Data mining of smart meters for load category based disaggregation of residential power consumption

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H I G H L I G H T S

• A disaggregational algorithm is proposed to identify load categories by power factors.
• A top-down unsupervised structure is proposed to learn and model load signatures.
• Hourly active and reactive power consumptions are disaggregated into categories.
• The proposed solution applies to general households on single-house and block levels.
• The algorithm could achieve over 80% accuracy for major load categories.

A R T I C L E I N F O

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A B S T R A C T

Non-Intrusive Load Monitoring (NILM) techniques have been leveraged by new instrument and machine learning algorithms to provide customers the breakdown of their energy usage. The state-of-art indicates a large amount of high-frequency measurement (> 1 Hz) can lead to accurate disaggregation. This paper, however, proposes a disaggregation algorithm relies on hourly smart meter readings, aiming to extend the application of the low-frequency data that is accessible by both utilities and customers. The output of the disaggregation includes the breakdown of energy into load-category-based components that have different average power factors. The disaggregated data will support small-scale planning, e.g., in microgrid, by revealing the variance and patterns in different load categories. Our approach is built on a top-down structure that requires no prior knowledge or general models of individual loads. Using clustering and optimization techniques, we infer the load signatures of each category based on the active and reactive power from smart meters. The signatures are updated periodically using the most recent smart meter data. The results show that our disaggregation approach could be applied to random houses in different seasons and to single house and small neighborhood in both offline and quasi-real-time context.

1. Introduction

The Non-Intrusive Load Monitoring (NILM) of residential electric loads provides new opportunities for energy efficiency

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effective [10–12], they typically require a large amount of training data measured at less than 15-min frequency, and the accuracy may decay as the number of appliances increases [11]. Also, as pointed in [13], the HMM approach is not compatible with DR programs due to its dependency on uncontrolled load patterns. Nevertheless, most existing disaggregation approaches attempt to solve the disaggregation problem at the individual load level which appeals to either high-frequency measurement or machine-learning models trained by large amount of data. Extra devices other than smart meters or upgrades of infrastructure are most likely needed to meet the signature requirement [8,14]. As a result, most disaggregation approaches are mainly customer oriented, whereas fewer studies have been focusing on the utility side. Moreover, the privacy of customers is also a major concern in term of information sharing among utilities, customers, and third-party disaggregation vendors [15].

This paper studies the disaggregation problem from the utility’s perspective, where the target loads in a household are not known in advance, and smart meters are the only available sensors. The disaggregation algorithm for utilities needs to be adaptive to general households, to work with low-frequency measurement, and not to violate customer privacy. Although smart meters are capable of high-frequency measurement (<15-min), useful information could still be retrieved at low frequency with existing Advanced Metering Infrastructure (AMI). In fact, utilities such as BC Hydro only collect hourly electricity usage data [16]. This is due to government regulation that protects customer privacy.

The disaggregation granularity in this paper is enlarged to load categories that group end-uses with comparable power factors (PFs). The purposes of PF categories are to:

- Identify load categories that are recognizable across general households in an unsupervised context with available data (active and reactive power).
- Disaggregate to a low-frequency compatible aggregation level, instead of to individual load level, to satisfy the low-frequency constraint faced by certain utilities.
- Avoid inferring appliance-level information which may expose customers’ privacy.
- Analyze the variance and patterns in different load categories featured by power factors.

The proposed algorithm first infers the signatures of potential load categories based on hourly aggregate active (P) and reactive power (Q) measured by real-world smart meters. The algorithm then separates each load category in each hour through the weighted least squares (WLS) method constrained by the inferred signatures. The outcome includes the separation of meter readings into sub-readings of high, medium, and low power factor load categories. Utilities could use the results in:

- Analyzing load variance in different categories on various aggregation levels (single house or neighborhood).
- Scrutinizing loads that affect the power quality.
- Infer emerging loads that are critical to infrastructure planning, e.g. electric vehicle (EV) charging.
- Planning for power supply, power factor (PF) correction, residential DR, and Volt-VAR control.

These benefits are particularly useful in small scales such as microgrid, in which traditional planning methods may under-perform with less averaged data and more abrupt variance seen in small scales.

The remainder of the paper is organized as follows. Section 2 briefly reviews related works. Section 3 provides the theoretical analysis of the overall algorithm. Section 4 analyzes the disaggregation results. Section 5 summarizes the paper.
3. Description of the method

3.1. Problem overview

The disaggregation of active power (P) and reactive power (Q) could be described generally in (1) as an under-determined linear system finding the consumption and power angle of each load category, given only the aggregate consumption of all the loads at time \( t \).

\[
P(t) = \sum_{i=1}^{N} x_i(t) + \epsilon_P, \quad \text{for} \ x_i(t) \in [x_i^{\min}, x_i^{\max}],
\]

\[
Q(t) = \sum_{i=1}^{N} x_i(t) \tan(\theta_i) + \epsilon_Q,
\]

where \( x_i(t) \) is the real power (source signal) of the \( i \)th load category at time \( t \); \( \theta_i \) is the typical power angle of the load category; \( N \) is the number of load categories; \( \epsilon_P \) and \( \epsilon_Q \) are the errors; and \( x_i^{\min} \) and \( x_i^{\max} \) are the lower and upper bound of \( x_i(t) \).

