



Complex Networks

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Roadmap

- Introduction
- Data processing
- Machine learning models
- Experimental procedure
- Performance evaluation
- Conclusion and References



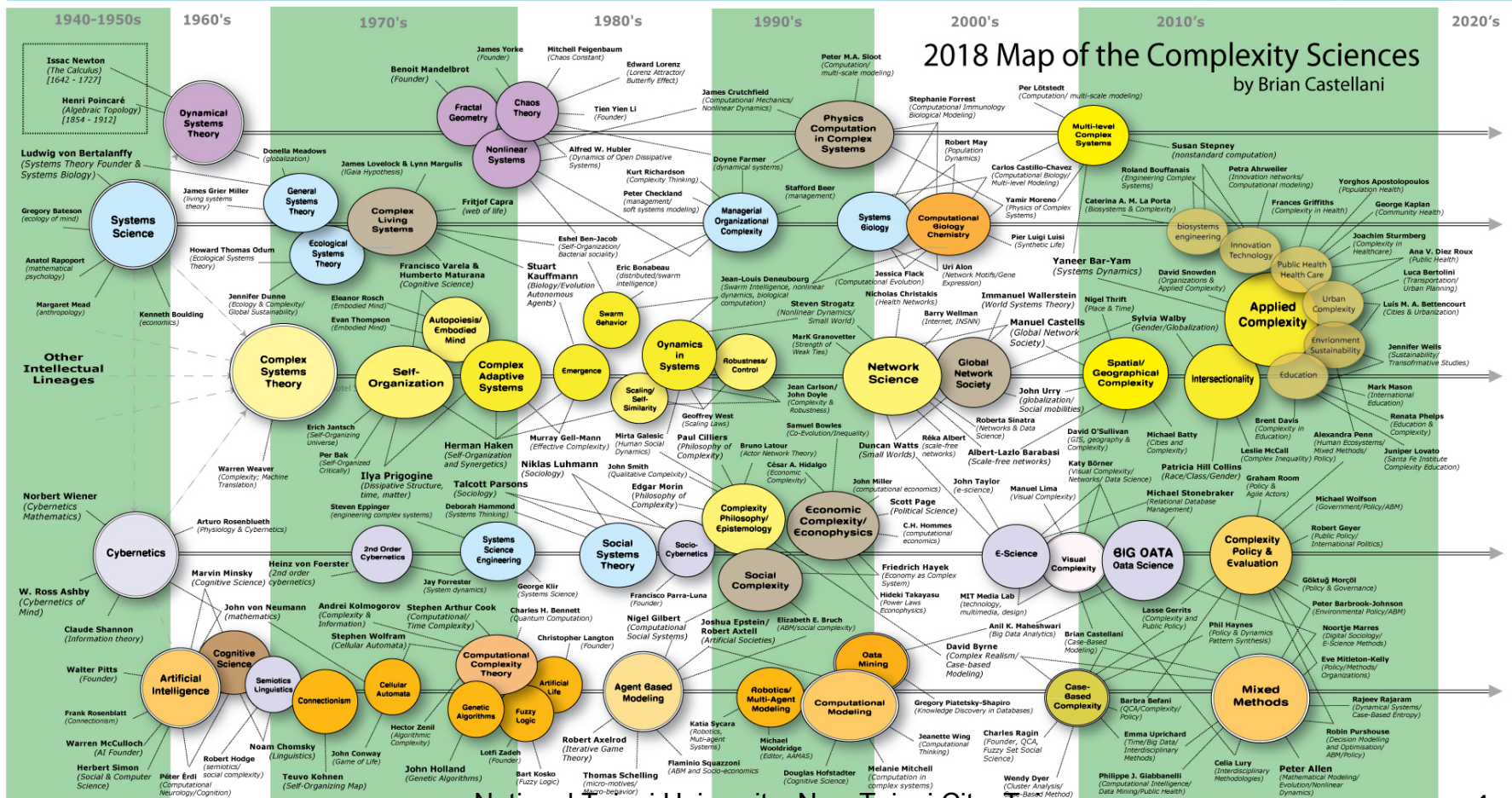
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Complex Systems



