass  $M_{\rm w}$  and z-average root-mean-square radius of gyration  $R_g$ . For small particles, we used a standard Zimm plot analysis to find  $M_{\rm w}$  and  $R_{\rm g}$  from the Rayleigh ratio  $R_{\rm vv}(q)$ , determined from the time-averaged scattered intensity<sup>16</sup>

$$\frac{KC}{R_{\rm vv}(q)} \simeq \frac{1}{M_{\rm w}} \left( 1 + \frac{1}{3} R_{\rm g}^2 q^2 \right) + 2A_2 C \tag{1}$$

where  $K=4\pi^2n^2(\mathrm{d}n/\mathrm{d}C)^2/(N_A\lambda_0^4)$ ,  $q=(4\pi n/\lambda_0)\sin(\theta/2)$  is the scattering wave vector, and  $A_2$  is the second virial coefficient, with  $N_A$ , n, C,  $\lambda_0$ , and  $\theta$  being Avogadro's constant, the solvent refractive index, the concentration (g/mL), the light wavelength in a vacuum, and the scattering angle, respectively. The angular range at which these measurements were carried out was restricted to keep  $qR \ll 1$ . For PNIPAM, the values used for dn/dC were 0.167 and 0.174 mL/g at 25 and 40 °C, respectively. 17 It should be mentioned that, for most of the batches in Table 1, only one dilute sample from each batch at a concentration of  $\sim\!\!10^{-5}\,\text{g/mL}$  was used in the static laser light scattering to obtain  $M_{\rm w}$  and  $R_{\rm g}$ . Because the samples are so dilute and  $A_2$  in eq 1 is so small for PNIPAM in water, 18 the difference between  $M_{\rm w}$ measured using only one dilute sample and that using a group

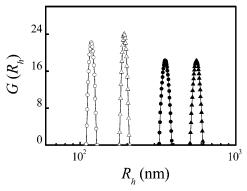


Figure 1. Normalized hydrodynamic radius distribution of self-cross-linked NIPAM microgels in water at 25  $^{\circ}$ C (solid symbols) and 40  $^{\circ}$ C (open symbols) for batch 053 (triangles, C $=4.87\times10^{-5}$  g/mL) and batch 038 (circles,  $C=2.62\times10^{-5}$ g/mL), as was measured by DLS at scattering angles of 12 and 15° for batches 053 and 038 at 25 °C and at 30° for both batches at 40 °C.

of samples is negligible. For larger particles, we fit the data to the form

$$\frac{KC}{R_{vv}(q, R)} = \frac{1}{M_{w}P(q, R)}$$
 (2)

where  $P(q, R) = [3/(q^3R^3)(\sin(qR) - qR\cos(qR))]^2$  is the form factor for uniform spheres with radius R.

We used dynamic light scattering (DLS) to measure the time correlation function of the scattered intensity  $g^2(\tau)$  as a function of the decay time  $\tau$ . The DLS measurements were made at a scattering angle of  $\theta = 30^{\circ}$  unless otherwise noted. The samples were prepared by diluting the sphere dispersions to polymer concentrations of  $10^{-5}$  g/mL. The hydrodynamic radius  $\langle R_h \rangle$  and polydispersity of the samples were determined from analysis of  $g^2(\tau)$  using either CONTIN<sup>19</sup> or cumulant analysis.<sup>20</sup> In general, the particle size distributions were very narrow with relative standard deviations of about 10%.

The solid density of the particles was calculated from the results of both static and DLS measurements. Previous studies have shown that PNIPAM microgel particles are spherical.<sup>1,3</sup> For spherical particles with a narrow particle size distribution, the solid density ho can be calculated from the simple equation  $M_{
m w}$  $= 4/_3\pi\rho\langle R_{\rm h}\rangle^3 N_{\rm A}$ .

