## SIMON FRASER UNIVERSITY Department of Economics

Econ 815 Financial Economics, I Prof. Kasa Summer 2019

## FINAL EXAM

Answer the following True, False, or Uncertain. Briefly explain. (8 points each).

- 1. The risk-free rate increases when the variance of output increases.
- 2. Disagreement increases asset prices.
- 3. According to the Lucas model, price/dividend ratios are constant if investors have log preferences.
- 4. Increased uncertainty increases option prices.
- 5. The Black-Scholes formula assumes complete markets.
- 6. (30 points). Use Put-Call Parity to express the value of a put option in terms of the value of a call option, the current stock price, the strike price, and the interest rate.
- 7. (30 points). A representative household has preferences

$$E_0 \sum_{t=0}^{\infty} \beta^t \log C_t$$

Consider an equity claim that yields a stream of nonstorable dividends,  $d_t$ . In equilibrium,  $C_t = d_t$ . The dividend process follows a 2-state Markov chain with state space  $d_t \in \{d_L, d_H\}$  and transition matrix,

$$P = \left[ \begin{array}{cc} \pi_L & 1 - \pi_L \\ 1 - \pi_H & \pi_H \end{array} \right]$$

Let  $p_t$  be the ex-dividend price of the 'Lucas tree' (i.e., if you buy it at time-t, your first dividend receipt will be in period-(t + 1)).

- (a) Derive the equilibrium price function, mapping the state of the economy at time-t into  $p_t$ . (Hint: you may find it easier to compute the price/dividend ratio). How does the rate of return evolve over time?
- (b) Compute the (state-dependent) risk-free interest rate.

Now suppose a fast-talking foreign 'entrepreneur' moves to the country and undertakes a leveraged buyout of economy's stock market. His operation is financed by issuing risk-free bonds which pay  $\eta \in (0, y_L)$  each period, and by selling equity claims that pay  $d_t - \eta$  per period.

- (c) Compute the value of the bonds issued by the entrepreneur's firm. Compute the value of the firm's equity.
- (d) How do your answers to part (c) compare to your answers to parts (a) and (b)? (Hint: This question is related to an important result in corporate finance, known as the 'Modigliani-Miller Theorem'.)