

## How Much Would You Pay to Resolve Long-Run Risk?<sup>†</sup>

By LARRY G. EPSTEIN, EMMANUEL FARHI, AND TOMASZ STRZALECKI\*

*Though risk aversion and the elasticity of intertemporal substitution have been the subjects of careful scrutiny, the long-run risks literature as well as the broader literature using recursive utility to address asset pricing puzzles has ignored the full implications of their parameter specifications. Recursive utility implies that the temporal resolution of risk matters and a quantitative assessment thereof should be part of the calibration process. This paper gives a sense of the magnitudes of implied timing premia. Its objective is to inject temporal resolution of risk into the discussion of the quantitative properties of long-run risks and related models. (JEL D81, G11, G12)*

The long-run risks model of Bansal and Yaron (2004) has delivered a unified explanation of several otherwise puzzling aspects of asset markets.<sup>1</sup> Since Mehra and Prescott (1985) posed the equity premium puzzle, it has been understood that the asset market puzzles are *quantitative* and that an explanation must be consistent with observations in other markets and also with introspection. Imposing such discipline led Mehra and Prescott to exclude rationalization of the observed equity premium by levels of risk aversion exceeding their well-known upper bound of ten. This bound on risk aversion has been largely respected since, including in long-run risk models (LRR). However, we suggest in this paper that quantitative discipline has been lax in another equally important aspect of the long-run risks model.

\*Epstein: Department of Economics, Boston University, 270 Bay State Road, Boston, MA 02215 (e-mail: [lepstein@bu.edu](mailto:lepstein@bu.edu)); Farhi: Department of Economics, Harvard University, 1805 Cambridge Street, Cambridge, MA 02138, and NBER (e-mail: [efarhi@fas.harvard.edu](mailto:efarhi@fas.harvard.edu)); Strzalecki: Department of Economics, Harvard University, 1805 Cambridge Street, Cambridge, MA 02138 (e-mail: [tomasz\\_strzalecki@harvard.edu](mailto:tomasz_strzalecki@harvard.edu)). We thank Robert Barro, Jarda Borovicka, John Campbell, Eddie Dekel, Faruk Gul, Wolfgang Pesendorfer, Ben Polak, Todd Sarver, Costis Skiadas, Jessica Wachter, Stan Zin, and two referees, as well as the audiences at the AEA meetings in San Diego, Bank of Portugal, University Montreal, and Tel Aviv for useful comments. We thank David Rezza Baqaee for excellent research assistance. This paper was written in part while Epstein was visiting the Economics Research Department of the Bank of Portugal and Strzalecki was visiting the Institute for Advanced Studies at Hebrew University and then the Cowles Foundation at Yale University. We are grateful for their support and hospitality, and also for the support of the Sloan Foundation (Strzalecki) and for NSF grants SES-0917740 and SES-1216339 (Epstein) and SES-1123729 and CAREER grant SES-1255062 (Strzalecki). The authors declare that they have no relevant or material financial interests that relate to the research described in this paper.

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<sup>1</sup>In his opening remarks, Bansal (2007) lists the following puzzles: the level of equity premium; asset price volatility; the large cross-sectional differences in average returns across equity portfolios, such as value and growth portfolios; and in bond and foreign exchange markets, the violations of the expectations hypothesis and the ensuing return predictability that is quantitatively difficult to explain. He then writes: “What risks and investor concerns can provide a unified explanation for these asset market facts? One potential explanation of all these anomalies is the long-run risks model.” For elaboration and many additional references see Bansal (2007); Piazzesi and Schneider (2007); Hansen, Heaton, and Li (2008); Colacito and Croce (2011); and Chen (2010).

As a representative agent model, LRR has two key components: the endowment process and preferences. The former is modeled as having a persistent predictable component for consumption growth and its volatility; it will be described more precisely below. The representative agent has Epstein-Zin preferences (Epstein and Zin 1989; Weil 1990), which permit a partial disentangling of the elasticity of intertemporal substitution (EIS) and the coefficient of relative risk aversion (RRA). Denoting time  $t$  consumption by  $c_t$ , continuation utilities  $U_t$  satisfy the recursion

$$(1) \quad U_t^\rho = (1 - \beta) c_t^\rho + \beta [E_t(U_{t+1}^\alpha)]^{\rho/\alpha}$$

when  $\rho \neq 0$ , and otherwise

$$(2) \quad \log U_t = (1 - \beta) \log c_t + \beta \log [E_t(U_{t+1}^\alpha)]^{1/\alpha}.$$

We assume that  $\rho < 1$ ,  $0 \neq \alpha < 1$ , and  $0 < \beta < 1$ . The utility of a deterministic consumption path is in the constant elasticity of substitution (CES) class with the elasticity of intertemporal substitution

$$\text{EIS} = \frac{1}{1 - \rho}.$$

Epstein and Zin (1989) show that  $1 - \alpha$  is the measure of relative risk aversion for timeless wealth gambles and also for suitable gambles in consumption where all risk is resolved at a single instant, justifying thereby the identification

$$\text{RRA} = 1 - \alpha.$$

The noted disentangling is possible because a decrease in  $\alpha$  increases risk aversion without affecting the attitude toward consumption smoothing over time given certainty, unlike in the standard additive power utility model where  $\rho = \alpha$ . With these interpretations of  $\rho$  and  $\alpha$ , parameter values in the LRR literature are specified with due care paid to evidence about the elasticity of substitution and the degree of risk aversion. However, as is clear from the theoretical literature,  $\rho$  and  $\alpha$  affect also another aspect of preference in addition to the EIS and RRA. Clearly, judging the plausibility of parameter values requires that one consider their full quantitative implications for all dimensions of preference.