#### **Results and Discussion**

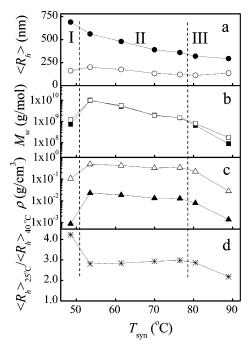
Particle Characterization. Figure 1 shows the distribution of the hydrodynamic radii obtained by CONTIN analysis of the DLS data for samples from batches 053 (triangles) and 038 (circles) at 25 (solid symbols) and 40 (open symbols) °C, below and above the LCST of PNIPAM, which is typically around 33 °C. Below the LCST, the distributions are characterized by average hydrodynamic radii of 560 and 352 nm and small relative standard deviations of about 10%. The average radius decreases by a factor of 2.9, and the distributions become even narrower as the temperature is increased.

We also probed the particle structures by comparing the particle radii from the static measurements, which measure the particle size on the basis of the refractive index variations, and from the dynamic measurements, which measure the particle size on the basis of the hydrodynamic size. The ratios of  $R_g/\langle R_h \rangle$  are between 0.8 and 1 at 25 °C and between 0.65 and 0.8 at 40 °C for all the particles measured, close to the theoretical value of 0.77 for uniform spheres.

<sup>(16)</sup> Zimm, B. H. *J. Chem. Phys.* **1948**, *16*, 1099.
(17) Gao, J.; Wu, C. *Macromolecules* **1997**, *30*, 6873.
(18) Gao, J.; Hu, Z. *Langmuir* **2002**, *18*, 1360.

<sup>(19)</sup> Provencher, S. W. Makromol. Chem. 1979, 180, 201; Comput. Phys. Commun. 1982, 27, 229.

<sup>(20)</sup> Chu, B. Laser Light Scattering, Academic Press: Boston, 1991.

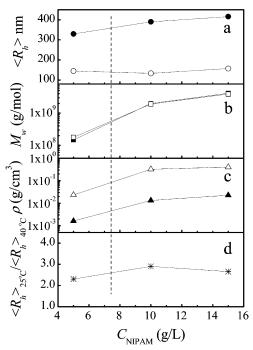


**Figure 2.** (a) z-average hydrodynamic radius  $\langle R_h \rangle$ , (b) weightaverage molar mass  $M_{\rm w}$ , (c) average solid density  $\rho$ , and (d) reduced size  $\langle R_h \rangle_{25^{\circ}\text{C}}/\langle R_h \rangle_{40^{\circ}\text{C}}$  of particles produced as a function of the reaction temperature  $T_{\rm syn}$  at a constant initial  $C_{\rm NIPAM}$  of 10 g/L and an initial  $C_{\rm KPS}$  of 400 mg/L. The solid and open symbols represent data taken at 25 and 40 °C, respectively. The light scattering measurements were made on dilute samples with  $C \sim 10^{-5}$  g/mL. The dashed lines separate regions of sufficient (II) and insufficient (I and III) cross-linking.

Influence of the Reaction Conditions. The formation of self-cross-linked gel nanospheres was investigated systematically as functions of the reaction temperature  $T_{\rm syn}$ , initial NIPAM monomer concentration  $C_{\rm NIPAM}$ , and initial KPS initiator concentration  $C_{KPS}$ .

The production of self-cross-linked microgels was first investigated at different reaction temperatures, while the initial concentrations of NIPAM and KPS were kept at 10 g/L and 400 mg/L, respectively. Different reaction times, as are specified in Table 1, were used to ensure the completion of the monomer conversion. Figure 2 shows how the average hydrodynamic radius  $\langle R_h \rangle$ , molar mass  $M_{\rm w}$ , solid density  $\rho$ , and swelling ratio  $\langle R_{\rm h} \rangle_{25^{\circ}{\rm C}} / \langle R_{\rm h} \rangle_{40^{\circ}{\rm C}}$ change with the reaction temperature. The data can be discussed in terms of three temperature regions, as are shown separated by dashed lines in Figure 2: (I)  $T_{\rm syn}$  < 52 °C, (II) 52 <  $T_{\rm syn}$  < 78 °C, and (III)  $T_{\rm syn}$  > 78 °C. Only in region II were the measured values of  $M_{\rm w}$  at 25 and 40 °C consistent. In both of the other regions, the values of  $M_{\rm w}$  measured at 40 °C were higher than those measured at 25 °C. We interpret the observation of higher  $M_{\rm w}$  values at 40 °C than at 25 °C as a sign of insufficient crosslinking; it has been shown<sup>21</sup> that, if cross-linking is insufficient, free chains will pack or adsorb onto existing gel spheres or associate to form aggregates when the temperature is above the LCST but will dissociate below the LCST, leading to a change in the average  $M_{\rm w}$  of the particles.

