The Theory of Human Capital Revisited: 
On the Interaction of General and Specific Investments*

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Summary
Human capital theory distinguishes between training in general-usage and firm-specific skills. Becker (1964) argues that employers will only invest in specific training, not general training, when labour markets are competitive. The paper reconsiders Becker’s theory. Using essentially his framework, we show that there exists an incentive complementarity between employer-sponsored general and specific training: the possibility to provide specific training leads the employer to invest in general human capital. Conversely, the latter reduces the hold-up problem that arises with firm-specific training. We also consider the desirability of institutionalized training programs and the virtues of breach penalties, and discuss some empirical facts that could be explained by the theory.

Keywords: Human Capital Formation, General and Specific Training, Hold-up Problem

JEL–Classification: C78, L14, L15, D82

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Based on the transferability of the acquired skills, human capital theory distinguishes between investments in general-usage and specific human capital. As pointed out by Becker (1964), this distinction is important if these investments take the form of employer-provided training. While the returns to specific training can be realized only in an ongoing relationship with the training firm, general training increases the productivity of a worker in many firms besides those providing it. Becker’s theory separately addresses these phenomena and draws two main conclusions. First, employers will share the returns and the cost of investments in firm-specific skills with their employees. Second, in a competitive labour market firms will not invest into general skills of their employees due to their inability to collect the returns from such investments. Therefore, workers will pay the full cost of general training.

Yet, there is a large body of evidence indicating that firms voluntarily bear the cost of training, even if the acquired skills are largely general in nature. This is particularly apparent in countries with institutionalized apprenticeship systems. In Germany, for example, participants in the system engage in part-time schooling and on-the-job training and receive upon completion a nation-wide accepted certificate that helps to make their skills marketable throughout the profession. Franz and Soskice (1995) estimate that in 1985 German employers paid a net cost per apprentice of about DM 12,300 (approximately USD 5000). Using 1991 survey data on training firms in Germany, von Bardeleben, Beicht and Feher (1995) conclude that even under the most conservative assumptions, the net cost of an apprentice in a larger German firm exceeds DM 7,500.¹

The present paper reconsiders Becker’s seminal arguments in a framework where firms can provide both general and specific training. To this end, we employ a simple model that preserves two essential characteristics of the standard theory: a) the labour market

¹Interestingly, this study also estimates net training costs to be negative for small firms (see Section 2 for a discussion). For further evidence on firm-sponsored general training, see Soskice (1994) and Harhoff and Kane (1997) for Germany, and Ryan (1980) and Bishop (1991) for the U.S.
is frictionless in the sense that a worker always receives the full return from general training and b) he obtains a share of the return from specific training. Our main result is that employers may still voluntarily provide a positive amount of general training or, alternatively, be willing to share the costs of such training with their employees.

As a first step to this conclusion, we find that general and specific investments cannot be separately analyzed. Rather, the presence of the relationship-specific rent that is generated through firm-specific training makes the parties’ returns from either type of investment interdependent even if (as we posit) there is no technological link between them. The idea of our approach can be outlined as follows. If a firm can provide only general training, it has no incentives to invest since the employee can recover the full return on his human capital in the absence of market imperfections. If, in contrast, the firm can also expend investments in relationship-specific skills, this will create a wedge between the worker’s productivity if he leaves his current employer and his productivity if employment continues beyond the training period. Once training is completed, firm and worker are therefore in a bilateral monopoly position.

Now suppose that in the ensuing wage negotiations, the surplus from continued employment is divided with the external market opportunities acting as outside options. Outside options – as opposed to threat points – act as a lower bound to a party’s payoffs in negotiations but otherwise do not affect the outcome.\(^2\) Then, although the (above market) rent depends only on the worker’s specific human capital, the way in which it is shared also depends on his general skills. In particular, as long as the external market opportunity of the worker (which fully reflects his marginal product from general training) is binding, negotiations will lead to the going market wage. As a result, the rent from specific human capital accrues entirely to the firm while it appropriates no return from the worker’s general human capital. If this rent is sufficiently large relative

\(^2\)This result has been derived in a version of the Rubinstein game where at least one party can terminate bargaining and take an outside option (Shaked and Sutton, 1984).
to the return on general human capital, however, or if the worker’s bargaining power is sufficiently high, his share of the surplus from continued employment will be above what he can realize on the external market. As a consequence, the worker captures part of the rent from specific skills and a ‘Hold-up’ problem (Williamson, 1985; Grout, 1984) arises. While hold-up discourages specific training, it at the same time improves the firm’s incentives to provide general training: although external wages rise one-to-one with a worker’s productivity from general skills, the wage he obtains if he stays with the training firm rises by less than that if surplus sharing (hold-up) occurs.

A number of results follow immediately from this observation. First, the higher the level of specific training, the larger the resulting gap and, hence, the more incentives the firm has to to invest into general training. Second, the reverse also holds, i.e., general skills enhance the firm’s provision of specific training relative to a scenario where general training is not taken into consideration. This is because in situations where a worker’s outside wage is binding for given investment levels, the employer reaps the full return from specific investments on the margin because each worker’s equilibrium wage then coincides with his marginal product from general training. As a consequence, her investment incentives in specific training increase as compared to a setting without general training where the worker’s outside wage poses a weaker constraint in bargaining. Hence, general and specific human capital are complementary from the firm’s point of view even if their returns (and provision costs) are technologically disconnected. For this reason, we also find that the parties will agree on a general training level in excess of the first best if this investment can be contracted upon in advance (as would, e.g., be the case in the German ‘dual system’). Since general and specific training are complements, a higher level of general training stimulates the provision of specific investments, and thus further alleviates the hold-up problem that arises when specific training is non-contractible. Finally, we argue that extending our framework to al-
low for (equilibrium) turnover or the possibility of long-term contractual arrangements qualitatively leaves these conclusions unaffected.

These conclusions are straightforward implications of our main result: the presence of specific skills creates rents which will be shared in a way that allows the firm to partly recapture its general training outlays. Key to understanding this property of the wage bargaining outcome is that some form of the outside option principle applies. In other words, the default payoffs in case of a disagreement during negotiations do not rise one-to-one by what the parties’ can obtain on the external market. The latter would be true if one considered the polar case of Nash bargaining instead, where the parties’ external market opportunities act as threat points. Under Nash bargaining, the worker’s default payoff is identical to his outside wage, which in a competitive labour market equals his product from general skills. While specific training would still generate an above-market rent, its division would be unaffected by general training outlays and the firm would have no incentive to invest in general skills. The results we derive thus do depend on the bargaining solution. The reader should keep in mind, however, that what matters qualitatively is only that negotiations do not exactly follow the Nash-solution, where the worker’s threat point (and his final payoff from bargaining in our formulation) rises one-to-one with his outside option. This condition is testable and appears to be satisfied in practice (see, e.g., Binmore, Shaked and Sutton, 1989; Knez and Camerer, 1995; Kahn and Murnighan, 1993, and Oosterbeek et al, 2004, for experimental evidence and Scaramozzino (1991) for econometrical evidence in a study of the UK manufacturing industry).