The above model of utility belongs to the recursive class developed by Kreps and Porteus (1978) in order to model nonindifference to the way in which a given risk resolves over time. For a simple example, suppose that consumption is fixed and certain in periods 0 and 1, and that it will be constant thereafter either at a high level or at a low level, depending on the outcome of the toss of an unbiased coin. Do you care whether the coin is tossed at  $t = 1$  or at  $t = 2$ ? We emphasize that it is risk about consumption—and not income—that is at issue, so that there is no apparent planning advantage to having the coin tossed early. According to the standard additive power utility model ( $\rho = \alpha$ ), the time of resolution of the

given risk is a matter of indifference. But not so more generally for recursive utility. For the specification (1)–(2), it is well known that early resolution of a given risk (here tossing the coin at  $t = 1$ ) is always preferable if and only if

$$(3) \quad 1 - \alpha = \text{RRA} > \frac{1}{\text{EIS}} = 1 - \rho.$$

This condition is satisfied by the parameter values typically used in LRR models where both EIS and RRA are typically taken to exceed 1. Moreover, there is clear intuition that nonindifference to temporal resolution of risk might matter in matching asset market data: because long-run risks are not resolved until much later, they are treated differently, and penalized more heavily than are current risks, thus permitting a large risk premium to emerge even when shocks to current consumption are small. This begs the question whether the differential treatment required to match asset returns data is plausible, which is obviously a quantitative question and calls for evidence about the attitude toward temporal resolution.

We are not aware of any market-based or experimental evidence that might help with a quantitative assessment.<sup>2</sup> In principle, the attitude toward the temporal resolution of risk may underlie behavior in many multiperiod settings. However, it is not clear how to disentangle the attitude toward the psychic benefit of early resolution of consumption risk, which is the issue at hand, from either the instrumental benefit of early resolution of income risk—which is plausibly more directly observable at the micro level—or the pricing of consumption risk which is observable from asset market data.<sup>3</sup> Of course, the approach of the long-run risk literature yields information about the former *under the assumption* of Epstein-Zin utility and a suitable endowment process. However, our objective is to judge whether this approach is a good one. To do so, we suggest a simple thought experiment that through introspection may help to judge plausibility of the parameter values used in the LRR literature. Thought experiments and introspection play a role also in assessing risk aversion parameters (see, for example, Kandel and Stambaugh 1990, 1991; Mankiw and Zeldes 1991; and Rabin 2000). In the latter context one considers questions of the form, “How much would you pay for the following hypothetical gamble?” Here we ask instead, “What fraction of your consumption stream would you give up in order for all risk to be resolved next month?” We call this fraction the *timing premium* and study its dependence on the parameters of the model.

<sup>2</sup>The small experimental literature that we are aware of (see, e.g., Ahlbrecht and Weber 1996; Brown and Kim forthcoming, and references therein) focuses on whether individuals prefer early or late resolution, not on the strength of this preference. Our paper may provide stimulus for more work along these lines; an important question is how to extrapolate from the experimentally feasible risks and time intervals. There is also some evidence from field experiments that many individuals choose not to learn their test results for various diseases (see, e.g., Thornton 2008; and Oster, Shoulson, and Dorsey 2013); given the clear instrumental value of information, this implies that the psychic benefit of early resolution is negative. However, it seems even harder to extrapolate from health outcomes that those studies focus on to consumption outcomes that are relevant here.

<sup>3</sup>There is a literature that seeks to understand risk pricing across maturities (see e.g., Hansen, Heaton, and Li 2008; and Hansen and Scheinkman 2009). In particular, Binsbergen, Brandt, and Koijen (2012) use data on dividend strips prices to show that the long-run risks model (as well as other classic models) have counterfactual predictions for the pricing of securities with varying maturities. Since there seem to be no parameterizations of these models which can resolve these puzzles and simultaneously match the moments addressed by Bansal and Yaron (2004), the work of Binsbergen, Brandt, and Koijen (2012) is complementary to ours in that it provides motivation for search for alternative (endowment and/or preference) models.

A picture that seems to emerge is that models which assume high persistence of the consumption process (as in Bansal and Yaron 2004) tend to imply a timing premium of the order of 25–30 percent, much higher than in an i.i.d. model where it is of the order of 7–10 percent. The intuition that persistence inflates the timing premium is corroborated with the rare disaster model; assuming high persistence of the jump process (as in Wachter 2013) implies a timing premium of the order of 40 percent, much higher than in the i.i.d. model of Barro (2009), where it is around 20 percent.

Section I presents our theoretical and numerical results for the LRR model. Section II offers an extended discussion of the results framed as answers to the following series of questions: Why pay a premium for early resolution? Is introspection possible/useful? How is the premium for early resolution related to the welfare cost of risk (Lucas 1987)? What is the effect of modifying the endowment process to be i.i.d., or to correspond to rare disasters (Barro 2006, 2009) or persistent rare disasters (Wachter 2013)? What if a nonexpected utility model of risk preferences is adopted? Section III concludes and includes a brief comparison with related papers by Ai (2007) and D’Addona and Brevik (2011).

### I. How Much Would You Pay?

*The LRR Consumption Process.*—Consider a consumption process of the following form:

$$(4) \quad \log \frac{c_{t+1}}{c_t} = m + x_t + \sigma_t W_{c,t+1}$$

$$x_{t+1} = ax_t + \varphi \sigma_t W_{x,t+1}$$

$$\sigma_{t+1}^2 = \sigma^2 + \nu(\sigma_t^2 - \sigma^2) + \sigma_w W_{w,t+1},$$

where  $0 < a < 1$  and  $W_{c,t}$ ,  $W_{x,t}$ , and  $W_{w,t}$  are standard Gaussian innovations, mutually independent and i.i.d. over time.

Here  $x_t$  is a persistently varying predictable component of the drift in consumption growth. Though  $\varphi$  should be thought of as much smaller than unity, small innovations to  $x_t$  are important because they affect not only consumption prospects in the short run but also consumption for the indefinite future. The parameter  $a$  determines persistence of the expected growth rate process.

The volatility of consumption growth, represented by  $\sigma_t$ , is time-varying with unconditional variance given by  $\sigma^2$ . The empirical importance of stochastic volatility is emphasized by Bansal, Kiku, and Yaron (2012) and Beeler and Campbell (2012). Setting  $\nu = 0 = \sigma_w$  turns off stochastic volatility and leads to a process with a constant variance of consumption growth; Bansal and Yaron refer to this model as Case I and to the model with stochastic volatility as Case II.