In region II, where the values of  $M_{\rm w}$  measured below and above the LSCT are consistent and we believe that sufficient cross-linking has occurred,  $M_{\rm w}$ ,  $\langle R_{\rm h} \rangle_{25^{\circ}\rm C}$ , and  $\langle R_h \rangle_{40^{\circ}\text{C}}$  all decrease with an increasing reaction temperature. The ratio of  $\langle R_h \rangle_{25^{\circ}\text{C}} / \langle R_h \rangle_{40^{\circ}\text{C}}$  changes little in this



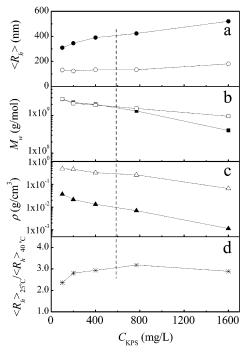
**Figure 3.** (a)  $\langle R_{\rm h} \rangle$ , (b)  $M_{\rm w}$ , (c)  $\rho$ , and (d)  $\langle R_{\rm h} \rangle_{25^{\circ} \rm C} / \langle R_{\rm h} \rangle_{40^{\circ} \rm C}$  of particles produced as a function of the initial  $C_{\rm NIPAM}$  at a constant initial  $C_{KPS}$  of 400 mg/L and a constant  $T_{syn}$  of 70 °C. The solid and open symbols represent data taken at 25 and 40 °C, respectively. Light scattering measurements were made on dilute samples with  $C \sim 10^{-5}$  g/mL. The dashed line separates regions of sufficient (right side) and insufficient (left side) crosslinking.

region, falling between 3.0 and 2.8. The high ratio of  $\langle R_h \rangle_{25^{\circ}\text{C}} / \langle R_h \rangle_{40^{\circ}\text{C}}$  results in a large difference in the solid density of the gel spheres below and above the LCST. The solid density  $\rho$  of the gel spheres measured at 40 °C decreases from 0.48 to 0.32 g/cm<sup>3</sup> as the reaction temperature is increased, whereas that measured at 25 °C decreases from 0.023 to 0.013 g/cm<sup>3</sup>. Above 80 °C in region III, these trends continue, except that the molar mass measured at 40 °C is higher than that at 25 °C, indicating that not all of the linear chains have been cross-linked.

At temperatures below about 50 °C, both the polymerization and the cross-linking rates were reduced. Batch 062, synthesized at 39 °C, showed only minimal evidence of monomer conversion into polymers. The value of  $M_{\!\scriptscriptstyle 
m W}$ measured at 25 °C was only  $1.4 \times 10^5$  g/mol, indicating no gel particle formation. In batch 055, synthesized between 42 and 43 °C, the  $M_{\rm w}$  values were  $3.9 \times 10^6$  and  $6.2 \times 10^7$  at 25 and 40 °C, respectively, possibly indicating minimal particle formation, where the different values of  $M_{\rm w}$  measured at the two temperatures again indicates the packing or aggregation of free chains. Only in batch 054, synthesized between 48 and 49 °C, is there clear evidence of stable particle formation by self-cross-linking; here, the values for both  $M_{\rm w}$  and  $\langle R_{\rm h} \rangle$  are high, though the increase in  $M_{\rm w}$  upon heating the solution to 40 °C indicates some packing or aggregation of un-cross-linked polymer chains. This lower limit for stable particle formation is slightly lower than that reported by other authors.<sup>22</sup>

The influence of the monomer concentration  $C_{\text{NIPAM}}$  on self-cross-linking is shown in Figure 3 where  $\langle R_h \rangle$ ,  $M_w$ ,  $\rho$ , and the ratio  $\langle R_h \rangle_{25^{\circ}C} / \langle R_h \rangle_{40^{\circ}C}$  are plotted as functions of  $C_{NIPAM}$  for polymerization at the standard reaction temperature of 70 °C and constant a  $C_{KPS}$  of 400 mg/L. As

<sup>(22)</sup> Tam, K. C.; Wu, X. Y.; Pelton, R. H. J. Polym. Sci., Part A: Polym. Chem. 1993, 31, 963.



