

Morris & Shin (AER, 1998)

- MS show that the existence of multiple equilibria in 2nd generation currency crisis models depends crucially on the assumption of Common Knowledge - you know what other speculators are going to do. If instead speculators have "imperfect common knowledge" arising from idiosyncratic private information, then multiple equilibria disappear, and a unique equilibrium is generated.
- MS show that an important aspect of currency crises is the "quality" of information conveyed to the market (i.e., to what extent it is Common Knowledge).

Assumptions

- 1.) A continuum of speculators on the interval $[0,1]$ must decide whether to attack a pegged exchange rate. There are only 2 possible actions "attack" or "don't attack".
- 2.) Each speculator has one unit of domestic currency.

- 3.) The state of fundamentals is described by a parameter θ , uniformly distributed on $[0, 1]$. A high value of θ represents "strong fundamentals".
- 4.) The shadow floating ex. rate is defined as $f(\theta)$ [where the ex. rate is defined as the value of domestic currency]. $f' > 0$
- 5.) The ex. rate is pegged at a value $\bar{e} > f(\theta)$, $\forall \theta$. Therefore, $\bar{e} - f(\theta)$ is the profit to speculators from a devaluation.
- 6.) However, speculators must pay a fixed cost, t , to take a position. Net profits are therefore $\bar{e} - f(\theta) - t = D(\theta) - t$. $D' < 0$ and $D(1) < t$ [if fundamentals are really strong, then it doesn't pay to attack, even if everyone does].

The payoff matrix to a speculator is therefore

	"success"	"failure"
Attack	$D(\theta) - t$	$-t$
Don't Attack	0	0

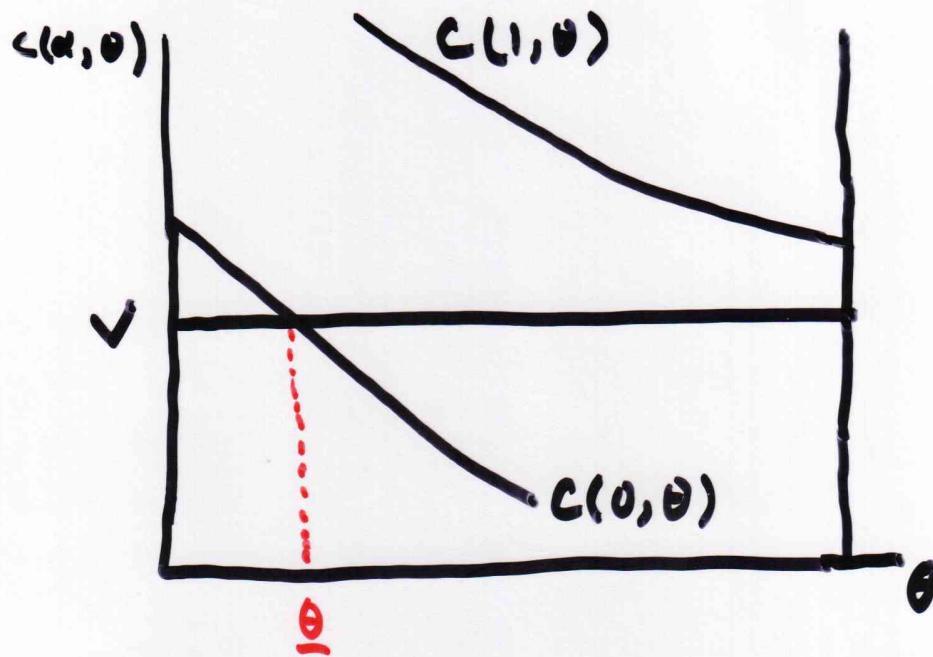
Unfortunately, speculators don't know θ , nor do they know whether an attack will succeed.

- 7.) The Central Bank derives a payoff of v from maintaining the peg. It faces a cost, c , of defending the peg. c decreases with θ , and increases with the proportion, α , of speculators who attack the peg, i.e., ~~$c(\alpha, \theta)$~~

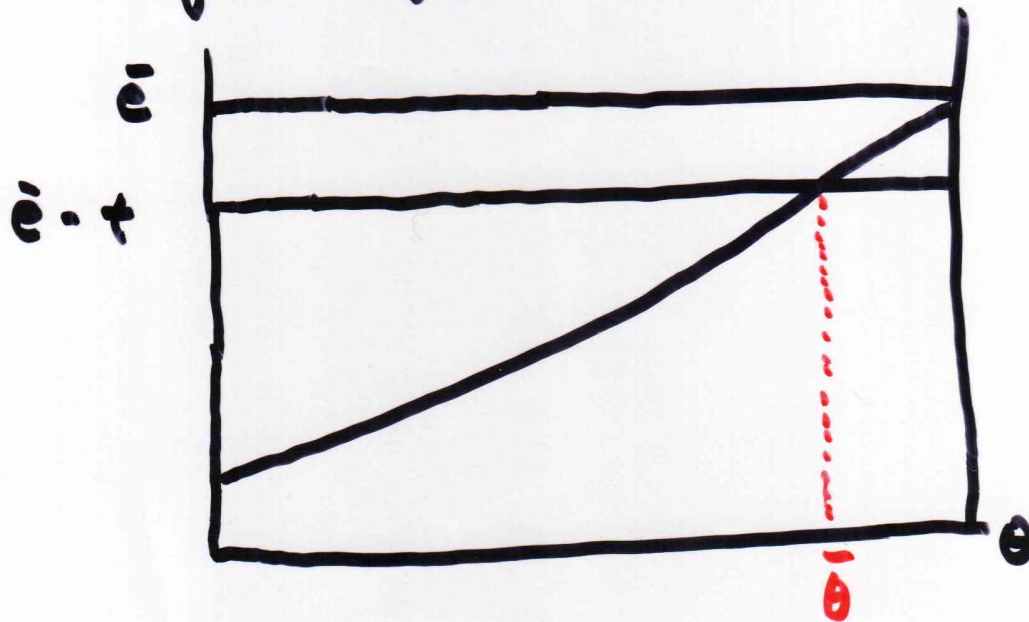
$$\text{ ~~c~~ } c = c(\overset{+}{\alpha}, \overset{-}{\theta})$$

Assume $c(0, 0) > v$ [when fundamentals are really bad, the CB abandons the peg no matter what], and $c(1, 1) > v$ [when everybody attacks, the CB abandons the peg, no matter how strong fundamentals are].

The following graph depicts these assumptions



8.) $\bar{e} - f(1) < t$ [when fundamentals are really strong, it doesn't pay to attack].



These assumptions divide the space of fundamentals into 3 regions:



9.) Speculators do not observe θ . Each receives an independent noisy signal, x_i , of θ . x_i is uniformly distributed around θ , $x_i \in [\theta - \epsilon, \theta + \epsilon]$.

Note : Signals are correlated. Your signal tells about θ and other people's signals

Timing

- 1.) Nature draws θ
- 2.) Traders observe signals, x_i , and simultaneously decide whether to attack.
- 3.) CB observes θ and the number of attackers, and then decides whether to hang on or devalue.

Theorem : There is a unique θ^* such that, in any equilibrium the CB abandons the peg if and only if $\theta \leq \theta^*$