Unlike the typical bottom-up approach that uses fixed bases as source signals and finds the activation matrix that recovers the measurement \( P(t) \), we define \( x_i(t) \) in (1) as the base of the \( i \)th load category with varying magnitude in \([x_i^{\min}, x_i^{\max}]\).

Neglecting the error terms in (1), we separate (1) in \( \mathbb{R}^{NT} \) into a sub problem in \( \mathbb{R}^{N} \) and another in \( \mathbb{R}^{NT} \), where \( T \) is the length of the disaggregation window. The problem in \( \mathbb{R}^{N} \) infers \( \theta_i \) prior to the new disaggregation in \( \mathbb{R}^{NT} \). The structure of our disaggregation approach is illustrated in Fig. 1. The hourly power data and timestamps in this paper are available through utility meters. The load signature inference step generates signatures of potential load categories based on historical P–Q data. The disaggregation step then separates each category by the parallel matching of P and Q. The disaggregation results are able to readjust the signatures through the feedback in Fig. 1.

3.2. Load categories from clustering

Load categories in this paper are defined as the clusters of loads that exhibit similar power factors. Fig. 2 shows a clustered P–Q scatter plot of the data from a real-world smart meter. We infer the power angle and power range that best represent each cluster as signatures, and use these signatures in the disaggregation step.

The agglomerative clustering method with weighted-average linkages is used to create clusters with various sizes. The size of the cluster here means the ‘weight’ of each cluster, i.e. the number of data points and their magnitude.

3.3. Load signature inference

The idea of load signature inference from aggregate P & Q comes from the observation of the hourly smart meter data (Fig. 3). For different dwell and heating types, the scatters of hourly P–Q form linear patterns in radial directions. Based on this observation, an important assumption in this paper is made as that each individual load, regardless of multi-state or single-state, has a fixed power factor (PF) over one-hour periods. Hence, if a radial line in Fig. 3 represents the true consumption of a single load and the average consumption of the load in each operation cycle is consistent, the variance along the line will indicate its ON duration (e.g. lighting).

However, each radial line may not represent an individual load because of the aggregation effect (e.g. multiple loads turned on at the same time). In this case, each radial line in Fig. 3, if regarded as vector, is the addition of multiple load vectors. Goncalves et al. use a matching pursuit approach to synthesize component vectors and find matching on–off events to validate the synthesis [22]. However, because each load may have various active states over one hour (due to active duration or multiple states), vector synthesis with matching pursuit will yield a large number of ON–OFF matches without correct labeling. Therefore, within the 1-hour time frame, it is challenging to find signatures at single-load level, or to represent a load by a state model without prior knowledge.

The solution in this paper is to apply clustering on the aggregate data regarding the power angles, which allows us to represent each load cluster as:

\[
\hat{\nu}_i = \hat{P}_i \hat{\theta}_i,
\]

where vector \( \hat{\nu}_i \) is the signature vector of the \( i \)th cluster with inferred typical power angle \( \hat{\theta}_i \) and active power \( \hat{P}_i \in [0, \hat{P}_i^{\max}] \), for a maximum possible active power, \( \hat{P}_i^{\max} \).

The signature vector, \( \hat{\nu}_i \), represents the typical power characteristics of the cluster. In disaggregation, \( \hat{\theta}_i \) is fixed while \( \hat{P}_i \)
is allowed to vary in range. Eq. (2) relies on the assumption that the PF of each cluster averages to a constant in the hourly context. Section 3.3.1 explains how to derive $\hat{\theta}_i$ for each cluster. Section 3.3.2 describes how to derive $P_i$. Sections 3.3.1 and 3.3.2 combined derive the signature vector in (2) which will be used in disaggregation in Section 3.4.

3.3.1. Inferring power angles

The challenge of finding the typical angle of a cluster of loads is the interference from other clusters due to the aggregation effect. If each cluster is represented by a signature vector and we are given the addition results of all the vectors, then our goal is to resolve the addition and recover $\hat{\theta}_i$. In this paper, an optimization-based method of resolving vector addition is applied to find $\hat{\theta}_i$ in (3). The symbols in (3) are explained in Table 1 and (4). The problem in (3) mainly depends on the constraints to shrink the search space.

Note that (3)–(4) generally apply to less than three load clusters. For more clusters, (3)–(4) need to be adjusted. Nevertheless, disaggregation into more than three clusters may not apply to residential context with smaller power factor range (e.g. 0.90–0.99). More clusters will cause sparsity in cluster and effectively lead to disaggregating single loads instead of groups. For example, if a cluster has a range of 0.93–0.95, only several or even no load will fall into this category.

\[
\text{min} : \quad J(\hat{\theta}) = (\hat{\theta} - \hat{\theta})^2, \\
\text{s.t. :} \quad lb_i < \hat{\theta}_i < ub_i, \\
SR \theta = \hat{\theta}, \\
\hat{\theta}_{i+1} - \hat{\theta}_i \geq \hat{\theta}_{i+1} - \hat{\theta}_i, \\
\begin{cases} 
|lb_\theta| < |\theta_\theta| < |ub_\theta| & \text{if } W_{\text{low}} > W_{\text{high}} \\
0 < |\theta_\theta| - |\theta_\theta| < |ub_\theta| & \text{if } W_{\text{low}} \leq W_{\text{high}}, 
\end{cases} \\
\hat{\theta} = \arctan(\hat{Q}/\hat{P}), \\
\hat{\theta} = \sum_{i=1}^n \arctan(q/p)/n, \\
\hat{Q}_i = \frac{N}{i=1} Q_i, \quad \hat{P}_i = \frac{N}{i=1} P_i, \\
Q_i = P_i \tan(\hat{\theta}_i), \quad P_i = L_i W_i, \\
L_i = \frac{n_i}{i=1} P_i^{(k)}/n_i, \\
|\theta_\theta| = \left(\sum_{i=1}^N \theta_i^2\right)^{1/2}, \\
lb_\theta \in [lb_\theta - |\theta_\theta|, 0), \quad ub_\theta \in (0, |ub_\theta| - |\theta_\theta|].
\]