**Figure 4.** (a)  $\langle R_h \rangle$ , (b)  $M_w$ , (c)  $\rho$ , and (d)  $\langle R_h \rangle_{25^{\circ}\text{C}} \langle R_h \rangle_{40^{\circ}\text{C}}$  of particles produced as a function of the initial  $C_{\text{NPS}}$  at a constant initial  $C_{\text{NIPAM}}$  of 10 g/L and a constant  $T_{\text{syn}}$  of 70 °C. The solid and open symbols represent data taken at 25 and 40 °C, respectively. Light scattering measurements were made on dilute samples with  $C \sim 10^{-5}$  g/mL. The dashed line separates regions of sufficient (left side) and insufficient (right side) crosslinking.

 $C_{\rm NIPAM}$  increases from 5 to 15 g/L,  $\langle R_h \rangle_{25^{\circ}\rm C},~M_w,$  and  $\rho$  all increase. The data for the molar mass for batch 039 made with a  $C_{\rm NIPAM}$  of 5 g/L show insufficient self-cross-linking; the dashed line on Figure 3 indicates that the threshold for sufficient self-cross-linking lies between 5 and 10 g/L, and we have not determined its precise location. At an even lower  $C_{\rm NIPAM}$  of 1 g/L, no particles were observed.

The influence of the initiator concentration  $C_{\text{KPS}}$  on self-cross-linking was studied at a constant initial  $C_{\text{NIPAM}}$  of 10 g/L and a constant reaction temperature  $T_{\text{syn}}$  of 70 °C. As is shown in Figure 4,  $\langle R_h \rangle_{25^{\circ}\text{C}}$  increases while  $M_{\text{w}}$  and  $\rho$  both decrease with  $C_{\text{KPS}}$  for the range of  $C_{\text{KPS}}$  values studied. At the lowest  $C_{\text{KPS}}$  value used (50 mg/L in batch 058), a density of 0.042 g/cm³ was measured at 25 °C, the highest value obtained for self-cross-linked swollen particles in this work; this value is higher than that observed in BIS cross-linked gels. <sup>18</sup> To the right of the dashed line in Figure 4, a region of high  $C_{\text{KPS}}$  is observed, where  $M_{\text{w}}$  at 40 °C is higher than that at 25 °C, indicating that insufficient self-cross-linking has occurred.

The trends observed in the data shown in Figures 2–4 can be discussed in terms of the ratio of free radicals to monomers. In Figure 2, this ratio increases with the temperature; while the total concentration of KPS is constant, the number of free radicals available increases with the temperature. In Figure 3, the ratio decreases as  $C_{\text{NIPAM}}$  is increased. The trends in these two figures are then the same;  $\langle R_{\text{h}} \rangle_{\text{25}^{\circ}\text{C}}$ ,  $M_{\text{w}}$ , and  $\rho$  all decrease as the ratio of free radicals to monomers increases. The exception to this behavior is shown in Figure 4, where the ratio increase as  $C_{\text{KPS}}$  increases; while both  $M_{\text{w}}$  and  $\rho$  decrease, an *increase* in  $\langle R_{\text{h}} \rangle_{\text{25}^{\circ}\text{C}}$  is observed. This ratio also appears to be important in defining the regions where sufficient self-cross-linking occurs. The threshold for sufficient cross-linking, as is indicated by a dashed line in both Figures

3 and 4, corresponds to a ratio of  $C_{\rm KPS}$  to  $C_{\rm NIPAM}$  of approximately 0.06.