The LRR literature also distinguishes between consumption and dividends and specifies a suitable process for the latter. But it is the consumption process as a whole—and not its components—that is important here in trying to understand the nature of preferences.

In LRR models, a consumption process similar to the above is the endowment of a representative agent in a Lucas-style exchange economy. It is well known that there is limited theoretical justification for the assumption of a representative agent; here it requires that everyone have identical Epstein-Zin (hence homothetic) preferences. Regardless, we treat the representative agent as a real individual when introspecting about her preferences. The infinite horizon can be understood as arising from a bequest motive, or as a rough approximation to a long but finitely lived individual.

*Definition of the Timing Premium.*—Here is the thought experiment. You are facing consumption described by (4) for  $t = 0, 1, \dots$ . In particular, the riskiness of consumption resolves only gradually over time ( $c_t$  and  $x_t$  are realized only at time  $t$ ). How much would you pay at time 0 to have all risk resolved next period? More precisely, you are offered the option of having all risk resolved at time 1. The cost is that you would have to relinquish the fraction  $\pi$  of both current consumption and of the consumption that is subsequently realized for every later period. What is the maximum value  $\pi^*$  for which you would be willing to accept this offer? Call  $\pi^*$  the *timing premium* for the consumption process in (4). Formally, let  $U_0$  be the utility of the consumption process in (4) with risk resolved gradually, and let  $U_0^*$  be the utility of the alternative process where all risk is resolved at time 1. Then<sup>4</sup>

$$\pi^* = 1 - \frac{U_0}{U_0^*}.$$

*Theoretical Derivation for EIS = 1.*—The magnitude of EIS, particularly whether it is less than or greater than 1, is a source of debate. Bansal and Yaron argue for an elasticity larger than 1 (in fact,  $EIS > 1$  is important for the empirical performance of their model). Because closed-form solutions are not available for  $EIS \neq 1$ , we compute values of the timing premium numerically below. However, first we derive a closed-form expression for the timing premium under the assumption of a unitary elasticity of substitution and restricting attention to the case of constant volatility for consumption growth.

Continuation utilities of the consumption process in (4), with risk resolved gradually, solve a recursive relation. Guess and verify that utility is given by

$$\log U_0 = \log c_0 + \frac{\beta}{1 - \beta a} x_0 + \frac{\beta}{1 - \beta} m + \frac{\alpha}{2} \frac{\beta \sigma^2}{1 - \beta} \left( 1 + \frac{\varphi^2 \beta^2}{(1 - \beta a)^2} \right).$$

<sup>4</sup>Utility admits an interpretation in terms of consumption perpetuities. For any consumption process  $c$ , its utility as defined in (1)–(2) equals that level of consumption which if received in every period and state would be indifferent to  $c$ . Thus  $\pi^*$  can be described as the fraction of the consumption perpetuity that if relinquished would just offset the benefit of early resolution of risk.

Denote by  $U_0^*$  the utility of the alternative process where all risk is resolved at time 1. Then the continuation utility  $U_1^*$  at time 1 is given by

$$\begin{aligned} \log U_1^* &= (1 - \beta)[\log c_1 + \beta \log c_2 + \beta^2 \log c_3 + \dots] \\ &= \log c_0 + \sum_{t=1}^{\infty} \beta^{t-1} \log (c_t/c_{t-1}). \end{aligned}$$

Therefore, from the time 0 perspective,  $\log U_1^*$  is normally distributed with mean  $\log c_0 + \frac{m}{1 - \beta} + \frac{a}{1 - \beta a} x_0$  and variance  $\frac{\sigma^2}{1 - \beta^2} \left( 1 + \frac{\varphi^2}{(1 - \beta a)^2} \right)$ . Conclude that

$$\begin{aligned} \log U_0^* &= (1 - \beta) \log c_0 + \beta \log (E_0(U_1^*)^\alpha)^{1/\alpha} \\ &= \log c_0 + \frac{\beta}{1 - \beta a} x_0 + \frac{\beta}{1 - \beta} m + \frac{\alpha}{2} \frac{\beta \sigma^2}{1 - \beta^2} \left( 1 + \frac{\varphi^2 \beta^2}{(1 - \beta a)^2} \right). \end{aligned}$$

Accordingly, one arrives at the following expression for the timing premium:

$$\pi^* = 1 - \exp \left[ \frac{\alpha}{2} \frac{\beta^2 \sigma^2}{1 - \beta^2} \left( 1 + \frac{\varphi^2 \beta^2}{(1 - \beta a)^2} \right) \right].$$

The premium is positive (i.e., early resolution is preferred) if and only if  $\alpha < 0$ , consistent with (3). In that case, the premium is increasing in RRA,  $\sigma^2$ ,  $\varphi$ ,  $\beta$ , and  $a$ , as one would expect. The first column of Table 1 gives a sense of the quantitative meaning of this formula for the parameter values (other than EIS) specified in Bansal and Yaron (2004) for a monthly frequency. (The risk premium described in the last row is defined in Section II.)

*Numerical Results.*—For values of EIS different than 1, we rely on numerical methods. To obtain the value of  $U_0$  we note that the value function  $U$  in (1) can be written as  $U(c, x, \sigma) = cH(x, \sigma)$ , where  $H : \mathbb{R} \times \mathbb{R}_+ \rightarrow \mathbb{R}_+$  is a solution to the functional equation

$$(5) \quad H(x, \sigma) = \left\{ 1 - \beta + \beta e^{\rho \left( m + x + \frac{\alpha \sigma^2}{2} \right)} E_{x, \sigma} H(x', \sigma'^\alpha)^{\frac{\rho}{\alpha}} \right\}^{\frac{1}{\rho}}.$$

$E_{x, \sigma}$  is the expectation conditional on  $x$  and  $\sigma$ . We discretize  $x$  and  $\sigma$ , approximate  $H$  by a Chebyshev polynomial, and approximate the expectation by a quadrature. Thus our approximation to (5) can be written as a system of nonlinear equations. We solve this system using AMPL. To compute the value of early resolution  $U_0^*$  we run Matlab Monte Carlo simulations with a fixed time horizon  $T = 2,500$  months (pasting  $U_0$  as the continuation value at  $T$ ).

