

## Solutions to Midterm Exam

### Part I

Qn.	Answer	Reference Page
1.	b.	175
2.	c.	187
3.	b.	95
4.	b.	
5.	a.	113
6.	c.	123
7.	c.	123
8.	b.	129
9.	c.	
10.	d.	142
11.	c.	154
12.	c.	142
13.	a.	161
14.	d.	162-164
15.	c.	155-157
16.	a.	182
17.	b.	182
18.	b.	195
19.	c.	207
20.	a.	213
21.	c.	191
22.	d.	200
23.	a.	214
24.	d.	219
25.	b.	219

### Part II

1. (a).  $Q_y = 19 - 2Q_x$ .

(b). In equilibrium,  $\frac{MU_x}{MU_y} = \frac{P_x}{P_y}$ ,

or

$$\frac{1-2Q_x-Q_y}{8-2Q_y-Q_x} = 2.$$

Solving,  $Q_x^* = 5$ ,  $Q_y^* = 7$ .

(c). Assumptions of nonsatiation, rationality.

4. (a). In equilibrium,  $\frac{MU_x}{MU_y} = \frac{P_x}{P_y}$ , or  $\frac{MU_x}{MU_y} = 2$ . This is true at the following quantities:

x = 1; y = 4.  
x = 2; y = 5.  
x = 3; y = 6.  
x = 4; y = 7.  
x = 5; y = 8.

The budget constraint is satisfied only at the bundle (3, 6).

(b). At (3,6),  $MU_x/MU_y = P_x/P_y$ , and  $2(3) + 1(6) = 12$ .

(c). To find the overall utility, add the marginal utilities of the first three units of x and the first six units of y. This is equal to 93.

5.(a). The  $AP$  is given by  $AP = k_1x_1 - k_2x_1^2$ . To find max  $AP$  we set the derivative of  $AP$  with respect to  $x_1$  zero, and solve for  $x_1$ .  $AP$  reaches a maximum at  $x_1 = k_1/2k_2$ .

(b). The  $MP$  is given by  $MP = 2k_1x_1 - 3k_2x_1^2$ . To find the max  $AP$  we set the derivative of  $MP$  with respect to  $x_1$  zero, and solve for  $x_1$ .  $MP$  reaches a maximum at  $x_1 = k_1/3k_2$ .

(c). Since  $x_1, k_1, k_2 > 0$ ,  $k_1/3k_2 < k_1/2k_2$ . Therefore,  $MP$  reaches its maximum at a smaller input of  $x_1$  than  $AP$ .