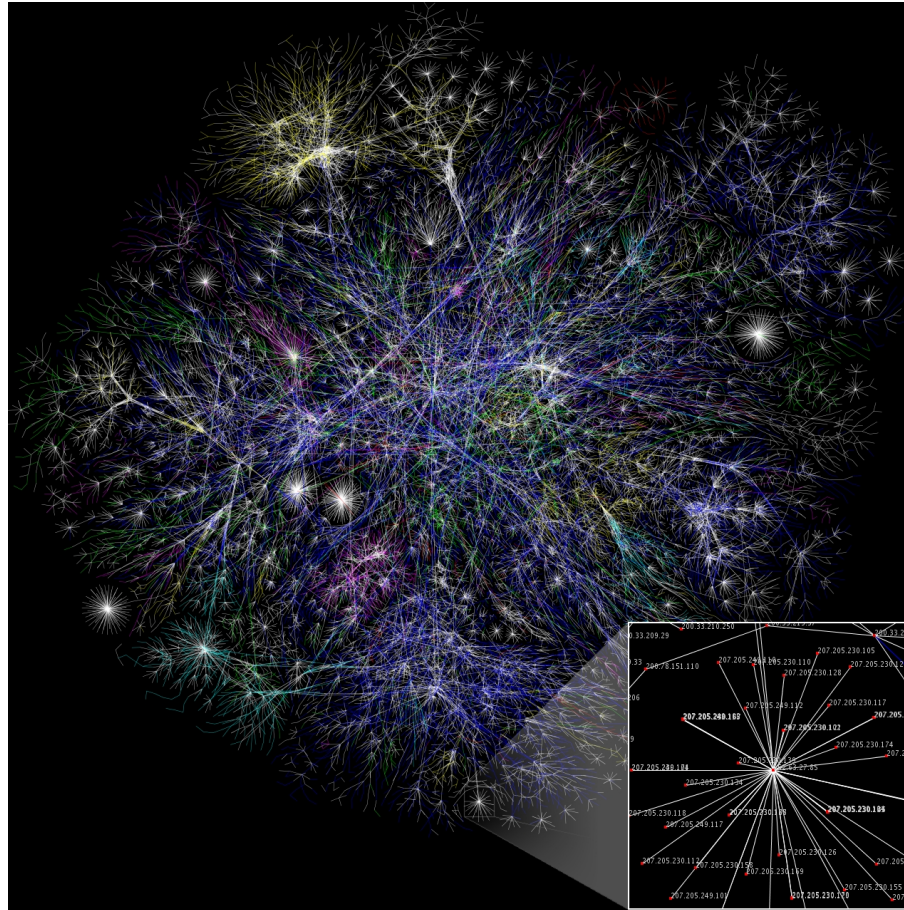
See below on how to read map!



National Taipei University, New Taipei City, Taiwan

[illegible]

The Internet



https://en.wikipedia.org/wiki/Complex_network#/media/File:Internet_map_1024.jpg
By The Opte Project - Originally from the English Wikipedia
<https://commons.wikimedia.org/w/index.php?curid=1538544>



The Internet

- Partial map of the Internet based on the January 15, 2005 data found on opte.org.
- Each line is drawn between two nodes, representing two IP addresses.
- The length of the lines are indicative of the delay between those two nodes.
- This graph represents less than 30% of the Class C networks reachable by the data collection program in early 2005.
- Lines are color-coded according to their corresponding RFC 1918 allocation as follows: Dark blue: net, ca, us Green: com, org Red: mil, gov, edu Yellow: jp, cn, tw, au, de Magenta: uk, it, pl, fr Gold: br, kr, nl White: unknown