TABLE 1—PREMIA IN THE LRR MODEL

	BY (but EIS = 1)	BY (Case I)	BY (Case II)
$\sigma$	0.0078	0.0078	0.0078
$\varphi$	0.044	0.044	0.044
$a$	0.9790	0.9790	0.9790
$\sigma_w$	0	0	$0.23 \times 10^{-5}$
$\nu$	0	0	0.987
$\beta$	0.998	0.998	0.998
RRA	7.5 or 10	7.5 or 10	7.5 or 10
EIS	1	1.5	1.5
Timing premium $\pi^*$	20% or 27%	23% or 29%	24% or 31%
Risk premium $\bar{\pi}$	38% or 48%	48% or 56%	48% or 57%

Table 1 reports our numerical results for  $EIS = 1.5$ . Figure 1 plots the isoquants of the timing and risk premia for the two specifications and a range of preference parameters.<sup>5</sup> We compute the timing premium and the risk premium for initial values of the state variables corresponding to the modal point of the state space  $x_0 = 0$  and  $\sigma_0^2 = \sigma^2$ . Although we do not report such numbers, it could be interesting to also compute the timing premium and the risk premium at other points of the state space or perhaps their average over the state space with respect to the ergodic distribution.

## II. Discussion and Perspective

*Why Pay a Premium?*—Would you give up 25 or 30 percent of your lifetime consumption in order to have all risk resolved next month? Keep in mind that it is risk about consumption that is at issue rather than risk about income or security returns. Thus, early resolution does not have any apparent instrumental value. Kreps and Porteus (1978, 1979) suggest that an instrumental value might arise because of an unmodeled underlying planning problem. Essentially, there are more primitive preferences defined over deeper variables that are the ultimate source of satisfaction; utility defined on consumption is an indirect utility function, and early resolution has value for reasons familiar from Spence and Zeckhauser (1972), for example. This sounds plausible in theory, but one needs a more concrete story in order to believe that it could generate a sizable timing premium.<sup>6</sup>

At a psychic level, early resolution of risk may reduce anxiety. However, anxiety is plausibly more important when risk must be endured for a long time. Therefore, the risk premium required for bearing a lottery is greater the longer the time that the individual has to live with the anxiety of not knowing how the lottery will be resolved. In other words, the willingness to bear a given risk declines as the date of resolution

<sup>5</sup>We limit RRA to be no greater than 10, the upper bound considered reasonable by Mehra and Prescott (1985) despite the fact that in the literature many calibrated, as well as estimated (see Chen, Favilukis, and Ludvigson 2013), parameter values exceed 10. Those parameter values would inflate the timing premium further.

<sup>6</sup>Ergin and Sarver (2012) characterize behavior, in terms of choice between “lotteries over sets of lotteries,” that indicates (or can be represented via) a hidden planning problem. It remains to see if this work will help in assessing the magnitudes of timing premia.

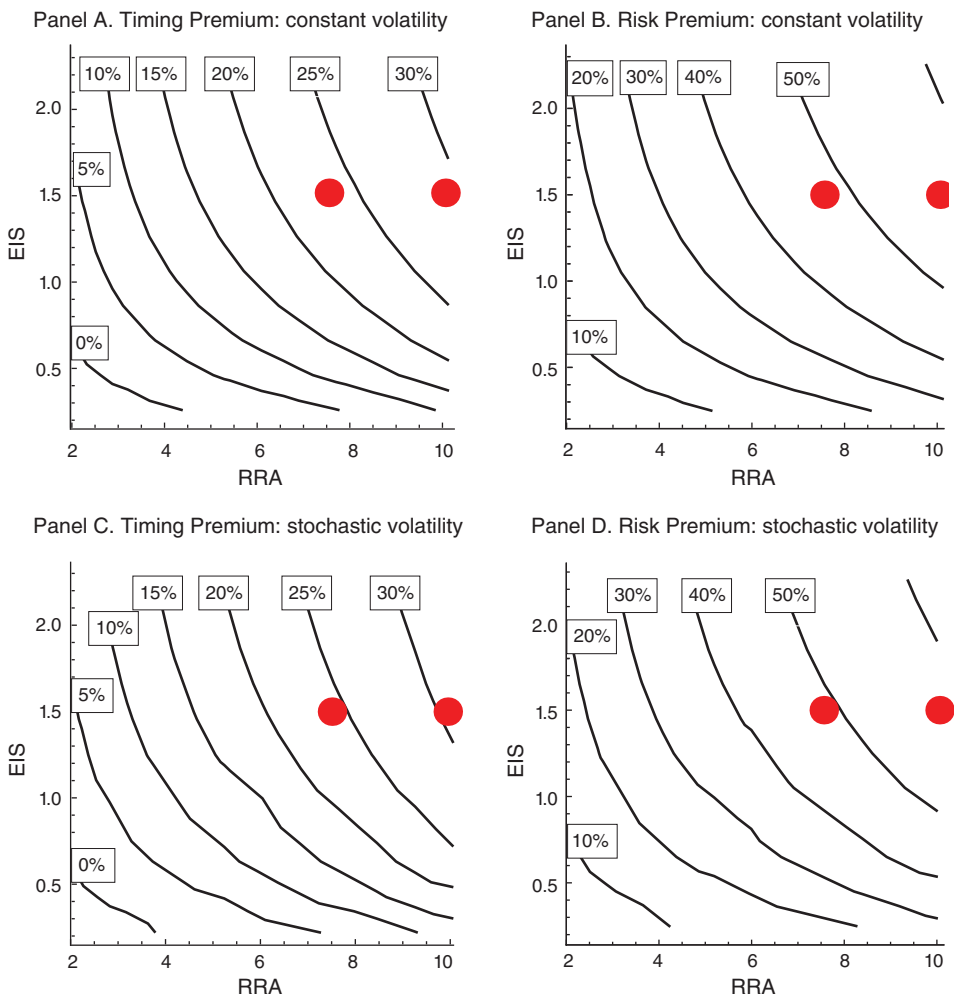


FIGURE 1. PREMIUM ISOQUANT MAPS FOR THE LRR MODEL

Notes: The gray dots denote the calibrated values of EIS and RRA. Other parameters are as in Table 1.

approaches, a form of dynamic inconsistency. However, such dynamic inconsistency is precluded when utility is recursive and thus anxiety cannot be a rationale for a timing premium given the utility functions considered here. (This argument is due to Grant, Kajii, and Polak 2000; Caplin and Leahy 2001; and Epstein 2008). To the extent that introspection is based in part on considerations of anxiety, stated timing premia overstate premia that are consistent with LRR.