The concept of blindly resolving vector additions is based on the estimation of the mean active (turn-on) power, $L_i \in L$, and the weight, $W_i \in W$, of each cluster. The objective is to find $L$ and $W$ that generate the weighted-summed angle, $\hat{\theta}$, of all the clusters close to the direct observation, $\hat{\theta}$, from the aggregate P–Q data (3a). Eq. (3i), based on $L$ and $W$, shows the P–Q components of each cluster in $\hat{\theta}$. The problem in (3a) could also be described in (3c) as finding the rotational matrix $R$ that rotates the inferred vector, $\hat{\theta}$, to the observed vector, $\hat{\theta}$ about an arbitrary axis through origin in a Cartesian coordinate system formed by the power angle of each cluster, subject to a uniform scaling defined by $S$ (Fig. 4). $R$ can be derived from (4) given in Box I. Based on our test data, the diagonal entries of $SR$ are typically larger than 0.95, so 0.95($\hat{\theta}_{i+1} - \hat{\theta}_i$) $\geq$ $\hat{\theta}_{i+1} - \hat{\theta}_i$. A more conservative constraint would be (3d).

Constraint (3e) denotes that if the low-PF clusters have less weight, $\hat{\theta}$ will be longer than $\theta_\theta$ due to the square in (3k) and that $\hat{\theta}_{\text{low}} > \hat{\theta}_{\text{low}}$, and vice versa. $lb_\theta$ and $ub_\theta$ in (3l) belong to discrete sets of possible values dependent on the angle boundaries from clustering. The minimum value of $lb_\theta$ depends on the lower bound angle of each cluster, $lb_\theta$, in (3b). Similarly the maximum value of $ub_\theta$ depends on each $ub_\theta$. In a high-level loop, $lb_\theta$ or $ub_\theta$ is incremented in the range in (3l) until $\hat{\theta}$ is solved. For each step in the loop over $lb_\theta$ or $ub_\theta$, $\hat{\theta}$ is solved multiple times in a nested iteration. The high-level loop over $lb_\theta$ or $ub_\theta$ breaks when at least two $\hat{\theta}$ converge at the same time (changes in two $\hat{\theta}$ reduce close to
\[ R = \begin{bmatrix} u_x^2 (1 - \cos \phi) + \cos \phi & u_x u_y (1 - \cos \phi) - u_z \sin \phi & u_x u_z (1 - \cos \phi) + u_y \sin \phi \\ u_y u_x (1 - \cos \phi) + u_z \sin \phi & u_y^2 (1 - \cos \phi) + \cos \phi & u_y u_z (1 - \cos \phi) - u_x \sin \phi \\ u_z u_x (1 - \cos \phi) - u_y \sin \phi & u_z u_y (1 - \cos \phi) + u_x \sin \phi & u_z^2 (1 - \cos \phi) + \cos \phi \end{bmatrix}, \]  

(4a)

where:

\[ \bar{r} = (u_x, u_y, u_z) = \hat{\theta} \times \bar{\theta}, \]

(4b)

\[ \phi = \arccos \left( \frac{\hat{\theta} \cdot \bar{\theta}}{|\hat{\theta}| \cdot |\bar{\theta}|} \right). \]  

(4c)

Box I.