Scale-Free Networks

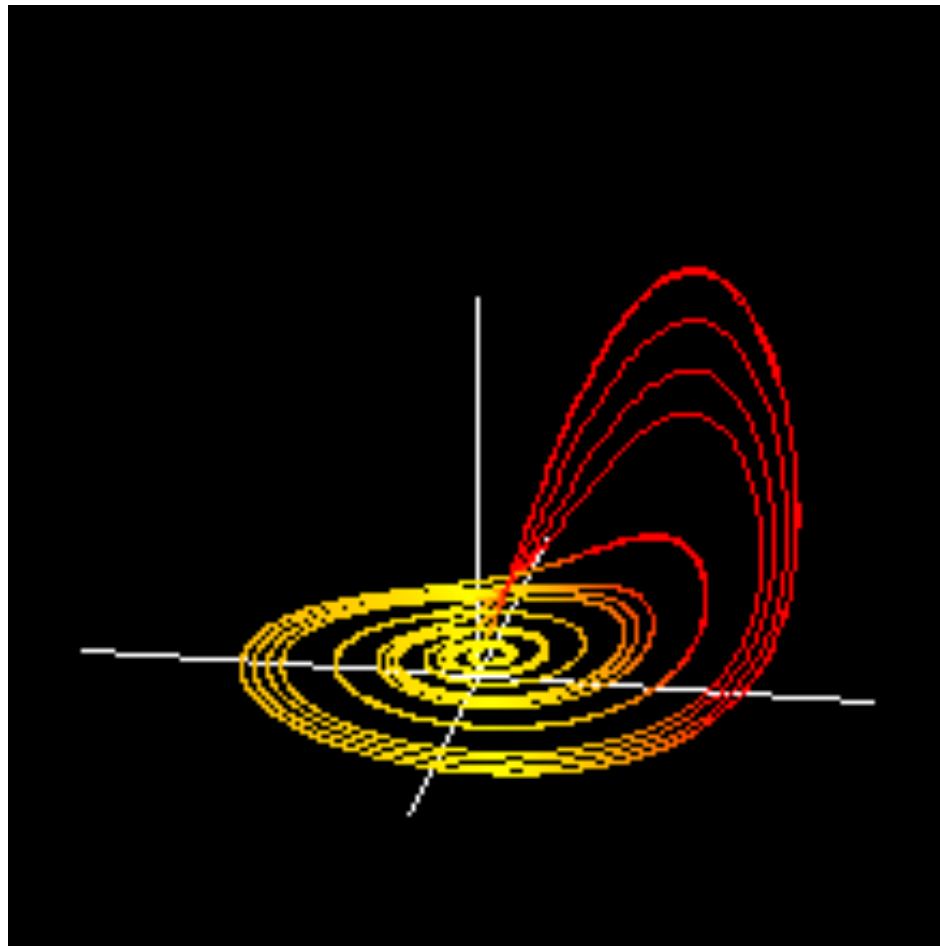




Scale-Free Network

- An example of complex scale-free network.
- Graph represents the metadata of thousands of archive documents, documenting the social network of hundreds of League of Nations personals.
- M. Grandjean, "La connaissance est un réseau," *Les Cahiers du Numérique*, vol. 10, no. 3, pp. 37-54.

Dynamical Systems





Dynamical Systems

- The Rössler attractor is a chaotic attractor solution to the system:

$$\dot{x} = -y - z$$

$$\dot{y} = x + ay$$

$$\dot{z} = b + z(x - c)$$

- Proposed by Rössler in 1976
- Often called *Rössler system*
- Here, $(x, y, z) \in \mathbb{R}^3$ are dynamical variables defining the phase space and $(a, b, c) \in \mathbb{R}^3$ are parameters



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Machine Learning

- Using machine learning techniques to detect network intrusions is an important topic in cybersecurity.
- Machine learning algorithms have been used to successfully classify network anomalies and intrusions.
- Supervised machine learning algorithms:
 - Support vector machine: SVM
 - Long short-term memory: LSTM
 - Gated recurrent unit: GRU
 - Broad learning system: BLS



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BGP and NSL-KDD Datasets

- Used to evaluate anomaly detection and intrusion techniques
- **BGP:**
 - Routing records from Réseaux IP Européens (RIPE)
 - BCNET regular traffic
- **NSL-KDD:**
 - an improvement of the KDD'99 dataset
 - used in various intrusion detection systems (IDSs)



BGP Datasets

- Anomalous data: **days of the attack**
- Regular data: **two days prior and two days after the attack**
- **37** numerical features from BGP update messages
- Best performance: **60%** for training and **40%** for testing

	Regular (min)	Anomaly (min)	Regular (training)	Anomaly (training)	Regular (test)	Anomaly (test)
Code Red I	6,599	600	3,678	362	2,921	239
Nimda	3,678	3,521	3,677	2,123	1	1,399
Slammer	6,330	869	3,209	531	3121	339



NSL-KDD Dataset

- KDDTrain+ and KDDTest+: training and test datasets
- KDDTes⁻²¹: a subset of the KDDTest+ dataset that does not include records correctly classified by 21 models