For perspective, note that modeling nonindifference to the temporal resolution of risk is the *objective* in the Kreps and Porteus papers. Such nonindifference is plausible in theory as a property of “rational” preferences. Further, Epstein and Zin (1989) show that permitting a nonzero timing premium has the modeling benefit of allowing a partial separation between EIS and RRA. Thus even if one is skeptical about the descriptive importance of a nonzero timing premium, one might view



its use as a *cost* of separating EIS and RRA.<sup>7</sup> How costly is a quantitative question. Similarly, it is a quantitative issue whether nonindifference to timing makes sense as an important component of an empirical model. But applied papers using Epstein-Zin utility have accepted such nonindifference uncritically.

*Is Introspection Possible? Useful?*—One might question whether introspection is possible or reliable given the artificial nature of the question posed in the thought experiment: how much would you pay to have your lifetime risk resolved next month, keeping in mind that you cannot use that information. But the starkness of the question arguably helps introspection. For example, one might feel strongly, as we do, “why should I give up 25 percent... just to know earlier, when I can’t even use that information?” In fact, it is arguably easier to introspect than if one is allowed to use the information to reoptimize, in which case self-assessment of the timing premium would involve introspection about all of substitutability, risk aversion, *and* early resolution, as well as about the available financial instruments and more generally the collection of all consumption processes in an expected budget set.

Introspection is at best a matter of opinion and is inherently subjective. While we are not arguing that a consensus is possible, we are hoping that our exercise may help *some* people understand the LRR model more fully. The alternative is to leave the modeling exercise completely undisciplined, which we find unsatisfactory.

*How is the Timing Premium Related to the Welfare Cost of Risk?*—Perspective on the timing premium is provided by examining also what the representative agent would be willing to pay to eliminate risk entirely. Lucas (1987) introduced such a calculation into macroeconomics as a way to measure the welfare costs of business cycle fluctuations. His conclusion that consumption risk has very small welfare costs stimulated many others to see how different model specifications might lead to larger costs. Our interest here is less in the total cost of risk per se than in using the latter to provide further perspective on the size of the timing premium. Specifically, are the timing premia reported in Table 1 large *relative* to the total welfare cost of risk?

Consider the deterministic consumption process  $\bar{c} = (\bar{c}_t)$  where, for every  $t$ ,  $\bar{c}_t = E_0 c_t$ , where  $E_0$  is the expectation starting with  $x_0 = 0$  and  $\sigma_0^2 = \sigma^2$ .

Its utility at time 0 is  $\bar{U}_0$ . Whenever  $\alpha < 1$ , risk is costly ( $\bar{U}_0 > U_0$ ) and the cost may be measured by the *risk premium*  $\bar{\pi}$ , where<sup>8</sup>

$$\bar{\pi} = 1 - U_0/\bar{U}_0.$$

The last row of Table 1 shows the welfare costs implied by the LRR model. For the parameter values used by Bansal and Yaron (2004), an individual giving up roughly 50 percent of her deterministic consumption  $\bar{c}_t$  in every period would still be no worse off than with the long-run risk process in (4).

<sup>7</sup>This has always been Epstein’s view.

<sup>8</sup>Lucas uses  $\frac{\bar{\pi}}{1-\bar{\pi}}$  to measure the benefit of eliminating risk rather than  $\bar{\pi}$  to measure its cost. The difference between the two measures parallels the difference between the compensating variation (used here) and the equivalent variation (used by Lucas) of a policy change.

It can be verified further that, as one would expect,

$$\bar{U}_0 > U_0^* > U_0 \quad \text{if } \alpha < 0.$$

This suggests the following decomposition:

$$\frac{U_0}{\bar{U}_0} = \frac{U_0}{U_0^*} \cdot \frac{U_0^*}{\bar{U}_0},$$

whereby the total cost of risk is decomposed into the cost of bearing risk that is resolved late (after time 1), and the cost of bearing risk all of which is resolved early (at time 1). The relative importance of the first factor is given by

$$\frac{U_0^*/U_0}{\bar{U}_0/U_0} = \frac{U_0^*}{\bar{U}_0} = \frac{1 - \bar{\pi}}{1 - \pi^*}.$$

For the parameter values in Table 1, the indicated ratio is between 0.62 and 0.77. Thus, between two-thirds and three-quarters of the cost (in constant consumption perpetuity) of risk is attributable to the cost of late resolution.

*What is the Role of the Endowment Process?*—The numbers presented in Table 1 and Figure 1 depend on the parameters of the endowment process and in particular on the degree of persistence.<sup>9</sup> To examine the importance of persistence and to offer perspective on the improved fit of asset market data provided by the LRR model, we compare its timing premia to those implied by the benchmark i.i.d. model.<sup>10</sup> An i.i.d. growth process for consumption is a workhorse model, fits US data well, and is hard to distinguish statistically from the LRR process. It is assumed in, for example, Campbell and Cochrane (1999); Calvet and Fisher (2007), where dividends are separated from consumption; and in Barberis, Huang, and Santos (2001).

Table 2 assumes  $\beta = 0.998$ , and that  $\log(c_{t+1}/c_t)$  is i.i.d.  $N(m, \sigma^2)$ , with  $m = 0.0015$  and  $\sigma^2 = 0.00007$ . These latter values are roughly consistent with the annual mean (1.8 percent) and standard deviation (2.9 percent) for real per capita consumption growth used by Bansal and Yaron (2004) to calibrate their model. Comparison with Table 1 shows that timing premia here are considerably smaller than for the LRR model.