An explanation of these trends can be found in the principles of surfactant-free emulsion polymerization and colloidal stability.  $^{23}$  In surfactant-free conditions, an ionic initiator such as KPS not only initiates polymerization but also acts as the source of charge required to stabilize the aggregate particles and a source of ionic strength. When the KPS is added to the reaction mixture, it dissociates into its ionic constituents, some of which decompose into ionic free radicals  $\dot{SO_4}^-$ . The sulfate groups are incorporated into the polymer chains, providing the surface charge required to stabilize the particles. The particles grow by association of PNIPAM chains until they reach a surface potential  $\psi$  high enough to prevent further association of the chains and coagulation between the particles.

A few simple relations can be used to discuss the trends observed in Figures 2-4 in the regions where effective self-cross-linking occurs. An aggregate sphere of radius R made up of  $N_{\rm c}$  precursor chains, each having average molar mass  $M_{\rm c}$  and carrying some average number of charged groups, will have a surface charge density per particle  $\sigma$  given by

$$\sigma \propto N_c/R^2 \tag{3}$$

This relationship can be written in terms of  $N_c$ ,  $M_c$ , and the solid density of the aggregate  $\rho_a$ 

$$\sigma \propto N_c^{1/3} (\rho_a/M_c)^{2/3} \tag{4}$$

because  $M_{\rm w}=N_{\rm c}M_{\rm c}={}^4/_3\pi\rho_{\rm a}R^3N_{\rm A}$ . The surface potential  $\psi$  depends on the surface charge density  $\sigma$  and the Debye screening length  $\kappa^{-1}$  and is given, approximately, by<sup>24</sup>

$$\psi \propto \sigma/\kappa$$
 (5)

Because the Debye screening length is inversely proportional to the square root of the concentration of the screening ions [I], this equation can be rewritten as

$$\psi \propto \sigma/[I]^{1/2} \tag{6}$$

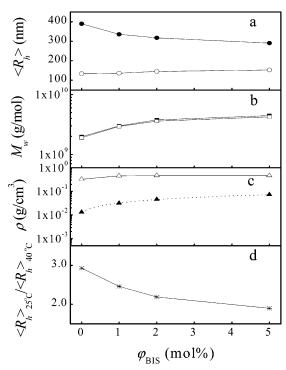
The chains will aggregate until  $\psi$  is large enough to prevent further association. For cases where [I] is constant, the surface charge density  $\sigma$  alone, as is given by eq 4, is sufficient to determine when the particles reach their stable sizes.

For the reaction batches shown in Figures 2 and 3, an increase in the molar ratio of free radicals to monomers leads to a decrease in  $M_c$  and an increase in the total number of chains. From eq 4, a constant  $\sigma$  for smaller  $M_c$ values also means that  $N_c$ , the average number of associated chains inside each sphere, will be smaller. Here, we have neglected changes in the aggregate density because the association of the chains occurs at temperatures well above the LCST, where the aggregates exist in a highly collapsed state. As a result of smaller  $M_c$  and  $N_{\rm c}$  values, the molar mass  $M_{\rm w}$  should decrease significantly as the ratio of free radicals to monomers is increased, as is observed in the trends shown in Figures 2 and 3. A careful examination of the density data shown in Figures 2 and 3 does reveal small decreases in the solid density as the ratio of free radicals to monomers increases. An important aspect of the particle formation is the incor-

<sup>(23)</sup> Gilbert, R. G.  $Emulsion\,Polymerization,\,a\,Mechanistic\,Approach;$  Academic Press: London, 1995.

<sup>(24)</sup> Peach, S. Macromolecules 1998, 31, 3372.





**Figure 5.** (a)  $\langle R_h \rangle$ , (b)  $M_w$ , (c)  $\rho$ , and (d)  $\langle R_h \rangle_{25^{\circ}C} \langle R_h \rangle_{40^{\circ}C}$  of particles produced as a function of the initial molar ratio of BIS to NIPAM ( $\varphi_{BIS}$ ) at a constant initial  $C_{NIPAM}$  of 10 g/L, constant initial  $C_{KPS}$  of 400 mg/L, and constant  $T_{syn}$  of 70 °C. The solid and open symbols represent data taken at 25 and 40 °C, respectively. Light scattering measurements were made on samples with concentrations  $C \sim 10^{-5}$  g/mL. The dashed line is a fit of eq 7 to the data.