The present paper is related to several contributions in the literature. First, we adopt our theoretical approach from previous work on specific investments and the hold-up problem (see, among others, Grout, 1984; Grossman and Hart, 1986; Hart and Moore, 1990; and Edlin and Reichelstein, 1996). In particular, our analysis draws on
MacLeod and Malcomson (1993a, 1995) who provide a natural framework to study both general and specific investments in bilateral trade relationships. To formalize how the rent generated through specific investments is shared among the parties, the authors develop a bargaining game where negotiation and trade takes place over time, which reflects the long-term nature of employment relationships well. The equilibrium outcome follows the outside option principle, which we adopt for analytical simplicity. As argued above, however, that the outside option principle applies in its pure form is not necessary for our findings.

Second, a number of recent papers have suggested different reasons for why we observe firm-sponsored general training. This literature primarily focuses on general human capital accumulation and disregards specific skills. One prominent explanation is based on asymmetric information between the training firm and potential future employers. Katz and Ziderman (1990) study a model where a worker’s level of training is unobserved by the market (See also Chiang and Chiang, 1990, and Chang and Wang, 1996). In Acemoglu and Pischke (1998), the training firm obtains superior information on the worker’s ability during the training period. In both cases, the informational dis-
advantage of firms in the external labour market causes the equilibrium market wage to fall short of the marginal product of skilled workers. A similar situation arises if general skills are only valuable in a small number of firms (Stevens, 1994; Gersbach and Schmutzler, 2003) or if there are search costs associated with finding alternative employers (Acemoglu, 1997). Surveying the literature, Acemoglu and Pischke (1999) call this common element a ‘compressed wage structure’ in that there exists a wedge between the wage and the marginal product from general skills which increases in the level of training provided, and identify ‘compressed wages’ as necessary and sufficient for employee-sponsored general training. In general, therefore, there must be some form of market friction which allow training firms to enjoy monopsony power over its workers, thus compressing wages and enabling them to capture (part of) the return from general training. The authors go on to show that wage compression can endogenously emerge in economies with minimum wages, wage-setting unions, or worker moral hazard. They also note that investment in specific training can have a similar effect as long as general and specific skills are complements in a firm’s production function. A related point has been put made by Franz and Soskice (1995) who recognize that employers may provide general training if general and specific investments are complements in the firm’s investment cost function. Whether or not such technological complementarities exist is an open empirical question. The present paper demonstrates, though, that these are not needed. Our argument also involves frictions that allow firms to at least partially exercise some market power, but those frictions endogenously arise through training in firm-specific skills because specific skills naturally generate rents. It is then the division of these rents in the ensuing wage bargaining between employer and employee that leads to a wage that does not always rise one-to-one the workers marginal product from general skills.\(^5\)

\(^5\)While the bargaining outcome thus resembles the compressed wage structure in Acemoglu and Pischke (1999) at the margin, the wage schedule differs in absolute terms because, as we will see, the
The remainder of the paper proceeds as follows. Section 1.1 develops the basic model with general and specific investments which is analyzed in Section 1.2. In Section 2 we discuss our results and their implications and relate them to empirical evidence. A final Section 3 concludes. Unless otherwise indicated, all proofs are relegated to the Appendix.

1 A Model of General and Specific Training

1.1. The Basic Framework

Consider the following simple model of human capital accumulation in the labour market. There are two risk-neutral parties: a worker and a firm operating in a competitive labour market.\(^6\) Time is divided into a training period \(t = 1\) and a subsequent employment period \(t = 2\) and there is no discounting. In period \(t\), the worker produces an output of \(v_t\), measured in monetary terms, and receives a wage \(w_t\). Without loss of generality, we normalize his disutility from work to zero. In the first period, the worker is unskilled but may be trained by the firm in both general and firm-specific skills. The firm’s total outlays for general and specific training are denoted by \(g \in [0, \bar{g}] \subset \mathbb{R}\) and \(s \in [0, \bar{s}] \subset \mathbb{R}\), respectively. Throughout the analysis, we assume that the firm controls the training technology for both types of skills and incurs the training cost (which it can possibly shift onto the worker through lower wage payments, however). Also, the amount of specific on-the-job training \(s\) cannot be contractually specified. Training in general skills \(g\), in contrast, may or may not be contractible, depending for example employee always receives at least his marginal product from general training.

\(^6\)Restricting attention to a single worker-firm pair is done for expositional convenience only and inconsequential for the results that follow. It is formally justified if there is a sufficiently large number of firms in the market and all firms have access to the same technology that is linear in the number of workers they employ. Risk-neutrality helps us to abstract from insurance considerations that would unnecessarily complicate the analysis (see Rosen, 1985, for a survey on this issue).
on whether there is a formal apprenticeship program in which the parties participate or not.

For simplicity, we let the productivity of an unskilled worker in $t = 1$ be independent of the amount of training he receives and be equal to $v_1 = v_1 \geq 0$. The output $v_2$ of a skilled worker in $t = 2$ is determined by the firm’s investments in general and specific training, $g$ and $s$, as well as a random parameter $\theta$ which may be interpreted as the worker’s ability or as an industry-wide shock that affects market conditions. $\theta$ becomes known to both parties after the first period and is distributed according to a continuously differentiable distribution function $F(\theta)$ over a bounded support $[\bar{\theta}, \bar{\theta}]$.

Let $\sigma = (s, g, \theta) \in \Sigma$ be the state of the world in $t = 2$. To make our point as strong as possible, we disregard in what follows the possibility of technological complementarities between general and specific training. Thus, the productivity of a skilled worker is additively separable in $g$ and $s$,

$$v_2(s, g, \theta) = v^S(s, \theta) + v^G(g, \theta), \quad \forall \sigma \in \Sigma$$

where $v^S$ and $v^G$ are the components of $v_2$ that can be attributed to the acquisition of firm specific and general skills, respectively.

**Assumption 1.** The function $v_2(\cdot)$ is continuously differentiable, strictly concave and increasing in $(s, g)$. Furthermore, for all $\sigma \in \Sigma$,

a) $\lim_{i \to 0} \partial v_2(s, g, \theta)/\partial i = \infty$ and $\lim_{i \to \bar{i}} \partial v_2(s, g, \theta)/\partial i = 0$, $i \in \{s, g\}$,

b) $\inf_\sigma v_2(s, g, \theta) = v_2 \geq 0$ and $v_2(0, g, \theta) = v^G(g, \theta)$.

Part a) of Assumption 1 implies that it is always socially optimal to have a positive amount of either type of training. Part b) ensures that subsequent employment (whether with the current employer or with another firm on the external labour market) is always efficient. Moreover, in the absence of specific investments, all productivity
is general in nature. Given the state $\sigma$ at the beginning of period 2, worker and firm negotiate on the second-period wage in a way to be detailed below. Both parties are free to terminate their relationship at that time, i.e., the worker may decide to quit or the firm may decide to lay the worker off. In either case, the parties have access to the external labour market. The wage determined in this market is denoted by $w^E$. By definition, the worker’s general skills are perfectly marketable while his specific skills loose their value in case of a separation. Thus, another firm hiring the worker (or the firm hiring another skilled worker) would value his output at $v^G(g, \theta)$.