*Rare Disasters.*—Another specification of the endowment process that is prominent in the asset pricing literature is based on rare disasters. Barro (2009) also uses Epstein-Zin utility but he assumes an i.i.d. consumption process where in every period

<sup>9</sup>Bansal, Kiku, and Yaron (2012) use higher volatility persistence,  $\nu = 0.999$ . Our algorithm failed to find a solution to the value function. Hansen et al. (2007, Section 5.3) study a continuous time model where volatility follows a Feller square root process; they find an upper bound on volatility persistence beyond which the value function does not exist.

<sup>10</sup>The next subsection examines yet another endowment process.

TABLE 2—TIMING PREMIA FOR I.I.D. GROWTH RATE

RRA \ EIS	1.5	1	0.2	0.1
10	9.5%	7.8%	1.0%	0.0%
7.5	6.8%	5.6%	0.4%	-0.5%
5	4.3%	3.5%	0.0%	-0.8%
2	1.2%	0.9%	-0.9%	-1.1%
1	0.4%	0.0%	-1.0%	-1.2%

there is a small probability  $p$  of a negative shock that shrinks consumption by the factor  $b_t$ .<sup>11</sup> Specifically, the consumption process has the following representation:

$$\log \frac{c_{t+1}}{c_t} = m + \sigma W_{c,t+1} + \log(1 - b_t) W_{d,t+1},$$

where  $m$  is mean consumption growth,  $W_{c,t+1} \sim N(0, 1)$ ,  $W_{d,t+1} \sim \text{Bernoulli}(p)$ , and  $b_t$  follows a categorical distribution of disaster sizes obtained from data.<sup>12</sup> All those random variables are mutually independent and i.i.d. over time.

Wachter introduces persistence into this model by assuming that the disaster probability varies over time. Specifically, she assumes that  $W_{d,t+1} \sim \text{Bernoulli}(p_t)$ , where  $p_t = 1 - e^{-\lambda_t}$  and that  $\lambda$  follows the square root process

$$\lambda_{t+1} = (1 - \kappa)\lambda_t + \kappa\bar{\lambda} + \sigma_\lambda \sqrt{\lambda_t} \epsilon_{t+1},$$

where  $\bar{\lambda}$  is the mean value of  $\lambda$ ,  $\kappa$  measures persistence, and  $\sigma_\lambda$  measures the standard deviation.<sup>13</sup>

The parameter values used by Barro (2009) are for an annual frequency:  $RRA = 4$ ,  $EIS = 2$ ,  $p = 0.017$ ,  $m = 0.025$ ,  $\sigma = 0.02$ , and  $\beta = 0.951$ . The distribution of  $b_t$  has mean 0.29, minimum 0.15, maximum 0.73, and was obtained from the author. With these parameter values (and  $T = 200$  for the Monte Carlo simulation) the computed value of the timing premium is 18 percent and the risk premium is 29 percent.<sup>14</sup>

We discretize the parameter values used by Wachter (2013):  $RRA = 3$ ,  $EIS = 1$ ,  $\bar{\lambda} = 0.0355$ ,  $\kappa = 0.08$ ,  $\sigma_\lambda = 0.067$ ,  $m = 0.0252$ ,  $\sigma = 0.02$ , and  $\beta = 0.988$ . The categorical distribution of  $b_t$  has mean 0.22, minimum 0.1, maximum 0.68, and was obtained from the author. With these parameter values (and  $T = 200$  for the Monte Carlo simulation) the computed value of the timing premium is 42 percent and the

<sup>11</sup> He follows Barro (2006) and Rietz (1988).

<sup>12</sup> See also Barro and Jin (2011) who fit power laws to the distribution of disaster sizes; and Tsai and Wachter (2013), who allow for rare booms as well as rare disasters.

<sup>13</sup> Wachter's model is in continuous time. We use a discretized version of her process.

<sup>14</sup> For comparison, we also computed the values for the monthly parametrization and they are close: 19 percent and 29 percent, respectively.

risk premium is 65 percent.<sup>15,16</sup> It is instructive to compare these premium values to those obtained in the model without persistence: setting  $\sigma_\lambda = 0$  and  $\kappa = 1$  yields the timing premium of 22 percent and the risk premium of 46 percent.<sup>17</sup> Thus allowing for long-run shocks to the probability of disasters heavily inflates both premia.

*What about Other Preference Parameter Values?*—Are there parameter values that allow for sensible values of the timing premium and at the same time provide a good fit of the asset pricing data? Surely, setting EIS in the vicinity of the reciprocal of RRA leads to a small timing premium. With a high RRA needed to accommodate a high equity premium, this would require that EIS be significantly below 1. However, Bansal and Yaron (2004) point out that in their model EIS below 1 would lead to excessive levels and/or volatility for the risk-free rate. This is also true in the variable rare disaster model of Wachter (2013). In addition, Barro (2009) points out that EIS below 1 leads to the counterfactual prediction that an increase in economic uncertainty would lead to an increase in price-dividend ratios. It is possible that there exists a model of the endowment process that fits asset pricing data well with EIS smaller than 1; however, we are not aware of such a process.

*More General Risk Preferences.*—In (1)–(2) and in the Kreps-Porteus model more generally, risk preferences are in the vNM class. Epstein and Zin (1989) describe a more general class of recursive utility functions in which risk preferences that are consistent with the Allais paradox are also permitted. Some of these specifications have been used to address the equity premium and related puzzles (references are given below). Therefore, we explore briefly the quantitative implications of such generalizations for timing premia.

To preserve simplicity while generalizing preferences, as well as for the convenience of closed forms and for the clarity of intuition delivered thereby, we simplify the endowment process and assume that the (log) growth rate is i.i.d. with  $\log(c_{t+1}/c_t)$  distributed as  $N(m, \sigma^2)$ . Generalize (2) and consider utility defined by:

$$(6) \quad \log U_t = (1 - \beta) \log c_t + \beta \log \mu(U_{t+1}).$$

Here  $\mu(\cdot)$  is the certainty equivalent of random future utility using its conditional distribution at time  $t$ .<sup>18</sup> Assume that  $\mu(x) = x$  for any deterministic random variable  $x$ , that  $\mu$  respects first-order and second-order stochastic dominance, and that  $\mu$  is linearly homogeneous (constant relative risk aversion).