poration of the ionic groups SO<sub>4</sub><sup>-</sup> into the polymer chains and polymer chain networks. As the ratio of free radicals to monomers increases, the concentration of the covalently bound ionic groups increases, leading to an increase in the hydrophilicity of the particles. This results in a decrease of the solid density  $\rho$  of the gel particles when they are diluted, especially at temperatures below the LCST. Both Figures 2 and 3 clearly show this trend. An extreme case was seen in batch 034 where no particles were observed; we believe that the weight ratio of KPS to NIPAM was so high that the polymer chains were simply too hydrophilic to associate in water even at 70 °C. As is seen in both Figures 2 and 3, the particle size  $\langle R_h \rangle$  tends to decrease as the ratio of free radicals to monomers increases, confirming that the change in  $M_{\rm w}$ , rather than the change in  $\rho$ , dominates the change in  $\langle R_h \rangle$ .

For the data shown in Figure 4, both the ratio of decomposed KPS to NIPAM and the ionic strength increase as  $C_{KPS}$  is increased. Again, we expect that an increase in the molar ratio of free radicals to monomers should lead to a decrease in  $M_c$ ; however, the increasing ionic strength will mean that a higher  $N_c$ , and hence  $M_w$ , is expected to satisfy eq 6. Although in Figure 4 the trend of  $M_{\rm w}$  is still the same as that seen in Figures 2 and 3, the change of  $M_{\rm w}$  with  $C_{\rm KPS}$  is not as large as it would be if there were no screening effect. This can be seen by comparing the molar masses of the particles made with 15 g/L NIPAM and 400 mg/L KPS (batch 050), as is shown in Figure 3, to the trends of those at lower  $C_{\rm KPS}$  (batches 046 and 047), as shown in Figure 4. The  $M_{\rm w}$  values in Figure 4 for concentrations below 400 mg/L KPS, corresponding to a lower ionic strength, are lower. A decrease in  $\langle R_h \rangle$  might be expected to accompany this decrease in  $M_{\rm w}$ , which is not observed in Figure 4. However, the radius is measured at a low concentration, where the surface charge is no

longer screened and a further swelling of the particles is expected. The trends of an increasing radius and a decreasing density with a higher  $C_{KPS}$  are a consequence of the incorporation of more charge into the particles.

These results can be compared to studies of the synthesis of surfactant-free polystyrene nanospheres<sup>25</sup> and PNIPAM chain aggregates.<sup>21</sup> In these studies, the volume of the particles was observed to increase linearly with the initial monomer concentration and polymer chain concentration, respectively. The radii of the polystyrene nanospheres were also observed to increase as the initiator (KPS) concentration increased, but the change of  $M_{\rm w}$  was not recorded.

**Cross-Linking Characterization.** We investigated the extent of self-cross-linking by using a standard synthesis of PNIPAM gel spheres that includes the addition of a standard cross-linker, BIS. In Figure 5,  $\langle R_h \rangle$ ,  $M_{\rm w}$ ,  $\rho$ , and  $\langle R_{\rm h} \rangle_{25^{\circ}{\rm C}} / \langle R_{\rm h} \rangle_{40^{\circ}{\rm C}}$  are plotted for samples made of 0, 1, 2, and 5 mol % BIS to NIPAM  $\varphi_{BIS}$ . As  $\varphi_{BIS}$  increases,  $M_{\rm w}$  and  $\rho$  increase, and the gel spheres become less swollen at 25 °C. This is consistent with other work on PNIPAM microgels and the idea that increased BIS cross-linking leads to a higher gel density.9

Theoretically, it is possible to calculate the cross-linking density in terms of the number of repeat units between the neighboring cross-linking points, using the Huggins parameter  $^{10,26}$  or other treatments.  $^{12}$  Here, we simply use the solid density of the gel spheres at 25 °C as an indication of the amount of cross-linking to estimate the extent of self-cross-linking. We fit a function of the form

$$\rho = A(\varphi_{\rm BIS} + \varphi_{\rm o})^n \tag{7}$$

to the data points of Figure 5 for the solid density at 25 °C, where  $\varphi_0$  is the self-cross-linking contribution. We obtained values of  $\varphi_0 = 0.25 \pm 0.08$ , *A* (wt %) = 2.9 ± 0.2, and  $n = 0.56 \pm 0.04$ . This implies that, under standard reaction conditions, self-cross-linking occurs at a rate corresponding to  $\varphi_{BIS} = 0.25$  mol %.