**Assumption 2.** There is perfect competition on the external labour market in both periods and the state $\sigma = (s, g, \theta)$ is commonly observable. Hence, $w^E = v^G(g, \theta)$ for all $\sigma \in \Sigma$.

The sequence of events is as follows. In stage 0, the firm offers a wage contract $w_1$ to the worker that governs the training period. If feasible, the contract may also specify how much training in general skills $g$ he is to receive. Once hired the worker produces $v_1$, and the firm decides in stage 1 on training outlays $s$ and $g$. In stage 2, first period payoffs $\pi_1 = v_1 - w_1 - s - g$ and $u_1 = w_1$ are realized. The random parameter $\theta$ (e.g., the worker’s ability) becomes known in stage 3. The second-period wage $w_2$ is negotiated in stage 4. If employment continues, the worker produces $v_2$ and the parties’ second-period payoffs are $\pi_2 = v_2 - w_2$ and $u_2 = w_2$. If the relationship is terminated, either party can take up its external market opportunity. The payoffs in this case are denoted by $u^E$ and $\pi^E$, respectively.

For future reference, note that by Assumption 1, the worker should be hired in $t = 1$ and continued to be employed by the firm in $t = 2$, irrespective of its training outlays $s$ and $g$. The first-best amount of training each worker receives is thus uniquely defined

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The assumption that the worker should always stay with the training firm can be relaxed to allow for the possibility of efficient separation in $t = 2$. See our brief discussion at the end of this section.
by

$$(s^{FB}, g^{FB}) = \arg \max_{(s, g) \geq 0} \int_{\theta \in [\theta, \bar{\theta}]} [v_2(s, g, \theta)] dF(\theta) + \underline{v}_1 - s - g.$$ 

Using (1), the corresponding first-order conditions are

$$\int_{\theta \in [\theta, \bar{\theta}]} \frac{\partial v^S(s^{FB}, \theta)}{\partial s} dF(\theta) = 1 \quad \text{and} \quad \int_{\theta \in [\theta, \bar{\theta}]} \frac{\partial v^G(g^{FB}, \theta)}{\partial g} dF(\theta) = 1,$$

(2)

which equate the expected marginal return from each type of training with its marginal cost. As one would expect, $g^{FB}$ and $s^{FB}$ are determined independently from each other due to the separability of $v_2(\cdot)$.

It remains to describe the outcome of the negotiations between the firm and a worker on the second-period wage $w_2$. Recall that those take place under symmetric information since the state is known to both parties in stage 4. Clearly, if an agreement is reached and the relationship continues, the net surplus to be divided in negotiations is equal to second period net production $v_2 \geq 0$. However, each party can terminate the relationship and take up its external market opportunity in which case the payoff to the firm and the worker is $\pi^E$ and $u^E$, respectively. In the subsequent formal analysis, we assume for concreteness that negotiations can be formalized by a bargaining solution which ensures efficiency and is characterized by the outside option principle. How our results generalize to other bargaining solutions is discussed in Section 2 below.

**Assumption 3.** Let $\alpha \in (0, 1)$ be a parameter that measures the relative bargaining power of the worker. The second period equilibrium payoffs $\pi_{2}^*$ and $u_{2}^*$ in the negotiation

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A more detailed analysis can be found in our discussion paper Kessler and Lühlfdémann (2000).
game are unique and satisfy $\pi^*_2 + u^*_2 = v_2(s, g, \theta), \forall \sigma \in \Sigma$ where

$$u^*_2 = \begin{cases} \alpha v_2(\cdot) & \text{for } \alpha v_2(\cdot) \geq u^E \\ u^E & \text{otherwise,} \end{cases}$$

and

$$\pi^*_2 = \begin{cases} (1 - \alpha) v_2(\cdot) & \text{for } (1 - \alpha) v_2(\cdot) \geq \pi^E \\ \pi^E & \text{otherwise.} \end{cases}$$

Thus, worker and firm share the surplus from continued employment according to their relative bargaining power with their external market opportunities acting as an outside option, i.e., they constitute a lower bound on each party’s payoff but otherwise do not affect the outcome. This formulation is consistent with several extensive-form bargaining games that have been developed in the context of labour markets (Shaked and Sutton, 1984; MacLeod and Malcomson, 1993a, 1995). It can further be simplified by noting that $\pi^E = 0$ because competition on the external labour market ensures that the firm hiring another worker always has to pay him his full marginal product [Assumption 2]. Due to $v_2(\cdot) \geq 0$ [Assumption 1], the firm’s share of the surplus from continued employment always weakly exceeds the profit from taking up its external market opportunity. We can thus disregard the firm’s outside option in what follows and characterize the negotiation outcome in terms of the second period equilibrium wage $w^*_2$ which, using $u_2 = w_2$ and $u^E = w^E$, is given by

$$w^*_2 = \begin{cases} \alpha v_2(\cdot) & \text{for } \alpha v_2(\cdot) \geq w^E \\ w^E & \text{otherwise.} \end{cases}$$ (3)

More specifically, the unique subgame perfect equilibrium of the game studied by Shaked and Sutton (which is based on the Rubinstein bargaining game) coincides in the limit where discounting is negligible with the outcome in Assumption 3 for $\alpha = 1/2$. Arbitrary values of $\alpha$ can be introduced into the alternating-offers game by assuming that nature chooses which player makes an offer in each bargaining round with constant probability (Binmore, 1987). Using this variant of the Rubinstein game, MacLeod and Malcomson (1993a, 1995) develop a model of contract (re-)negotiation where trade occurs over time rather than at a single date, thus reflecting the long-term nature of employment relationships very well. Under our specification (and assuming that the worker strictly prefers not to work in the absence of a contract, i.e., a zero wage), the unique subgame perfect equilibrium in their model if the time interval between offers vanishes again coincides with the outcome in Assumption 3.
Two characteristics of $w^*_2$ are notable. First, the employee always receives at least his marginal product from general skills, $w^E = v^G(g, \theta)$. Second, if the worker prefers his equilibrium wage in the absence of an outside opportunity to the wage he can obtain in the external labour market, the latter does not influence the bargaining outcome (outside option principle). As the literature on non-cooperative bargaining has shown, this property will prevail if a quit (or layoff) effectively terminates the negotiations and forgoes all future gains from cooperation so that the worker cannot credibly threaten to quit in such a situation.\footnote{See, e.g., Osborne and Rubinstein (1990). Malcomson (1997) provides an extensive discussion of how market opportunities can enter the negotiation outcome and when they take the form of outside options. This point is discussed in more detail in Section 2.}

General Investments in Human Capital

Let us first investigate a situation where the firm cannot or does not invest into relationship specific skills of the worker by setting $s \equiv 0$. Because all training is then general, the employee is as valuable inside the existing relationship as on the external labour market. Hence, competition among firms ensures that the worker is paid his full marginal product $v^G(g, \theta)$, irrespective of whether the relationship is continued or the worker seeks outside employment. By (3), negotiations will lead to a second-period wage of $w^*_2 = w^E$: surplus sharing never occurs simply because there is no rent in excess of what can be obtained in the market. The firm’s second period profit is thus $\pi^*_2 = 0$ and the worker’s utility is $u^*_2 = v_2(0, g, \theta) = v^G(g, \theta)$. The expected overall returns from the relationship are then given by $E[\pi(0, g)] = v_1 - w_1 - g$ and $E[u(0, g)] = w_1 + E_\theta[v^G(g, \theta)]$, respectively. The following proposition is immediate and replicates Becker’s (1964) seminal argument.