It is convenient to use the renormalized certainty equivalent  $\mu^*$ , where for any positive random variable  $X$  and associated distribution,  $\mu^*(\log X) \equiv \log \mu(X)$ .

<sup>15</sup> As in our LRR calculations, we compute the value of the timing premium and the risk premium for an initial value of the state variable corresponding to the modal point of the state space  $\lambda_0 = \bar{\lambda}$ .

<sup>16</sup> As in the case of the Bansal-Yaron model, we compute the value of early resolution by Monte Carlo simulations. To compute the value of gradual resolution we use value iteration.

<sup>17</sup> The difference between these numbers and those that we obtain for Barro's specification can be accounted for by the different preference parameters and slightly different empirical distributions of disaster sizes.

<sup>18</sup> In general it depends on the information at  $t$ , but with the i.i.d. assumption such time dependence can be safely suppressed.

Then (see the Appendix) the timing premium is given in closed-form by  $\pi^* = 1 - \exp(-\beta\Delta)$ , where

$$(7) \quad \Delta \equiv \mu^*(\sum_0^\infty \beta^t \log(c_{t+1}/c_t)) - (1 - \beta)^{-1} \mu^*(\log(c_1/c_0)).$$

For the expected utility-based certainty equivalent,  $\mu^*(\log X) = \frac{1}{\alpha} \log E(X_{t+1}^\alpha)$ , and one obtains the Epstein-Zin implied timing premium; denote the corresponding  $\Delta$  by  $\Delta_{EZ}$ .

As an alternative, consider the following *disappointment aversion* certainty equivalent:<sup>19</sup> Fix  $0 < \gamma \leq 1$ , and for any positive random variable  $X$  (with distribution  $P$ ), define  $\mu_{da}(X)$  implicitly by

$$\log \mu_{da}(X) = E \log(X) - (\gamma^{-1} - 1) \int_{x \leq \mu_{da}(X)} (\log \mu_{da}(X) - \log x) dP(x),$$

or equivalently, (let  $Y = \log X$  and  $Q$  its induced distribution),

$$(8) \quad \mu_{da}^*(Y) = EY - (\gamma^{-1} - 1) \int_{y \leq \mu_{da}^*(Y)} (\mu_{da}^*(Y) - y) dQ(y).$$

The interpretation is that outcomes of  $X$  that are disappointing because they fall below the certainty equivalent are penalized relative to  $E \log(X)$ . If  $\gamma = 1$ , then  $\mu(X) = E \log(X)$  and, when substituted into (6), one obtains the expected utility model where  $RRA = EIS = 1$ . Accordingly, nonindifference to timing arises herein only from the disappointment factor when  $\gamma < 1$ . Because the latter adds to risk aversion, the effective degree of risk aversion is greater than 1. We compare this way of increasing risk aversion to using Epstein-Zin utility with  $\alpha < 0$ .

We show in the Appendix that the difference  $\Delta$  in (7), written now  $\Delta_{da}$ , can be expressed in the form

$$(9) \quad \Delta_{da} = \frac{m - \mu_{da}^*(\log(c_1/c_0))}{1 - \beta} \left( 1 - \left[ \frac{1 - \beta}{1 + \beta} \right]^{1/2} \right),$$

which expression involves the certainty equivalent of the single-period gamble only. Compare  $\Delta_{EZ}$  and  $\Delta_{da}$  to see the differing implications for timing premia of the expected utility versus disappointment aversion risk preferences. A meaningful comparison requires that the respective parameters  $\alpha$  and  $\gamma$  be suitably related. For example, suppose that the two certainty equivalents assign the same value to the

<sup>19</sup>The model is due to Gul (1991). For applications to finance, see Epstein and Zin (2001); and Ang, Bekaert, and Liu (2005). Routledge and Zin (2010) present and apply a generalization, which is investigated further empirically by Bonomo et al. (2011). See also Epstein and Zin (1990); and Bekaert, Hodrick, and Marshall (1997).

distribution of  $\log(c_1/c_0)$ . Then substitute  $\mu_{da}^*(\log(c_1/c_0)) = m + \frac{1}{2}\alpha \cdot \sigma^2$  into (9) to deduce that

$$(10) \quad \Delta_{da} = \left(1 - \left[\frac{1 - \beta}{1 + \beta}\right]^{1/2}\right) \frac{1 + \beta}{\beta} \Delta_{EZ} \simeq 2\Delta_{EZ}.$$

Roughly, disappointment aversion implies timing premia twice as large as those reported in Table 2 when  $\gamma$  is calibrated as described to  $\alpha = -9, -4, -1$ .

An alternative calibration is to assume that the two certainty equivalents assign the same value to the distribution of  $\sum_0^\infty \beta^t \log(c_{t+1}/c_t)$ . Then similar reasoning leads to the relation

$$(11) \quad \Delta_{da} = \frac{1}{\beta} \left( \left[\frac{1 + \beta}{1 - \beta}\right]^{1/2} - 1 \right) \Delta_{EZ} \simeq 30\Delta_{EZ},$$

and hence to much larger timing premia under disappointment aversion. (For example, the timing premium for  $\gamma$  that corresponds to  $\alpha = -1$  is about 23 percent.) Thus with either calibration, timing premia are larger than with Epstein-Zin utility.

The Appendix shows that (10) and (11) are valid for a broader class of risk preferences.

### III. Concluding Remarks

Though risk aversion and the elasticity of intertemporal substitution have been the subjects of careful scrutiny when calibrating preferences, the long-run risks literature and the broader literature using recursive utility to address asset pricing puzzles have ignored the full implications of their parameter specifications. Recursive utility implies that the temporal resolution of risk matters and a quantitative assessment of how much it matters should be part of the calibration process. This paper is not intended to provide an exhaustive or definitive assessment of parameters used in the literature. Its objective is to give a sense of the magnitudes of implied timing premia and to inject temporal resolution of risk into the discussion of the quantitative properties of LRR and related models.