---

**Table 1**  
Notation for symbols in (3).

<table>
<thead>
<tr>
<th>Variables &amp; dependents</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \hat{\theta}_i )</td>
<td>Inferred average power angle of the ( i )th cluster</td>
</tr>
<tr>
<td>( \hat{\Theta} )</td>
<td>Inferred average power angle of all loads in a house</td>
</tr>
<tr>
<td>( R )</td>
<td>Rotation matrix in 3D about arbitrary axis through the origin</td>
</tr>
<tr>
<td>( \hat{\theta} )</td>
<td>((\hat{\theta}_1, \hat{\theta}_2, \ldots)) as the inferred power angles of each cluster</td>
</tr>
<tr>
<td>( \bar{v}_\theta )</td>
<td>Vector in the coordinate system formed by ( \hat{\theta} )</td>
</tr>
<tr>
<td>( \bar{Q} )</td>
<td>Inferred reactive power of all loads in a house</td>
</tr>
<tr>
<td>( lb )</td>
<td>Lower bound of the inferred power angle of the ( i )th cluster (derived as cluster boundaries in Fig. 2)</td>
</tr>
<tr>
<td>( ub )</td>
<td>Upper bound of the ( i )th cluster</td>
</tr>
<tr>
<td>( \bar{\theta} )</td>
<td>The mean power angle of all loads from the aggregate P–Q data</td>
</tr>
<tr>
<td>( S )</td>
<td>Scaling matrix in 3D</td>
</tr>
<tr>
<td>( \bar{\theta} )</td>
<td>((\bar{\theta}_1, \bar{\theta}_2, \ldots)) as the observed (mean) power angles of each cluster</td>
</tr>
<tr>
<td>( lb_v )</td>
<td>Lower bound of the vector length difference</td>
</tr>
<tr>
<td>( ub_v )</td>
<td>Upper bound of the vector length difference</td>
</tr>
<tr>
<td>( \bar{v}_\theta )</td>
<td>Vector in the coordinate system formed by ( \bar{\theta} )</td>
</tr>
<tr>
<td>(</td>
<td>\cdot</td>
</tr>
<tr>
<td>( W_{low} )</td>
<td>Weight of low-PF clusters</td>
</tr>
<tr>
<td>( W_{high} )</td>
<td>Weight of high-PF clusters</td>
</tr>
<tr>
<td>( \bar{P} )</td>
<td>Inferred active power of all loads in a house</td>
</tr>
<tr>
<td>( n )</td>
<td>Total number of P–Q data points</td>
</tr>
<tr>
<td>( q )</td>
<td>Reactive component of a single P–Q point</td>
</tr>
<tr>
<td>( p )</td>
<td>Active component of a single P–Q point</td>
</tr>
<tr>
<td>( N )</td>
<td>Number of load clusters</td>
</tr>
<tr>
<td>( Q_i )</td>
<td>Reactive power of the signature for the ( i )th cluster</td>
</tr>
<tr>
<td>( L_i )</td>
<td>Power base denoting the active power of the ( i )th cluster</td>
</tr>
<tr>
<td>( W_i )</td>
<td>Weight of the ( i )th cluster, considering only the active states of the cluster</td>
</tr>
<tr>
<td>( P_i )</td>
<td>Active power of the signature for the ( i )th cluster considering the weight</td>
</tr>
<tr>
<td>( n_i )</td>
<td>Number of P–Q points in the ( i )th cluster</td>
</tr>
<tr>
<td>( P_k^{(i)} )</td>
<td>Active power of the ( k )th P–Q point in the ( i )th cluster</td>
</tr>
<tr>
<td>( lb )</td>
<td>((lb_1, \ldots, lb_N)) as the lower boundaries of clusters (e.g. Fig. 2)</td>
</tr>
<tr>
<td>( ub )</td>
<td>((ub_1, \ldots, ub_N)) as the upper boundaries of clusters</td>
</tr>
</tbody>
</table>

---

zero), that is, the loop finds the interval that contains the solution for \( \hat{\theta} \). For demonstration purposes, we choose the convergence of two \( \hat{\theta}_i \) instead of all to avoid lengthy iterations. One of the future works would be refining the initial value of \( lb_\theta \) or \( ub_\theta \) for faster
convergence. Because of nonlinearity and non-convexity, (3) is solved multiple times for each value of \( lb_\theta \) or \( ub_\theta \). As a result, the overall calculation speed depends on the selected range of \( lb_\theta \) or \( ub_\theta \) and the number of iterations for each value in \( lb_\theta \) or \( ub_\theta \). Fig. 5 illustrates the overall flow of finding the power angles.

3.3.2. Power magnitude

This section aims to find the upper bound, \( \hat{P}_i^{\max} \), of \( \hat{P}_i \) in (2). Our estimator is based on a PF filter, an addition filter, and statistical analysis. The two filters reduce the aggregation effect caused by simultaneous load events.

The PF filter is based on the hourly average PF of the whole house. It locates separate time frames \( T_i \), for high-, medium-, and low-PF periods (Fig. 6) based on the boundaries from clustering. Each \( T_i \) corresponds to the period when the aggregate PF falls into the range of a cluster. For each load cluster identified in, e.g., Fig. 2, only the data points that are within the corresponding \( T_i \) are preserved. The preserved points are more likely to contain true data points from the corresponding cluster, thus the following statistical analysis will be less affected by the aggregation effect.

The addition filter further removes points in the medium-PF cluster that are close to the sum of the points from the high-PF and low-PF clusters (5). That is,

\[
\text{remove} : \quad v_j : \begin{cases} 
    d(v_j, v_i + v_k) \leq \delta \\
    d(v_j, v_i + v_j + v_k) \leq \delta
\end{cases} \tag{5}
\]

where \( d(\cdot, \cdot) \) is the Euclidean distance operator, \( v_j = (p_j, q_j) \) is any P-Q point in the medium-PF cluster, \( i, j, \) and \( k \) represent the high-, medium-, and low-PF cluster, and \( \delta \) is the cut-out threshold.

The remaining points that pass the two filters are used in the final statistical analysis. At hourly frequency, each load cluster typically shows a Gamma distribution with a single peak (e.g. low-PF cluster in Fig. 7). If a large load exists, two or more peaks may be possible or the peak may be located at a large P (e.g. high and medium-PF clusters in Fig. 7). In this case, the peak with higher P represents \( \hat{P}_i^{\max} \) of the cluster. Points with higher P than \( \hat{P}_i^{\max} \) are possible results of aggregation effect. If the disaggregation result of each cluster show different peak power, \( \hat{P}_i^{\max} \) will be updated (input \( d \) in Fig. 1).