**Proposition 1.** Suppose the firm does not invest into specific skills of the employee, i.e., $s \equiv 0$. Then, the equilibrium level of general training $g^*$ and the first period wage $w^*_1$ satisfy
a) \( g^* = 0 \) and \( w_1^* = v_1 \) if \( g \) cannot be contracted upon,

b) \( g^* = g^{FB} \), and \( w_1^* = v_1 - g^{FB} \), if \( g \) is contractible.

The employer never pays for training in general skills because he cannot recover any returns from such training in the second period. If its training expenditures are non-contractible, no general human capital investments are made in equilibrium. If \( g \) is contractible and initial contracts \((w_1, g)\) are feasible, any outlays in general training have to be borne entirely by the employee by receiving a first-period wage below his productivity. Expressed differently, if we let \( \gamma \) be the worker’s cost share and express the first-period wage as \( w_1^* = \bar{w}_1 - \gamma g \) where \( \bar{w}_1 \) is the wage component that is independent of \( g \), then \( \bar{w}_1 = v_1 \) and \( \gamma = 1 \): the worker is paid his first-period marginal product and finances the full cost of his training out of his pay. Note that the proposition implicitly requires the worker not to be liquidity constrained, e.g., he can borrow against future wage income. Otherwise, although we still had \( w_1^* = v_1 - g^* \), it may be the case that \( g^* < g^{FB} \) if the worker might not be able to finance \( g = g^{FB} \) out of his first-period pay (his productivity during the training period is sufficiently low).

1.2. Investment in General and Specific Training

We now return to the possibility of investment in the acquisition of firm-specific skills. To see how training in firm-specific skills alters equilibrium characteristics, reconsider the outcome of negotiations on second-period wage contracts. For \( s > 0 \), there is now a positive rent \( v_2(s, g, \theta) - w^E = v_2(s, g, \theta) - v^G(g, \theta) = v^S(s, \theta) > 0 \) to be divided between worker and firm. While this rent depends solely on the level of specific training \( s \), the way in which it is shared depends also on \( g \) as can be seen from (3). For \( \alpha v_2 < w^E \Leftrightarrow v^S < v^G(1 - \alpha)/\alpha \), the worker’s share of the surplus generated in the existing relationship falls short of what he can obtain on the external labour market: since his alternative market opportunity is binding, the negotiated second period wage
is $w_2^* = w^E = v^G(g, \theta)$ and the rent from specific investments $v^S(\cdot)$ accrues entirely to the firm. Conversely, the negotiated wage exceeds the outside market wage for $\alpha v_2 \geq w^E \iff v^S \geq v^G(1 - \alpha)/\alpha$. In those states, the worker captures part of the rent generated through specific human capital accumulation through his share $\alpha$ of the overall surplus. His equilibrium wage then satisfies $w_2^* > w^E = v^G(g, \theta)$. As already noted by Becker, specific training investments imply that worker and firm are in a bilateral monopoly position after those investments have been made: if the worker quits and takes on another job, the firm’s expenditures are wasted because no replacement worker would be equally proficient in the required task. Similarly, the specific skills are not marketable if the worker is laid off and he would therefore be unable to recoup any specific investments on this own part. As is well known, once worker and firm share the rent from specific investments, the ‘Hold-up Problem’ [Williamson (1985), Grout (1984)] arises and the firm will under-invest. The crucial point to recognize, however, is that the firm’s hold-up with respect to its specific investments is beneficial with respect to its incentives to invest into general skills: whenever the worker receives part of the surplus from the firm’s expenditures on specific training, the firm at the same time captures part of the return on general training.

Formally, let $\Theta(s, g) = \{\theta \in [\hat{\theta}, \bar{\theta}] : v^S(s, \theta) \geq v^G(g, \theta)(1 - \alpha)/\alpha\}$ denote the set of states in which rent sharing occurs for given investments $(s, g)$. Inserting the expression for $w_2^*$ from (3) into the firm’s expected profit from the relationship, we obtain

$$E[\pi(s, g, \theta)] = v_1 - w_1 + \int_{\theta \in \Theta(\cdot)} (1 - \alpha) [v_2(s, g, \theta)] dF(\theta)$$

$$+ \int_{\theta \notin \Theta(\cdot)} [v_2(s, g, \theta) - v^G(g, \theta)] dF(\theta) - g - s. \quad (4)$$

Suppose first $g$ is not contractible, so that the employer would not be willing to provide general training for $s \equiv 0$. If specific investments are allowed for, the firm chooses $(s, g)$
so as to maximize (4), subject to the non-negativity constraints \( g \geq 0 \) and \( s \geq 0 \). As is easily seen, the latter constraint is never binding and can be ignored. Substituting for \( v_2(s, g, \theta) = v^S(s, \theta) + v^G(g, \theta) \), the first-order conditions for \((s^*, g^*)\) are

\[
\int_{\theta \in [\theta, \overline{\theta}]} \frac{\partial v^S(s^*, \theta)}{\partial s} dF(\theta) - \alpha \int_{\theta \in \Theta(\cdot)} \frac{\partial v^S(s^*, \theta)}{\partial s} dF(\theta) = 1, \quad (5)
\]

and

\[
(1 - \alpha) \int_{\theta \in \Theta(\cdot)} \frac{\partial v^G(g^*, \theta)}{\partial g} dF(\theta) \leq 1, \quad = 1 \text{ for } g^* > 0, \quad (6)
\]

where \( \Theta(\cdot) \) is evaluated at \((s^*, g^*)\). It is straightforward to verify that \( E[\pi(s, g)] \) is concave in \((s, g)\). Equilibrium training outlays \((s^*, g^*)\) are therefore unique and fully determined by (5) and (6). Also note that small changes in training outlays that affect the set of states in which surplus-sharing occurs do not enter the first-order conditions by definition of \( \Theta(\cdot) \) and continuity of \( F(\theta) \). Hence,

**Proposition 2.** Suppose the firm can train the worker in specific and general skills and training expenditures are non-contractible. Then, its equilibrium training outlays \((s^*, g^*)\) are characterized by

a) \( s^* < s^{FB} \) and \( 0 < g^* < g^{FB} \) if \( v^S(s^{FB}, \theta) > \frac{v_2}{\alpha} \) for some realization of \( \theta \in [\theta, \overline{\theta}] \),

b) \( s^* = s^{FB} \) and \( g^* = 0 \) otherwise.