## **Conclusions**

Results of the systematic synthesis and light scattering characterization of self-cross-linked PNIPAM microgels have been presented. The particle size  $\langle R_h \rangle$ , molar mass  $M_{\rm w}$ , and solid density  $\rho$  of the gel spheres have been investigated at 25 and 40 °C, below and above the LCST of PNIPAM, respectively, as functions of the reaction temperature  $T_{\text{syn}}$ , initial monomer concentration  $C_{\text{NIPAM}}$ , and initial initiator concentration  $C_{KPS}$ . We found suitable ranges of  $T_{\text{syn}}$ ,  $C_{\text{NIPAM}}$ , and  $C_{\text{KPS}}$  in which effective selfcross-linking can occur. In general, sufficient cross-linking was observed in samples where the solid content was greater than 30 wt % at 40 °C or 1.3 wt % at 25 °C. The formation of self-cross-linked chain networks requires that the local polymer chain concentration be high enough or, equivalently, the distance between the neighboring chains or chain segments be short enough so that there is a finite probability of tert-C free-radical propagation or termination occurring. We observe that regions of insufficient cross-linking correspond to regions where the molar ratio of KPS to NIPAM is high so that the polymer chains are highly charged and very hydrophilic; the exceptions are the cases of low-temperature synthesis where very little decomposed KPS is available for polymerization, let alone cross-linking. For samples made under standard reaction

<sup>(25)</sup> Zhang, W. M.; Gao, J.; Wu, C. Macromolecules 1997, 30, 6388. (26) Flory, P. J. *Principles of Polymer Chemistry*; Cornell University Press: New York, 1953.

conditions, ratios of  $C_{\text{KPS}}$  to  $C_{\text{NIPAM}}$  less than  $\sim 0.06$  are required for the formation of self-cross-linked particles. Comparison of data for self-cross-linked and BIS-cross-linked gel spheres indicates that self-cross-linking under standard reaction conditions occurs at a rate equivalent to the addition of 0.25 mol % BIS. It is important to note that the presence of intrinsic self-cross-linking under standard reaction conditions means that the actual degree of cross-linking that occurs in BIS-cross-linked particles is systematically higher than previously thought. Consistent with lower cross-linking, the swelling ratio for self-cross-linked spheres is generally higher than that for BIS-cross-linked spheres. The ratio of the radii  $\langle R_h \rangle_{25^{\circ}} c / \langle R_h \rangle_{40^{\circ}} c$  lies in a range between 2.8 and 3.0 and is generally highest in regions where the solid content is the lowest.

In this work, neither surfactant nor cross-linker is introduced. Only interchain self-cross-linking is involved in the formation of polymer chain networks. As cross-linker-free and surfactant-free particles, these slightly cross-linked soft PNIPAM microgels are more closely

related to PNIPAM and may be used as standard particles to study the PNIPAM chain and PNIPAM gel phase transitions and the interactions between PNIPAM and many other materials such as surfactants, <sup>27</sup> salts, <sup>28</sup> and solvents. <sup>29</sup> The particle size lies in a convenient and tunable submicron size range, which is ideal for studying the angular dependence of the scattered light, internal motion, <sup>30</sup> and other optical phenomena.

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<sup>(27)</sup> Wu, C.; Zhou, S. J. Polym. Sci., Part B: Polym. Phys. 1996, 34, 1597.

<sup>(28)</sup> Routh, A. F.; Vincent, B. Langmuir 2002, 18, 5366.
(29) Costa, R. O. R.; Freitas, R. F. S. Polymer 2002, 43, 5879.

<sup>(30)</sup> Wu, C.; Zhou, S. Macromolecules 1996, 29, 1574.