3.4. Load disaggregation

3.4.1. Formulation

Since the disaggregation granularity is reduced to load clusters instead of individual loads, the disaggregation problem could be simplified as a weighted least square (WLS) problem in (6).

\[
\begin{align*}
\text{min} & : & f(x_i) = E_i^2 + E_q^2, & \forall t, \tag{6a} \\
E_p & = P - \hat{P}, & \tag{6b} \\
\hat{P} & = \sum_{i=1}^{N} w_i x_i, & \tag{6c} \\
E_q & = Q - \hat{Q}, & \tag{6d} \\
\hat{Q} & = \sum_{i=1}^{N} w_i x_i \tan(\hat{\theta}_i), & \tag{6e} \\
& \text{s.t.} & 0 \leq x_i \leq \hat{P}_i^{\max}, & \tag{6f}
\end{align*}
\]

where \( E_p \) and \( E_q \) denotes the error in matching the aggregate active and reactive power at time \( t \), respectively. \( P \) and \( \hat{P} \) are the actual and inferred aggregate active power at \( t \). \( w_i \in w \) is the weight of the \( i \)-th cluster at \( t \). \( x_i \) is the active power of the \( i \)-th cluster at \( t \). \( N \) is the number of clusters. \( Q \) and \( \hat{Q} \) are the actual and inferred aggregate reactive power at \( t \).

3.4.2. Finding the weights

The main error in (6) is that a false active detection of a cluster will lead to inaccurate active states of other clusters while the aggregate power is still equal to the aggregate measurement. False active detection refers to a load is not turned on but the solver mistakenly computes that it is on. The weights \( w \) provide a supervisory solution to this problem. We estimate \( w \) based on:

- the sparsity of a cluster,
- the possible activation threshold of the \( i \)-th cluster (\( a_i \in \mathbb{R}^N \) [kW]),
- the aggregate power at time \( t \) (\( P \) [kW]),
- the aggregate PF at \( t \) (\( \phi \)), and
- the temporal probability of activation of each cluster at \( t \) (\( \nu_i \)).

The sparsity of a cluster in this paper is defined as that the cluster is only turned on occasionally over a month, resulting in a Gamma distribution (\( \Gamma \)) with small shape and scale parameters, \( \kappa \) and \( \vartheta \) (e.g. low-PF cluster in Fig. 7). If sparsity is detected in the
i\textsuperscript{th} cluster, the activation threshold, $a_i$, is defined in (7) as the most frequent power.

$$a_i = \begin{cases} \arg\max_{\hat{p} \in \hat{p}_i} (P(\hat{p}_i) \geq \gamma), & \text{if } a_i > \kappa \vartheta \\ \hat{p}_i \max / 2, & \text{if } a_i \leq \kappa \vartheta, \end{cases}$$

where $P(\cdot)$ denotes the probability function, $\hat{p}_i$ denotes all the active components of the filtered P–Q points in the i\textsuperscript{th} cluster, $\hat{p}_i$ is any point in $\hat{p}_i$, $\gamma$ denotes the cut-off threshold, and $\kappa \vartheta$ represents the mean of $\Gamma$.

The activation of the i\textsuperscript{th} cluster depends on $P$. For example, if $P > a_i$ at $t$, the cluster will have a higher probability of being active. However, the power of non-sparse clusters will also affect the inference. Therefore, $\varphi$ and $P_{\theta}$ are also considered to derive $w_{ij}$ in (6a). A sample inference algorithm for $w_{ij}$ is provided in Fig. 8, where $\varphi_j$ is the PF range of the i\textsuperscript{th} cluster, $P_{\text{on}}$ is the activation probability threshold, $w_{\text{off}}$ is the weight for possible OFF states, and $w_{\text{on}}$ is the weight for possible ON states.

The active probability $P_{\text{on}}$ at $t$ is derived from historical data as (8). Note that the process of finding $w$ only applies to cases when at least one sparse load cluster exists. For other cases without sparsity, $w$ are set to ones.

$$P_{\text{on}} = \begin{cases} \max(\hat{p}_i^t) / a_i, & \text{if } \max(\hat{p}_i^t) / a_i \leq 1 \\ 1, & \text{otherwise}, \end{cases}$$

where $\hat{p}_i^t$ includes all the power over the training period of the i\textsuperscript{th} cluster grouped by hour.

3.5. Updating signatures

The overall signature inference relies on the historical smart meter data. In this paper, the signatures are updated every month in a rolling window, which reduces seasonal effect by periodically updating the signatures. The seasonal effect can be further accounted for by updating the signatures when major changes in the correlation between clusters and the ambient temperature are detected.

4. Results and discussion

The optimization problem in (3) is solved using the Genetic Algorithm in MATLAB 2015b with both linear and nonlinear constraints. The problem in (6) is solved using the $fmincon$ function in MATLAB with default settings. All the calculations are performed on a computer with 2.26 GHz Intel Core 2 Duo processor and 8G RAM.

4.1. Test data

The test data used in this paper is from the Pecan Street database collected from real households in Austin, TX [23]. The database contains sub-metered data over several years. Disaggregation algorithms can be developed and validated with such data. Power factor of each load is assumed based on [24,25]. Note that the Pecan Street data of each house may not include all the loads inside the house, so some load clusters may be sparse. The test objectives of this paper are to examine the performance of the disaggregation algorithm:

- on different houses,
- in different seasons,
- in larger scale such as residential blocks,
- in real time with signatures derived from historical data.

4.2. Load signature inference

This paper tests the performance of the algorithm on houses with typical data shapes observed in the test data (Fig. 9). Each shape is explained in Table 2.

4.2.1. Ground truth

The clustering process creates a PF range ($\varphi_j$) for each cluster. The true load clusters are derived by grouping the individual loads that have PFs within each $\varphi_j$. The true signatures are derived in (9)–(10) where $N_j$ is the number of loads in each cluster with PF.
Fig. 9. P–Q scatter plots of the test data over two month.