Thus, the firm invests in general training if and only if hold-up with respect to specific training occurs with positive probability.

Under our assumptions on \( v_2(\cdot) \), the claim follows directly by comparing (5) with (2) and by inspection of (6). A formal proof is therefore omitted. The intuition for this finding has already been laid out in the preceding discussion. If hold-up occurs in some states of the word, the employee captures a fraction \( \alpha \) of the surplus from the firm’s
expenditures in his acquisition of specific (as well as general) skills. At the same time, however, the firm is also able to recover part of its expenditures on general training on the margin. This is true even though rent sharing implies that the firm’s overall profit from both types of training decreases relative to a situation where the employee’s alternative market opportunity is binding. Expressed differently, the firm captures part of the return from its general training outlays although the worker always receives at least his marginal product from general training. It is important to observe that this property of our model differs from the existing literature where wages are ‘compressed’ and workers receive less than the marginal productivity associated with their general skills (See Section 2 for a discussion).

Hold-up with respect to specific investments \( s^* < s^{FB} \) can only be avoided if, given efficient specific and no general training, the external wage of a worker with no marketable skills, \( w^E = v_2 \), is sufficiently high so as to make his outside market opportunity binding in every state of the world, i.e., \( \Theta(s^{FB}, 0) = \emptyset \), or equivalently, \( v^S(s^{FB}, \theta) \leq v_2 \frac{1-\alpha}{\alpha} \) for all realizations of \( \theta \). Otherwise, however, hold-up will occur and it is optimal for the employer to provide a positive amount of general training. Finally, note that since \( s^* > 0 \), the firm expects to realize a positive second-period profit. On a competitive labour market, those future profits will be competed away by means of first-period wage payments. Formally, we have \( E[\pi(s^*, g^*, \theta)] = 0 \Rightarrow w^*_1 > v_1 \), i.e., any rents from human capital accumulation are appropriated by the worker through a rise in his first period wage.

At first glance, the statement in Proposition 2 may lead one to conclude that a firm’s investment in general human capital negatively distorts the accumulation of specific human capital relative to a situation where general training is absent, \( g \equiv 0 \). The following result asserts that this conclusion is misleading:

**Proposition 3.** The firm’s expected-profit function (4) is supermodular in \( s \) and \( g \).
Therefore, general and specific training are complementary from the firm’s point of view and its optimal investments into specific human capital \( s^*(g) \) are nondecreasing in the level of general human capital \( g \) (and vice versa).

Intuitively, employees with a high level of general training receive higher external wage offers than those with fewer or no general skills. The outside market opportunity of workers with more general training will therefore bind more frequently, ceteris paribus. Although the firm has to match the external wage in those states, it at the same time reaps the full marginal return from its specific training outlays (rent sharing does not occur) and its incentives to provide specific training rise. In other words, general training alleviates the hold-up problem.

Figure 1 illustrates the above arguments. It depicts the firm’s optimally chosen expenditures in specific training \( s^* \) (respectively, general training \( g^* \)) as a function of a given level of \( g \) (respectively, \( s \)). If the worker had no general training, the firm would provide specific training of \( s^*(0) = s_{\min} \) which solves (5), evaluated at \( \Theta(s_{\min},0) \). The specific training outlays \( s^*(g) \) increase thereafter until \( g \) is sufficiently high that surplus sharing no longer occurs so that the firm invests efficiently, independent of \( g \). Conversely, no general training would be provided if \( s = 0 \) and this continues to be optimal up to some \( s = s' \) at which point surplus sharing occurs with positive probability, i.e., \( \Theta(s,0) \) is non-empty for \( s \geq s' \). From then on, the provision of general training \( g^*(s) \) increases because the likelihood of a surplus sharing outcome increases in \( s \), ceteris paribus. If this probability is equal to one, \( g^* \) is maximal and given by \( g_{\max} < g^{FB} \) which solves (6) for \( \Theta = [\bar{\theta}, \bar{\theta}] \). The equilibrium outlays \( (s^*, g^*) \) characterized in Proposition 2 can be found at the intersection of both curves. As long as \( s_{\min} < s^{FB} \iff \Theta(s^{FB},0) \neq \emptyset \), the intersection point is characterized by \( g^* > 0 \). Otherwise, we have \( s_{\min} = s^{FB} \) which implies \( s' > s^{FB} \) by definition of \( s' \) so that the curves intersect on the axis where \( g^* = 0 \). Also note that the effect of a drop in
the worker’s bargaining power does not necessarily encourage firm-sponsored general training: a reduction in \(\alpha\) reduces the probability that surplus sharing occurs, thus shifting \(s^*(g)\) upwards. Since \(g^*(s)\) also shifts upwards by the same token, however, the composite effect is ambiguous.

[Figure 1 about here]

Let us now turn to the case where \(g\) is contractible so that the firm can offer an initial contract \((w_1, g)\). As argued above, this situation is likely to prevail if a country has an institutionalized apprenticeship system. For a precontracted level of general training \(g\), the firm’s expenditures on specific training \(s^*(g)\) are determined by (5) and its associated expected profit is (4) evaluated at \((s^*(g), g)\). Consider a first-period contract that involves \(g = g^{FB}\). From our previous analysis, we already know that the share of general training outlays borne by the worker is strictly less than one if \(\Theta(s^*(g^{FB}), g^{FB})\) is non-empty. This condition is equivalent to \(s^*(g^{FB}) < s^{FB}\) or

\[
v^S(s^{FB}, \theta) > v^G(g^{FB}, \theta) \frac{1 - \alpha}{\alpha} \quad \text{for some} \quad \theta \in [\underline{\theta}, \bar{\theta}].
\]

(7)

The argument here is essentially the same as in Proposition 2. If hold-up with respect to specific training prevails, the firm captures part of the surplus from general training and is therefore willing to bear a positive share of those expenses. In this case, though, the equilibrium contract does not prescribe a first-best amount of general training:

**Proposition 4.** Suppose the firm can train the worker in general and specific skills and the amount of general training can be contracted upon. Then, the equilibrium levels of general and specific training are strictly larger than in a scenario where \(g\) is non-contractible. If (7) holds, equilibrium training outlays satisfy \(s^* < s^{FB}\) and \(g^* > g^{FB}\). In this case, the worker does not bear the full cost of his general training. Otherwise, \((s^*, g^*) = (s^{FB}, g^{FB})\) and the worker’s share of general training expenditures is equal to one.

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The result states that not only general but also specific training will be strictly larger in a situation where general training is contractible. In Germany with its institutionalized training system, apprentices attend a state-sponsored vocational school for two days a week. Hence, the amount of general training can indeed be seen as verifiable to a large degree. Our model then predicts that, due to the incentive-complementarity of general and specific training, specific training will be larger and (in a stochastic model) job turnover rates will be lower than in countries where general training is not contractible.