Timing premia depend on both the parameters of preference and on the nature of the endowment process. In the latter connection, we have demonstrated that, given Epstein-Zin utility, high persistence of the consumption process—as assumed in the LRR literature or in a version of the rare disaster model (Wachter 2013)—inflates timing premia to levels that seem implausible to us based on introspection (20–30 percent in the former case and 40 percent in the latter case). Though some may disagree with this admittedly subjective judgement, we believe that we have at least alerted readers to the need to be more cautious when calibrating asset pricing models that rely on nonindifference to temporal resolution as a key component. There are endowment and parameter specifications that imply much smaller timing premia, but while they can account for some asset pricing moments, they yield

counterfactual predictions for others. Another alternative is to seek a different model of preference. In Epstein-Zin utility (1) and (2), the two parameters  $\alpha$  and  $\rho$  govern three seemingly distinct aspects of preference, with the result that setting them to match values for EIS and RRA yields timing premia that are beyond direct control of the analyst. This limitation has been recognized from the start in Epstein and Zin (1989), but this paper may provide renewed impetus to the search for a more flexible model of preference.

For other thought experiments that reflect on parameter values in the LRR model, see D'Addona and Brevik (2011) and Ai (2007). D'Addona and Brevik assert that an agent with Epstein-Zin utility achieves higher utility levels if he can commit to ignoring information about the state variable  $x_t$  appearing in (4). Though they describe their results as concerning information, their analysis does not admit that interpretation: instead of changing the information structure of the agent, they endow the agent with a different consumption process that does not involve long-run risk (and has the appropriately adjusted unconditional variance). Thus, they de facto study aversion to autocorrelation of consumption instead of the (conceptually distinct) preference for ignoring information or nonindifference to the temporal resolution of risk. In a continuous-time economy with production, Ai (2007) considers the preference for early resolution from a quantitative perspective by asking how much consumption the agent is willing to forgo to learn perfectly the autocorrelated component of the production process instead of having just a noisy signal of it. Our starker thought experiment, where early resolution means that all risk is fully resolved, and the discrete-time exchange economy setting, arguably permits a sharper focus and makes it easier for introspection to operate. (See Section II for our related comments on whether introspection is useful.)

An important alternative to models based on recursive utility is the external habits model of Campbell and Cochrane (1999). Corresponding scrutiny of that model seems in order. Thus far plausibility of the habits formation process assumed for the representative agent has been judged solely by how it helps to match asset market data. The discipline urged by Mehra and Prescott (1985) suggests that at least one should examine also whether it seems plausible based on introspection about the quantitative effects of past consumption on current preferences. The difficulty of finding market-based evidence concerning external habits, or about timing premia, does not justify leaving them as *free parameters*.

#### APPENDIX: DETAILS FOR MORE GENERAL RISK PREFERENCES

To derive (7), use the fact that utilities are given by

$$\log U_0 = \log c_0 + \beta \left[ \frac{1}{1 - \beta} \mu^*(\log (c_1/c_0)) \right]$$

$$\log U_0^* = \log c_0 + \beta \left[ \mu^*(\sum_0^\infty \beta^t \log (c_{t+1}/c_t)) \right].$$

Let  $Y = \log(c_1/c_0)$  and  $Y' = \sum_0^\infty \beta^t \log(c_{t+1}/c_t)$ . They are distributed as  $N(m, \sigma^2)$  and  $N\left(\frac{m}{1-\beta}, \frac{\sigma^2}{1-\beta^2}\right)$ , respectively. Therefore,

$$Y'' \equiv (1 - \beta^2)^{1/2} Y' - m \left( \left[ \frac{1 + \beta}{1 - \beta} \right]^{1/2} - 1 \right) \text{ is } N(m, \sigma^2).$$

Because  $\mu_{da}(Y'')$  and  $\mu_{da}(Y)$  depend only on the distributions of  $Y''$  and  $Y$ , they must be equal. Note that  $\mu_{da}^*$  satisfies: for all  $\lambda \geq 0$ ,

$$(A1) \quad \mu_{da}^*(Y + \lambda) = \mu_{da}^*(Y) + \lambda \quad \text{and} \quad \mu_{da}^*(\lambda Y) = \lambda \mu_{da}^*(Y),$$

that is, it exhibits both CARA (constant absolute risk aversion) and CRRA (constant relative risk aversion). Conclude that the two certainty-equivalent values appearing in (7) are related by the equation

$$(A2) \quad (1 - \beta^2)^{1/2} \mu_{da}^*\left(\sum_0^\infty \beta^t \log(c_{t+1}/c_t)\right) - \mu_{da}^*(\log(c_1/c_0)) \\ = m \left( \left[ \frac{1 + \beta}{1 - \beta} \right]^{1/2} - 1 \right).$$

The preceding, and hence also equations (10) and (11), rely only on lognormality and on the fact that  $\mu_{da}^*$  satisfies (A1). Thus the comparative analysis of timing premia applies to any certainty equivalent function satisfying the latter properties. For example, it applies also to the following generalization of (8):

$$\mu_{gda}^*(Y) = EY - (\gamma^{-1} - 1) \int_{y \leq \delta \mu_{gda}^*(Y)} (\delta \mu_{gda}^*(Y) - y) dQ(y),$$

where  $0 < \delta \leq 1$ . Here outcomes are disappointing if they are smaller than the fraction  $\delta$  of the certainty equivalent. This generalization of disappointment aversion (which corresponds to the special case  $\delta = 1$ ) is in the spirit of that provided by Routledge and Zin (2010). (In our setting, their model would take the form  $\mu_{RZ}^*(Y) = EY - (\gamma^{-1} - 1) \int_{y \leq \log \delta + \mu_{RZ}^*(Y)} (\log \delta + \mu_{RZ}^*(Y) - y) dQ(y)$ , which violates the second condition in (A1)).

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