Fig. 10. Signature inference results for a Type-IV house.

∈ ϕ, θ^k_i is the angle of the k'th load in the i'th cluster, and p^k_i is the time-based load profile of the k'th load over the training period.

\[ \theta_i = \sum_{k=1}^{N_i} (\theta^k_i) / N_i. \]  

\[ p^\max_i = \max \left( \sum_{k=1}^{N_i} p^k_i \right). \]  

4.2.2. Power angles

We demonstrate the results for a type-IV single-family house in Austin, TX. Fig. 10 shows the inferred signature vector \( \hat{v}_i \) of each cluster, indicating that \( \theta_i \) of each cluster is close to the actual angle \( \theta_i \) of the actual signature, \( v_i \). The details are provided in Table 3.

4.2.3. Maximum power

In Fig. 10, the length of the vectors in solid lines indicates true \( p^\max_i \), and that of the vectors in dashed lines shows the inferred \( \hat{p}^\max_i \). Note that slightly larger \( \hat{p}^\max_i \) helps relax the bounds of the disaggregation problem in the later stage to avoid infeasible solutions. Due to the simplicity of our algorithm, \( \hat{p}^\max_i \) can be adjusted based on the disaggregation results by comparing \( \hat{p}^\max_i \) and the resulted maximum values after disaggregation. If a large discrepancy is detected, we adjust \( \hat{p}^\max_i \) and re-do the disaggregation (feedback in Fig. 1).

4.3. Load disaggregation

4.3.1. Evaluation metrics

The modified F-measure in [11] and the Mean Absolute Error (MAE) are used in this paper. The modified F-measure approach in [11] accounts for both binary events and power matching. However, due to that load clusters in this paper have various ON states, we adjust the threshold \( \rho \) in [11] as (11). In some cases when a less frequent event with large \( P \) occurs (e.g. pool pump), the F-measure approach may exaggerate the accuracy if \( \sigma(p^+_i) > \mu(p^+_i) \). Therefore, the MAE approach is additionally considered as a supplementary measure of performance.

\[ F\text{-measure} = \frac{2 \cdot \text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}}, \]  

\[ \text{Precision} = \frac{\text{ATP}}{\text{ATP} + \text{ITP} + \text{FP}}, \]  

\[ \text{Recall} = \frac{\text{ATP}}{\text{ATP} + \text{ITP} + \text{FN}}, \]  

\[ \text{ATP} \iff x > 0, \quad x_0 > 0, \quad |x - x_0| / x_0 \leq \rho, \]  

\[ \text{ITP} \iff x > 0, \quad x_0 > 0, \quad |x - x_0| / x_0 > \rho, \]  

\[ \text{FP} \iff x = 0, \quad x_0 = 0, \]  

\[ \text{FN} \iff x = 0, \quad x_0 > 0. \]  

\[ p^+_i = \{ p_i : p_i > p'_i \}, \]  

\[ \rho_i = \sigma(p^+_i) / \mu(p^+_i), \]  

where \( \text{ATP}, \text{ITP}, \text{FP}, \) and \( \text{FN} \) refer to the number of classifications that are accurate true positive, inaccurate true positive, false positive, and false negative. \( x \) denotes the power of a cluster at a given time from disaggregation, \( x_0 \) denotes the corresponding true power, \( \rho \) denotes the threshold for determining \( \text{ATP} \) and
Table 2
Typical P–Q shapes.

<table>
<thead>
<tr>
<th>Shape</th>
<th>Indication</th>
</tr>
</thead>
<tbody>
<tr>
<td>Type I</td>
<td>Loadswith high or low PF are small, or turned on in similar time periods</td>
</tr>
<tr>
<td>Type II</td>
<td>Loadswith high and low PF are both high, possibly turned on very often at the same time. Very large resistive loads are possible (e.g. EV charging)</td>
</tr>
<tr>
<td>Type III</td>
<td>Large high-PF loads and/or large low-PF loads, possibly turned on at different times</td>
</tr>
<tr>
<td>Type IV</td>
<td>Loadswith different PF have similar power consumption and usage patterns</td>
</tr>
</tbody>
</table>

Table 3
Detailed results of signature inference.

<table>
<thead>
<tr>
<th>Cluster 1</th>
<th>Cluster 2</th>
<th>Cluster 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\theta_i$ (degree)</td>
<td>2.6</td>
<td>11.7</td>
</tr>
<tr>
<td>$\hat{\theta}_i$ (degree)</td>
<td>2.6</td>
<td>11.8</td>
</tr>
<tr>
<td>Error in $\hat{\theta}_i$ (degree)</td>
<td>0.0</td>
<td>0.1</td>
</tr>
<tr>
<td>True $P_{\text{max}}^i$ (kW)</td>
<td>4.4</td>
<td>2.4</td>
</tr>
<tr>
<td>Inferred $P_{\text{max}}^i$ (kW)</td>
<td>5.6</td>
<td>3.3</td>
</tr>
<tr>
<td>$L_i$ (kW)</td>
<td>1.1</td>
<td>0.8</td>
</tr>
<tr>
<td>$W_i$ (%)</td>
<td>32</td>
<td>16</td>
</tr>
</tbody>
</table>

Table 4
Disaggregation evaluation for Type-I and III data (from high to low-PF).