Interestingly, worker and firm do not necessarily agree on the first-best level of $g$ even though such a contract is feasible. Rather, they may well decide on an inefficiently high provision of general training as is easily seen: suppose at a precontracted level $g^{FB}$, the firm’s (unilaterally chosen) expenditures in $s$ fall short of $s^{FB}$. A small increase in $g$ above $g^{FB}$ has only a second order effect on the returns to general training but improves the firm’s incentives to engage in specific training (Proposition 3). Raising $g$ thus has a positive first-order effect on the joint surplus from specific human capital accumulation and the worker optimally receives ‘too much’ general training in order to reduce a prevailing hold-up problem with respect to the firm’s specific human capital investments. Therefore, the conclusion that first-best training outlays cannot be implemented in general even if $g$ is contractible should not lead one to conclude that institutions which support such arrangements are undesirable. It is immediate from Propositions 2 and 4 that firms and workers are better off if they can agree upon a pre-specified level of general training in advance. Even if training in general skills is above the efficient amount, the incentive complementarity of both investments implies

\footnote{Again, a contract prescribing $g^* \geq g^{FB}$ may not be feasible if the employee is wealth constrained. Note, however, that the presence of specific training facilitates an agreement on $g$ because the firm’s second-period rent generated by the worker’s specific skills raises first period wages, thereby relaxing his liquidity constraint.}

\footnote{In Germany, firms sometimes complain that their apprentices spend ‘excessive’ time in vocational schools. While this claim may be justified, our model at the same time delivers a rationale of why excessive training may be optimal.}
that workers receive more training in specific skills, thereby increasing overall surplus.

Note that the above results are qualitatively unaffected if we extend the model to allow for quits and layoffs. Equilibrium labour turnover could easily be incorporated through introducing a random shock to the worker’s (or firm’s) external market opportunity. For example, the worker may learn that he dislikes his colleagues or that his spouse has found employment in another state. Alternatively, the firm may discover that the worker is unable to adapt to its corporate culture. In such a situation, the external market opportunities will then bind more often, thereby reducing the likelihood of a rent-sharing outcome. While the amount of general training that the firm is willing to provide on its own account in equilibrium will thus be lower, the general conclusions from our analysis clearly remain valid.\footnote{As has been noted by Booth and Chatterji (1998), if quits reduce firms’ incentives to invest in training unions could have a positive effect. In their model, union bargaining increases the share of rents going to trained workers, reduces quits, and causes firms to train more.}

Finally, let us briefly indicate how the above results change if it is instead the worker who decides how much to invest in his general skills, while the firm decides on how much specific training training he is to receive. First, it is immediate that the outcome remains unaffected in a situation where $g$ is contractible. Since the contractually agreed upon level of $g$ is always chosen so as to maximize joint surplus, (residual) decision rights do not matter and Proposition 4 continues to hold. Next, recall that in the absence of specific training ($s \equiv 0$), the worker receives the full marginal product from his general skills and would therefore invest efficiently even if $g$ cannot be contracted upon. Clearly, this argument carries over to the case where the firm invests in $s$ but the employee’s outside option is binding, i.e., surplus sharing never occurs. Otherwise, however, surplus sharing implies that he does not capture the full return from his investments at the margin and, as a result, under-invests. The outcome if $g$ is non-contractible and chosen by the worker thus inversely mirrors the result in Proposition 12.
3. The equilibrium level of general training is efficient if hold-up with respect to specific training does not occur with positive probability [the set $\Theta(s^{FB}, g^{FB})$ is empty] and inefficiently low (but positive) otherwise.

## 2 Discussion

In his seminal work, Becker (1964) drew the important distinction between general and specific investments in human capital. If the skills a worker acquires through on-the-job training are purely general, he argued, the wage on the external labour market will reflect the full marginal product from this training. Thus, workers capture the entire return from their general human capital in a competitive labour market. Conversely, training in perfectly specific skills has no effect on the worker’s productivity in other firms and the wage that an employee could get elsewhere would thus be independent of the amount of training he received. As a consequence, the return to specific human capital is shared between employees and firms. Becker concluded that employees must bear all the costs of their general training whereas the costs of specific training are shared between workers and firms.\(^\text{13}\) As noted earlier, however, the first prediction is at odds with empirical work on firm-sponsored formal training programs whose content is general in nature. The present framework reconciles Becker’s theory with empirical evidence in a framework that preserves its two main characteristics: a) the worker always receives the full return from general training and b) obtains a share of the return (rent) generated by specific training. The sole difference lies in the fact that we do not consider each type of human capital investment separately but rather allow for both general and specific training to be provided at the same time.\(^\text{14}\)

\(^\text{13}\) For a formal analysis on how the costs of specific investments are shared, see Hashimoto (1981).

\(^\text{14}\) Note that our model is formally equivalent to the Becker’s framework and yields identical predictions for $s \equiv 0$ and $g \equiv 0$, respectively.
possibility is taken into account, the sharp conclusion that firms should never pay for investments in general training no longer applies. Moreover, this result does not rely on general and specific skills being complements in production (or training expenditures) as the previous analysis has shown.

A body of recent research has suggested several reasons of why and under which circumstances firms may be willing to contribute to the costs of general training. One prominent explanation is based on informational asymmetries between the training firm and potential future employers.\textsuperscript{15} If the outside market is not as well informed as the current employer about a worker’s level of training or his other relevant characteristics, the worker’s general skills are no longer perfectly marketable and in essence become specific skills. An analogous line of reasoning applies if there are labour market frictions created by search or hiring costs (Acemoglu, 1997). In both cases, workers receive less than their marginal product from (general) training on average which improves firms’ investment incentives. Acemoglu and Pischke (1999) note further labour market imperfections where wages are below marginal product and rise less steeply than productivity so that the wedge between marginal product and (outside) wage is higher, the more trained a worker is.\textsuperscript{16} A similar mechanism is at work in our framework: although external wages are equal to worker’s marginal product from general training, the wage he obtains if he stays with the training firm rises by less than his overall productivity. Furthermore, the resulting gap is an increasing function of his level of specific training.

Although this property of our model is generated by the outcome of wage bargaining

\textsuperscript{15}See Katz and Zidermann (1990), Chiang and Chiang (1990), Chang and Wang (1996), and Acemoglu and Pischke (1998). For an analysis of what long-term (apprenticeship) contracts can achieve in this context, see Malcomson et al. (2003).

\textsuperscript{16}Apart from informational asymmetries, the authors study three situations where such a ‘compressed’ wage structure is likely to arise: union wage setting, minimum wages, and worker moral hazard.
as formalized in Assumption 3, it does not critically depend on the utilization of the pure outside option principle as we have already stressed in the Introduction. Implicit in this particular bargaining solution is the assumption that the default payoff each party receives in the course of bargaining is zero or, more importantly, independent of investments. In other words, the default payoffs in case of a disagreement during negotiations are unaffected by what the parties’ can obtain on the external market. On the opposite end of the spectrum is the Nash bargaining solution where the worker’s default payoff is *identical* to what he could obtain if he were to quit permanently, i.e., equal to $w^E$. Then, the gain from reaching an agreement would no longer be $v_2(s, g, \theta)$ but rather $v_2(s, g, \theta) - w^E = v^S(s, \theta)$. If the parties share this gain according to their relative bargaining powers, equilibrium payoffs would be $u^*_2 = w^E + \alpha v^S(\cdot)$ and $\pi^*_2 = (1 - \alpha) v^S(\cdot)$. As the latter is independent of $g$, the firm would have no incentive to invest in general skills. The additively separable structure of marginal products would thus be fully reflected in the worker’s post-training wage. There would be no interaction between the two types of skills and Becker’s original argument would fully carry over to a situation where both general and specific training is provided.

To assess this possibility, notice that for the employee’s threat point to be $w^E$, he must be able to take on a temporary job for one bargaining round that pays the same wage $w^E$ as a permanent job on the external labour market. Indeed, one can formalize the notions of alternative market opportunities acting a threat points (in the sense of Nash-bargaining) and as outside options as two limit cases of a non-cooperative alternating offers game. In the former case, the minimum time period for which the worker has to stick to an outside employer is one bargaining round whereas it approaches infinitely many rounds in the latter (Chiu and Yang, 1999).\footnote{In this case, the external market opportunity, if taken terminates the relationship and must be represented as an outside option. Alternatively, the distinction can be made based on search or relocation costs that are associated with finding an equally good job outside the current relationship.} As we have seen above, our
results are not valid when the employee can switch to an outside employer and return after only one round of bargaining. For all intermediate cases, however, the worker’s disagreement payoff does not rise one-to-one with his external market opportunity and our analysis continues to apply. More generally, what matters qualitatively is that negotiations do not follow exactly the Nash-solution.

On the empirical side, our approach has a number of implications that are similar to those of the existing literature. For example, since equilibrium turnover is lower the higher the level of firm-specific skills, one would expect lower turnover rates in industries where specific investments are very viable. The complementarity result in Proposition 3 then implies a negative correlation between both types of training and equilibrium turnover although low turnover rates per se do not improve a firm’s incentives to provide general training as has sometimes been suggested [Blinder and Krueger (1996)]. By the same token, since the equilibrium level of general training in our model depends (among other things) on its contractibility, the model predicts that both general and specific training are higher in countries where institutionalized training programs make the amount of general training more easily enforceable. If one reasonably presumes that this is the case for, e.g., Germany relative to the United States, our results suggest that there should also be more specific training and, hence, lower turnover rates in Germany than in the United States. Finally, surplus sharing implies that the post-training wage increases by less than a worker’s productivity.

All those predictions are supported by the data: the positive correlation between general training and retention rates is reported, e.g., in Blinder and Krueger (1986). Topel and Ward (1992) and Soskice (1994) find that the average number of jobs held by US
employees during the first ten years of their career is about five, but only one or two in Germany. Blanchflower, Oswald and Sanfrey (1996) find that an increase in profit per worker raises wages only at a rate of at most 0.3 and Loewenstein and Spletzer (1999) estimate that a worker’s return on employer-sponsored specific and general training is very similar, suggesting that surplus-sharing between firm and employer is prevalent. Although these observations stand in contrast to the classical theory (where turnover should be independent of the level of general training and wages should grow at the same rate as productivity), they are also consistent with, e.g., models that rely on informational asymmetries to explain firm-sponsored general training. We therefore next discuss some empirical regularities that are difficult to reconcile with the existing literature but may be accounted for by the interaction of general and specific training.

First, supporting evidence for the present model may lie in the significant differences in training expenses across sectors of the German economy. Franz and Soskice (1995) estimate the average yearly net training cost per apprentice at about DM 15000 in the industrial sector which largely consists of medium and large scale enterprises, and at only about DM 7000 per worker in the crafts and artisan sector (“Handwerk”). Similar results are found in von Bardeleben, Beicht and Feher (1995) who estimate that large firms with more than 500 employees have positive net training costs of about DM 7500 per employee, while the costs for the smallest firms with less than 10 employees (usually from the Handwerk sector) are close to zero or may even be negative.

Asymmetric information is certainly a relevant phenomenon, although perhaps less so in countries with formal training programs like Germany where apprentices receive upon completion a nation-wide accepted certificate which acknowledges their skill and overall training success. The certificate should reduce uncertainty in particular with respect to the amount of training received. In contrast, the unknown characteristic in Acemoglu and Pischke (1998) is the ability of the apprentice of which standardized exams may provide only a very noisy signal. Also, their empirical test supports the presence of adverse selection, because the salaries of employees that leave because they are drafted to the military (quits caused by exogenous reasons) are significantly higher that the salaries of those that either leave voluntarily or have been laid off. Our model cannot adequately account for these differences, which emphasizes the importance of adverse selection phenomena as a complementary explanation for the prevalence of general training.

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These patterns are somewhat surprising because the formal structure of apprenticeship programs in the two sectors is more or less the same, and it is not immediate why informational asymmetries or search costs should systematically differ between industrial and crafts sector. However, it seems quite plausible that firm-specific training is of considerable importance in large enterprises which are characterized by complex internal structures. In fact, Franz and Soskice (1995, p.220) note that “[...] in Germany, the requirements of a skilled worker (in the industrial sector) have radically changed. By contrast to the traditional craftsman or to a tradesman in a Fordist company who had a set of standardized skills which they could use in many different environments, the modern skilled employee plays a complex interactive role in the production, maintenance, organization of new processes, and so on.” In light of our findings, the differences in employer-sponsored training between the industrial and the crafts sector of the German economy may thus be traced back to the differences in the viability of specific training. This view is confirmed by the observation that retention rates after the completion of the apprenticeship program vary significantly with firm size: Soskice (1994) reports that the retention rates in small German firms with 5-9 employees are about 0.56, while they increase in firm size and reach a rate of 0.87 for companies with more than 1000 employees. This sample also exhibits a relation between the employer’s willingness to invest in general training and firm size: while about 41% of firms of less than 50 employees (and even 65% of firms with 5-9 workers) do not participate in formal training programs which are general to a large degree, the fraction of non-training firms continuously shrinks and becomes negligible for firms with more than 500 employees. This finding is in line with our theoretical results, where a high relevance of specific training leads not only to low turnover rates, but goes hand in hand with a more pronounced provision of firm-sponsored general training.

Second, the model predicts the usage of breach penalties as an instrument for firms to
protect their training outlays. To see this, suppose the employment contract includes a penalty that the worker must pay the firm if he or she quits and switches to an outside employer after the training period. Obviously, a sufficiently high fine will prevent the worker from taking up outside employment and the firm would obtain the full return from its investments on the margin.\textsuperscript{19} It is important to note, however, that this straightforward argument hinges on the presumption that bargaining at least in part follows the outside option principle. Breach penalty cannot be effective if external market opportunities act as threat points rather than outside options: although they drive a wedge between a worker’s marginal product and his outside market opportunities, the difference is independent of the amount of training received and, hence, penalty payments should have no effect on a firm’s incentive to train, irrespective of whether or not further market imperfections are present. Breach clauses are frequently subject to legal restrictions. Nevertheless, they exist in reality. One example is the German revenue service which trains students in a three-year trainee program who later serve as tax officials. If graduates quit the service within five years after completion of the program, they are subject to a breach penalty of about DM 25000. Similar clauses are used by German mining companies that provide advanced training programs in engineering. Also observe that the use of vested stock as part of an employee’s compensation package may serve as a substitute for explicit breach penalties if those are difficult to enforce.\textsuperscript{20}

Finally, our analysis can account for the fact that employers frequently sponsor general training of their employees only simultaneously with or after a period of in-house training.\textsuperscript{21} If in-house training is partly relationship-specific, it may take some time until

\textsuperscript{19}The usage of breach penalties requires long-term employment contracts that extend beyond the training period. For a more detailed analysis of what can be achieved with long-term contracts and penalties, see our discussion paper Kessler and Lülfesmann (2000).