<table>
<thead>
<tr>
<th>Type-I data</th>
<th>Type-III data</th>
</tr>
</thead>
<tbody>
<tr>
<td>MAE (kW)</td>
<td>[0.06, 0.08, 0.06]</td>
</tr>
<tr>
<td>F-measure (%)</td>
<td>[90.2, 80.5, 74.7]</td>
</tr>
</tbody>
</table>

$I_{TP}$, $P_{f,i}$ denotes the points with $P$ higher than $P_{f,i}$, $P_{f,i}$ denotes the most frequent non-base power of the $i$th true cluster, $\sigma(\cdot)$ is the standard deviation operator, and $\mu(\cdot)$ is the mean operator.

Compared to $\rho$ in [11], directly using the mean and variance of load cluster will result in exaggerated F-measure score because of larger variance in load cluster than in single load. The new definition of $\rho$ targets the upper tail of the histogram of $p_i$, which represent relatively rare events. Eq. (11) is calculated based on the dispersion of power in these rare events.

4.3.2. Test on typical profiles

For conciseness, this section provides the disaggregation results for two scenarios—households without EV (Type I) and with EV (Type III)—in this section (Figs. 11–12). Note that because of the nature of the test data, only the data of some of the loads in a household are available, thus resulting sparse load clusters (e.g. medium-PF cluster in Fig. 11) and low-power clusters (e.g. medium-PF in Fig. 12).

Figs. 11–12 indicate that sparse clusters do not necessarily cause large error, but the overlap of peaks and the typical turn-on power of a cluster do. For example, in Fig. 11, both the medium and low-PF clusters are sparse. If both clusters have high turn-on probabilities at time $t$ (condition (c) in Fig. 8), it will be uncertain which cluster should be ON if $P > a_i$. The medium-PF cluster in Fig. 12, due to low power, is affected by the small errors in the other two clusters. On the other hand, clusters with large resistive power could be more easily retrieved (e.g. EV load at 3-kW level in Fig. 12). The disaggregation performance on Type-I and Type-III data are evaluated in Table 4.

4.3.3. Seasonal effect

This section studies a set of data that contains heater and A/C (Figs. 13–14, Table 5).

Based on Figs. 13–14, large A/C load in summer and large heating load in winter lead to better disaggregation performance on the corresponding clusters (low-PF cluster in Fig. 13 and high-PF in Fig. 14). However, for example, a small error in the low-PF cluster in Fig. 13 may cause large error in the medium-PF cluster (sparse). Our solution is to remove the peaks in the medium-PF cluster that correlate to the peaks in the other clusters after disaggregation.

The raw results from disaggregation in the medium-PF cluster may contain peaks that are the residuals of the other two, thus strongly correlated to their peaks. For example, the raw results of the medium and high-PF clusters have correlation coefficient ($r$) of 0.74. After removing the erroneous peaks in the medium-PF cluster, $r$ is reduced to 0.08 (true $r = 0.03$). Note that the mitigation is only intended to demonstrate a potential solution on improving disaggregation performance. Future work will be required to improve general performance in disaggregating sparse clusters in single houses.

Fig. 14 further shows that the main errors reside in the non-resistive loads. Especially for sparse loads with various active states (low peaks and high peaks in the medium-PF in Fig. 14), the disaggregator is not able to differentiate between the medium and
Fig. 13. Disaggregation results in summer.

Fig. 14. Disaggregation results in winter.

Table 5
Disaggregation evaluation in summer and winter (from high to low-PF).

<table>
<thead>
<tr>
<th></th>
<th>Summer</th>
<th>Winter</th>
</tr>
</thead>
<tbody>
<tr>
<td>MAE (kW)</td>
<td>[0.07, 0.08, 0.11]</td>
<td>[0.08, 0.08, 0.09]</td>
</tr>
<tr>
<td>F-measure (%)</td>
<td>[82.9, 46.5, 95.3]</td>
<td>[94.9, 44.4, 89.9]</td>
</tr>
</tbody>
</table>

low-PF clusters with available information. Nevertheless, in the context of hourly frequency and single house, the disaggregation algorithm is able to identify the major seasonal loads without referring to temperature data. The drawbacks seen in Figs. 13–14 can be avoided if dealing with an aggregation of houses (discussed in the next section).

4.3.4. Aggregation of houses

The key advantage of the disaggregation algorithm in this paper is the scalability beyond single houses. A scenario in the microgrid context in [26] is considered, in which each node in the microgrid may connect to 10–12 houses. The aggregated consumption of 10–12 houses typically has less sparsity compared to the single-house cases. Hence, it is expected the errors due to sparsity (Fig. 14) can be reduced, and the disaggregation can be simplified by eliminating the steps in Fig. 8.

An example of 10-house aggregation is provided in Fig. 15. The results show the MAEs are [0.25, 0.44, 0.46] kW and the F-measure scores are [96.0, 84.3, 93.5]%. Note that because each cluster is always ON, we regard \( P_{\text{max}}^{i} \) as the threshold for separating the true negative, false negative, and false positive events in the F-measure metric.

Depending on application, combining the disaggregation results of the medium and low-PF clusters can offset the error and result in one larger load cluster with smaller error. For instance, if we combine the medium and low-PF clusters in Fig. 15, we can achieve an F-measure score of 99.9% and MAE of 0.4 kW for the combined cluster.