\textsuperscript{20}We thank George Baker for pointing this out to us.

\textsuperscript{21}Yu (1999) conducts a survey of evening MBA students at the HAAS business school at UC Berke-
a worker’s specific skills generate sufficient additional surplus until his outside wage falls short of the negotiated equilibrium wage inside the current relationship which is a prerequisite for general training to be viable. Expressed differently, if general investments would be provided prior to the specific training, outside employers could poach the worker upon completion of the general training period, and then train him in firm-specific skills themselves. The firm then recovers no return from general investments in the first period, and would rationally postpone its participation in general training until a sufficient level of specific human capital has been accumulated.

3 Concluding Remarks

This paper has studied a situation where the firm can invest in general as well as firm-specific human capital of its employees. Our main result was that these types of investments interact even if no technological link exists. Specifically, specific training not only renders the provision of general training viable for an employer, but the reverse also holds: the higher the level of a worker’s general human capital, the larger are the firm’s incentives to train him in specific skills. The finding therefore indicates that specific and general training are ‘incentive’ complements from the employer’s point of view. As a consequence, employers may be willing to sponsor general training even in competitive labour markets where outside wages fully reflect a worker’s marginal

\[ \text{ley. About 80\% of the students had partial to full tuition (which amounts to $19,000-$24,000 annually) paid for by the companies for which they work. He finds that the number of years an employee had worked for the company (as a proxy for the amount of firm-specific training the worker has acquired) has a significant positive impact on the percentage of firm-sponsored education. Likewise, large consulting firms such as McKinsey and Co. generally offer employees with two of more years of job tenure the possibility to take a paid leave in order to participate in MBA programs or complete their doctoral degrees. Importantly, the corresponding contract is signed at the beginning of the employment relationship, i.e., at a time where the company presumably has no more information on the employee’s ability than other firms. Of course, such offers may also serve as screening devices in recruitment. This alternative explanation, however, cannot account for the the contractually specified time sequence.} \]
product from his general human capital.

We have argued that there is not only evidence that firms sponsor general human capital accumulation of their workers, but also evidence that suggests the complementarity in the provision of general and specific training. Whether this complementarity can mainly be attributed to technological reasons or to the interaction we posit in the present paper is an empirical question which future research needs to address. We should emphasize, though, that our model does not preclude the possibility of a technological link between both types of training, be it on the output or on the cost side of production. The positive incentive effect that we have isolated in our analysis should be present irrespective of whether general and specific training are technological complements or substitutes.
Appendix

Proof of Proposition 3

By definition, $E[\pi(s,g)]$ is supermodular in $(s,g)$ if and only if $\partial E[\pi(s,g')]/\partial s \geq \partial E[\pi(s,g)]/\partial s$ for all $s$ and $g' > g$. Using (5), this condition is equivalent to

$$g' > g \Rightarrow \int_{\theta \in \Theta'} \frac{\partial v^S(s^*,\theta)}{\partial s} dF(\theta) \leq \int_{\theta \in \Theta} \frac{\partial v^S(s^*,\theta)}{\partial s} dF(\theta), \quad \forall s,$$

where $\Theta' \equiv \Theta(s,g')$ and $\Theta \equiv \Theta(s,g)$. Since $g' > g \Rightarrow v^G(g',\theta) > v^G(g,\theta)$ for all values of $\theta$, we have $\theta \in \Theta' \Rightarrow \theta \in \Theta \equiv \Theta' \subseteq \Theta$, which together with $\partial v^S(s^*,\theta)/\partial s > 0$ implies (8). Also observe that the inequality in (8) is strict whenever either $\Theta \neq \emptyset$ or $\Theta' \neq \emptyset$, so we have $\Theta(s,g') = \emptyset \Rightarrow g^* > g^F$.  

Proof of Proposition 4

The equilibrium contract $(w^*_1, g^*)$ when $g$ is contractible maximizes expected surplus $S(g,s) \equiv E_{\theta} [v_2(s,g,\theta)] + \underline{v}_1 - s - g$ subject to $s = s^*(g)$ and $E[\pi(s,g)] \geq 0$.

Suppose first by way of contradiction that (7) is satisfied but $g^* < g^F$. Now consider a contract $g' = g^* + dg$ with $dg > 0$. Using (5), the change in expected surplus for $dg$ small is

$$dS = \left[ \int_{\theta} \frac{\partial v^G(g',\theta)}{\partial g} dF(\theta) - 1 \right] dg + \alpha \int_{\theta \in \Theta} \frac{\partial v^S(s^*,\theta)}{\partial s} dF(\theta) \frac{\partial s^*(g)}{\partial g} dg.$$

Note that by (2), the first term in brackets is non-negative for any $g^* \leq g^F$. Likewise, under condition (7), $\Theta(s^F,g^*)$ is non-empty for any $g^* \leq g^F$. (5) then implies $s^*(g^*) < s^F$, so that the second term is strictly positive. Furthermore, $\partial s^*/\partial g > 0$ for $\Theta(s^*(g),g) \neq \emptyset \Rightarrow s^* < s^F$ from the proof of Proposition 3. Thus, $dS > 0$, contradicting our presumption that $g^* < g^F$ is part of an equilibrium contract (an analogous argument can be applied to show that we must have $s^* < s^F$ in equilibrium).

If we decompose $w_1 = \bar{w}_1 - \gamma g$ again, we find using (1) and (4),

$$\bar{w}_1 = \underline{v}_1 + \int_{\theta \in \Theta} v^S(s^*(g),\theta)dF(\theta) - \alpha \int_{\theta \in \Theta} v^S(s^*(g),\theta)dF(\theta) - s^*(g) > \underline{v}_1$$

and

$$\gamma = 1 - (1 - \alpha) \int_{\theta \in \Theta} [v^G(g,\theta)] dF(\theta)/g. \tag{9}$$

The corresponding value of $\gamma$ can be obtained by evaluating (9) at $g^*$. Since $\Theta(s^*,g^*)$ is non-empty, we have $\gamma < 1$.

Finally, suppose (7) is not satisfied, i.e., $\Theta(s^F, g^F) = \emptyset$. Together with (5), this implies $s^*(g^F) = s^F$. Hence, the level of general training that maximizes $S(s,g)$ subject to $s = s^*(g)$ is equal to $g^F$. The claim $\gamma = 1$ follows immediately from (9) and $\Theta(s^F, g^F) = \emptyset$ which completes the proof. \hfill \Box
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