4.3.5. Real-time capability

The real-time potential of our algorithm is studied for the 10-house aggregation. The real-time implementation uses the signatures derived from the historical data in a real-time receding window with one-month length. In this way, the load signatures will be more accurate thanks to the most recent data. Fig. 16 and Table 6 show the results for a period of two weeks following the
Table 6

<table>
<thead>
<tr>
<th></th>
<th>Offline (over a month in Mar.)</th>
<th>Online (over two weeks in Apr.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MAE (kW)</td>
<td>[0.23, 0.44, 0.28]</td>
<td>[0.19, 0.42, 0.30]</td>
</tr>
<tr>
<td>F-measure (%)</td>
<td>[94.9, 78.1, 99.0]</td>
<td>[90.0, 72.9, 96.0]</td>
</tr>
</tbody>
</table>

![Fig. 17. Four-cluster disaggregation results for 10-house group.](image)

last day of March in Fig. 15. The online performance is comparable with the offline results.

4.3.6. More clusters

This section shows the disaggregation into four clusters using the true power angles (skipping Eqs. (3)–(4)). As mentioned in 3.3.1, disaggregation into more than three clusters is not suggested. The results in Fig. 17 yield F-scores of [92.0, 49.0, 69.0, 89.2]%. Despite that the true angles are used, the disaggregation performance degrades at granular level when clusters have similar PFs.

4.4. Sensitivity

The model for deriving the power angles in (3) is more complicated than directly using the average angles after clustering. This section compares the disaggregation performance with these two options. In addition, the benefit of using the PF and addition filters in finding the power magnitude (Section 3.3.2) will also be discussed.

Table 7 shows the comparison between using (3) and the average power angle of each cluster for disaggregating the 10-house aggregation. The average angle denotes the average from the raw P–Q points in each cluster. Model (3) generally improves the performance in all evaluation methods. The improvement is more substantial for larger scale as (3) is more consistent when dealing with less sparse load clusters. For single houses, the maximum improvement in F-score in the studied data is about 12%.

![Fig. 18. Average disaggregation performance with various errors in power angles.](image)

![Fig. 19. Error distribution in medium and low disaggregation performance.](image)

Figs. 18 and 19 show the analysis in parallel coordinates. We simulate 100 scenarios with random errors in each power angle. For each cluster, the absolute error evenly distributes between 0% and 30% as the deviation from the true angle (model (3) is skipped). Fig. 18 shows that large errors in the medium- and low-PF cluster result in low disaggregation performance (59%–68% average F-score). Lower errors, on the other hand, result in 81% average F-score. Fig. 19 shows individual results in low-performance disaggregation (<68%F-score). Errors in medium- and low-PF angles particularly degrade disaggregation performance due to that the medium- and low-PF clusters are more sparse in our test data.

The PF and addition filters in Section 3.3.2 affect the MAE in disaggregation. For the 10-house aggregation, these filters improve the MAE by an average of 5%. For single houses, the improvement in single clusters could reach 30%. These filters have more impact on clusters containing fewer individual loads.

4.5. Test in real-world application

The disaggregation approach is applied to a set of real-world aggregate data from a BC Hydro smart meter in Kootenay, BC, Canada (bottom-left in Fig. 2). The available data is the hourly measurement of P and Q for a single house with electric heating. Sub-metered data of individual loads are not available.

The disaggregation results are illustrated in Fig. 20. We validate the results based on our previous work in [27]. It infers the usage frequency and power consumption of typical residential loads. Fig. 20 shows that the medium-PF cluster only occasionally consumes large power in a weekly pattern (March 27 and April 4), indicating possible dishwasher load (Table II in [27]). The low-PF cluster corresponds to clothes washer and dryer because of
its more frequent turn-ons (clothes washer, used 5–9 times a week [27]) and occasional peaks (dryer, used for some but not all loads of clothes washer [27]). The high-PF cluster correlating to space heating, water heating, and range consumes the majority of power during off-work hours, evenings, weekends, and holidays. For example, the long duration of high-PF load started on March 28 (March 29 was Good Friday) and April 5 (Friday).

Fig. 15 also demonstrates that our algorithm could possibly reveal the consumption of typical loads that consume large active or reactive power. This could be achieved without the survey data or assumptions made in [27].

5. Conclusions

This paper proposes an unsupervised residential disaggregation algorithm that requires minimal prior knowledge of loads. The algorithm is able to detect possible load signatures on load-cluster level directly from the aggregate P–Q measured by smart meters at hourly frequency. Disaggregation of both P and Q are implemented by an optimization approach bounded by the inferred signatures. The results show that the algorithm is able to disaggregate load clusters categorized by power factors. The algorithm is adaptive to various composition and types of loads regardless of controlled loading (e.g. DR and direct load control). We further examine the seasonal effect on the disaggregation accuracy and find that large cooling or heating loads have no adverse effect on our algorithm. Real-time capability of our algorithm can be achieved by updating load signatures with the most recent historical data. The algorithm could yield improved results for small aggregation of houses, thus extending its application in microgrids for local grid planning and dispatch with enhanced data utilization.

Table 7

| Model vs. average power angles (data as improvement by (3) for 10-house aggregation). |
|----------------------------------|----------------|----------------|
| F-measure (%)                   | MAE on P (%)  | MAE on Q (%)  |
| High-PF cluster                 | 3.79          | 22.56          | 23.15          |
| Medium-PF cluster               | 18.15         | 10.16          | 0.00           |
| Low-PF cluster                  | 7.81          | 18.31          | 16.37          |

References