	Regular	DoS	U2R	R2L	Probe	Total
KDDTrain ⁺	67,343	45,927	52	995	11,656	125,973
KDDTest ⁺	9,711	7,458	200	2,754	2,421	22,544
KDDTest ⁻²¹	2,152	4,342	200	2,754	2,402	11,850

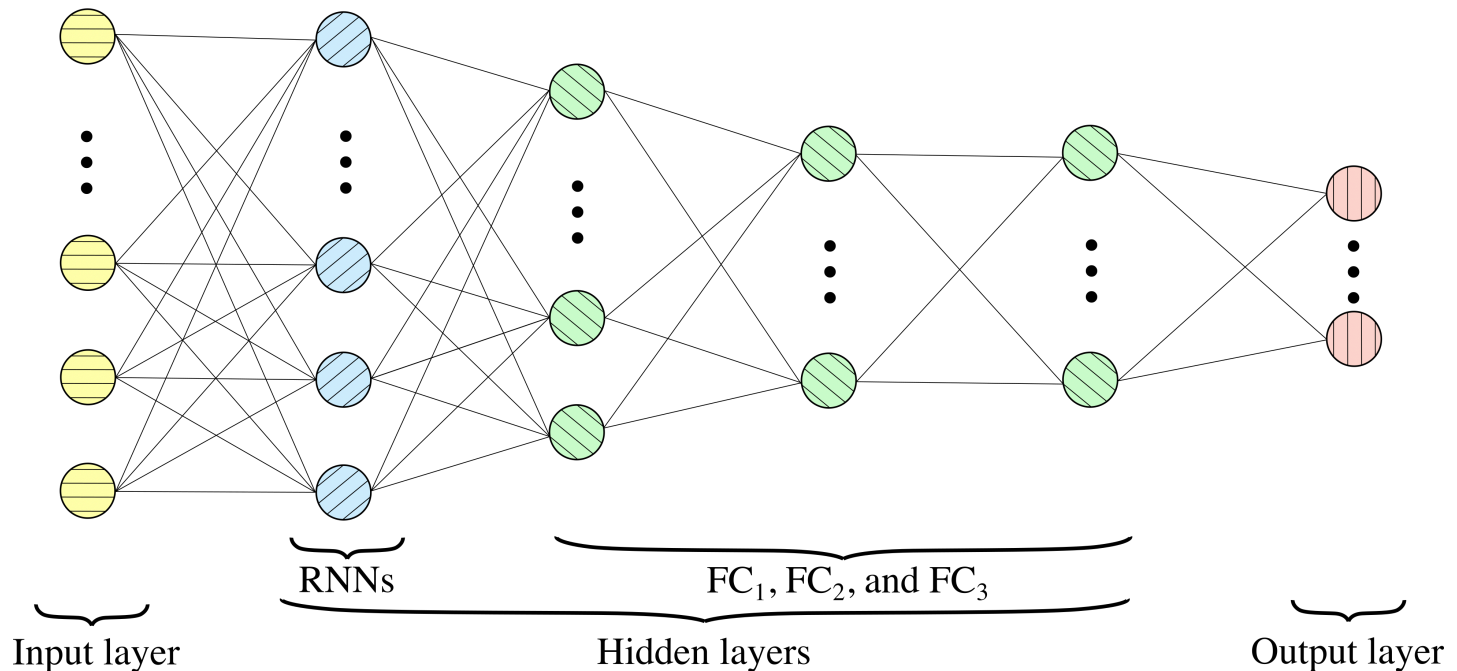


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 - Deep learning: multi-layer recurrent neural networks
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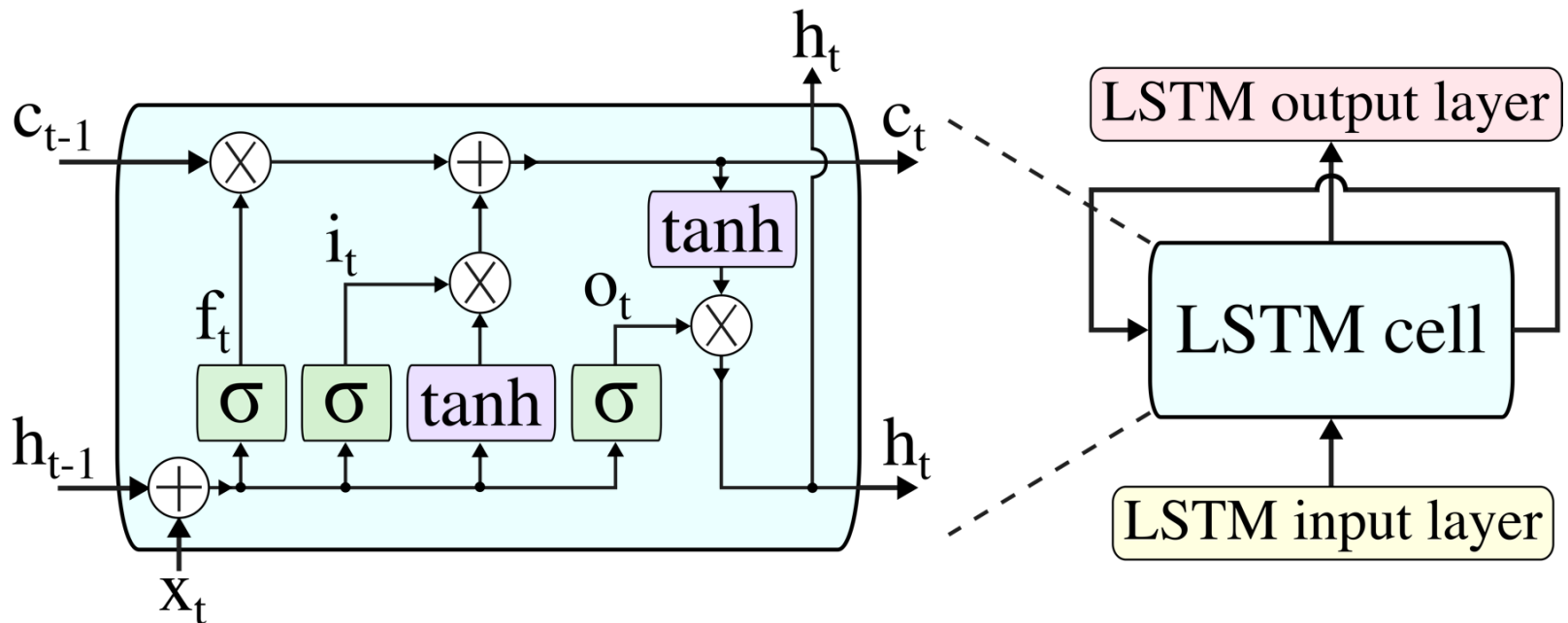
Deep Learning Neural Network

- 37 (BGP)/109 (NSL-KDD) RNNs, 80 FC_1 , 32 FC_2 , and 16 FC_3 fully connected (FC) hidden nodes:



Long Short-Term Memory: LSTM

- Repeating module for the Long Short-Term Memory (LSTM) neural network:





Long Short-Term Memory: LSTM

- The outputs of the forget gate f_t , the input gate i_t , and the output gate o_t at time t are:

$$f_t = \sigma(W_{if}x_t + b_{if} + U_{hf}h_{t-1} + b_{hf})$$

$$i_t = \sigma(W_{ii}x_t + b_{ii} + U_{hi}h_{t-1} + b_{hi})$$

$$o_t = \sigma(W_{io}x_t + b_{io} + U_{ho}h_{t-1} + b_{ho}),$$

where:

$\sigma(\cdot)$: logistic sigmoid function

x_t : current input vector

h_{t-1} : previous output vector

W_{if} , U_{hf} , W_{ii} , U_{hi} , W_{io} and U_{ho} : weight matrices

b_{if} , b_{hf} , b_{ii} , b_{hi} , b_{io} , and b_{ho} : bias vectors



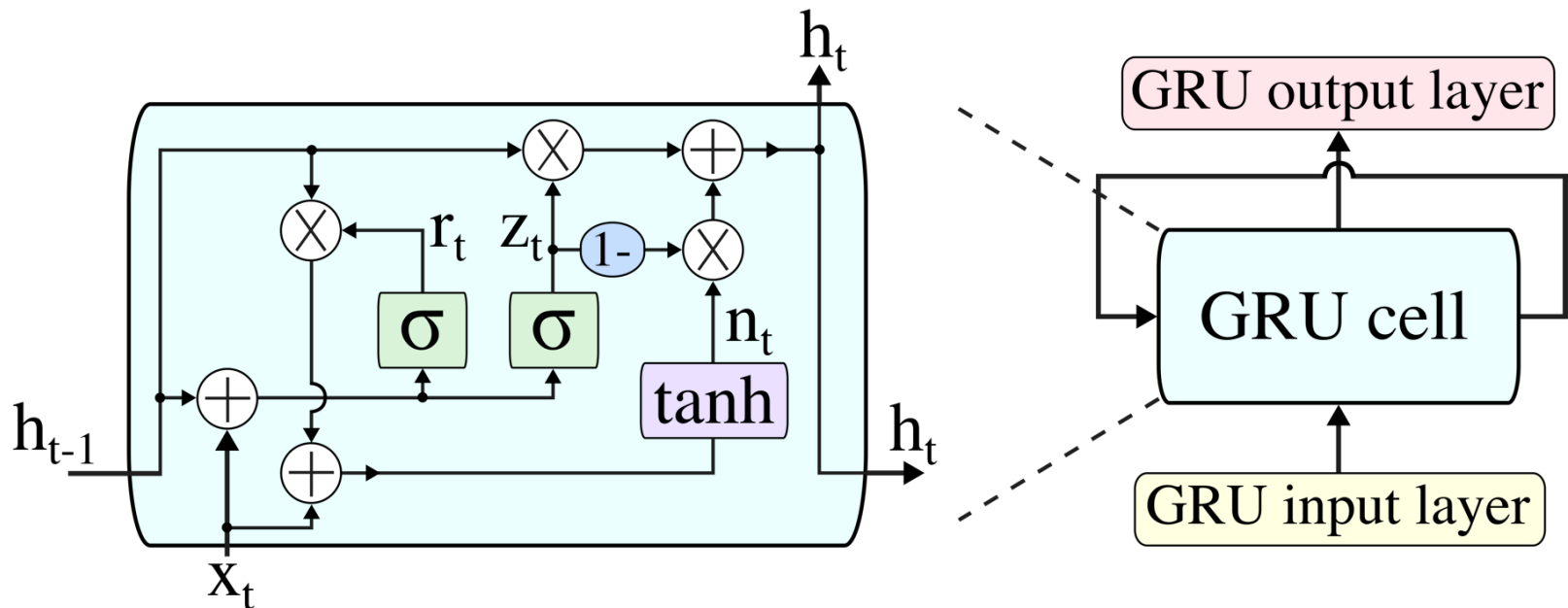
Long Short-Term Memory: LSTM

- Output i_t of the input gate decides if the information will be stored in the cell state. The sigmoid function is used to update the information.
- Cell state c_t :
$$c_t = f_t * c_{t-1} + i_t * \tanh(W_{ic}x_t + b_{ic} + U_{hc}h_{t-1} + b_{hc}),$$
where:

- $*$ denotes element-wise multiplications
- \tanh function: used to create a vector for the next cell state
- Output of the LSTM cell:
$$h_t = o_t * \tanh(c_t)$$

Gated Recurrent Unit: GRU

- Repeating module for the Gated Recurrent Unit (GRU) neural network:





Gated Recurrent Unit: GRU

- The outputs of the reset gate r_t and the update gate z_t at time t are:

$$r_t = \sigma(W_{ir}x_t + b_{ir} + U_{hr}h_{t-1} + b_{hr})$$
$$z_t = \sigma(W_{iz}x_t + b_{iz} + U_{hz}h_{t-1} + b_{hz}),$$

where:

- σ : sigmoid function
- x_t : input, h_{t-1} is the previous output of the GRU cell
- W_{ir} , U_{hr} , W_{iz} , and U_{hz} : weight matrices
- b_{ir} , b_{hr} , b_{iz} , and b_{hz} : bias vectors



Gated Recurrent Unit: GRU

- Output of the GRU cell:

$$h_t = (1 - z_t) * n_t + z_t * h_{t-1},$$

where n_t :

- $n_t = \tanh(W_{in}x_t + b_{in} + r_t * (U_{hn}h_{t-1} + b_{hn}))$
- W_{in} and U_{hn} : weight matrices
- b_{in} and b_{hn} : bias vectors

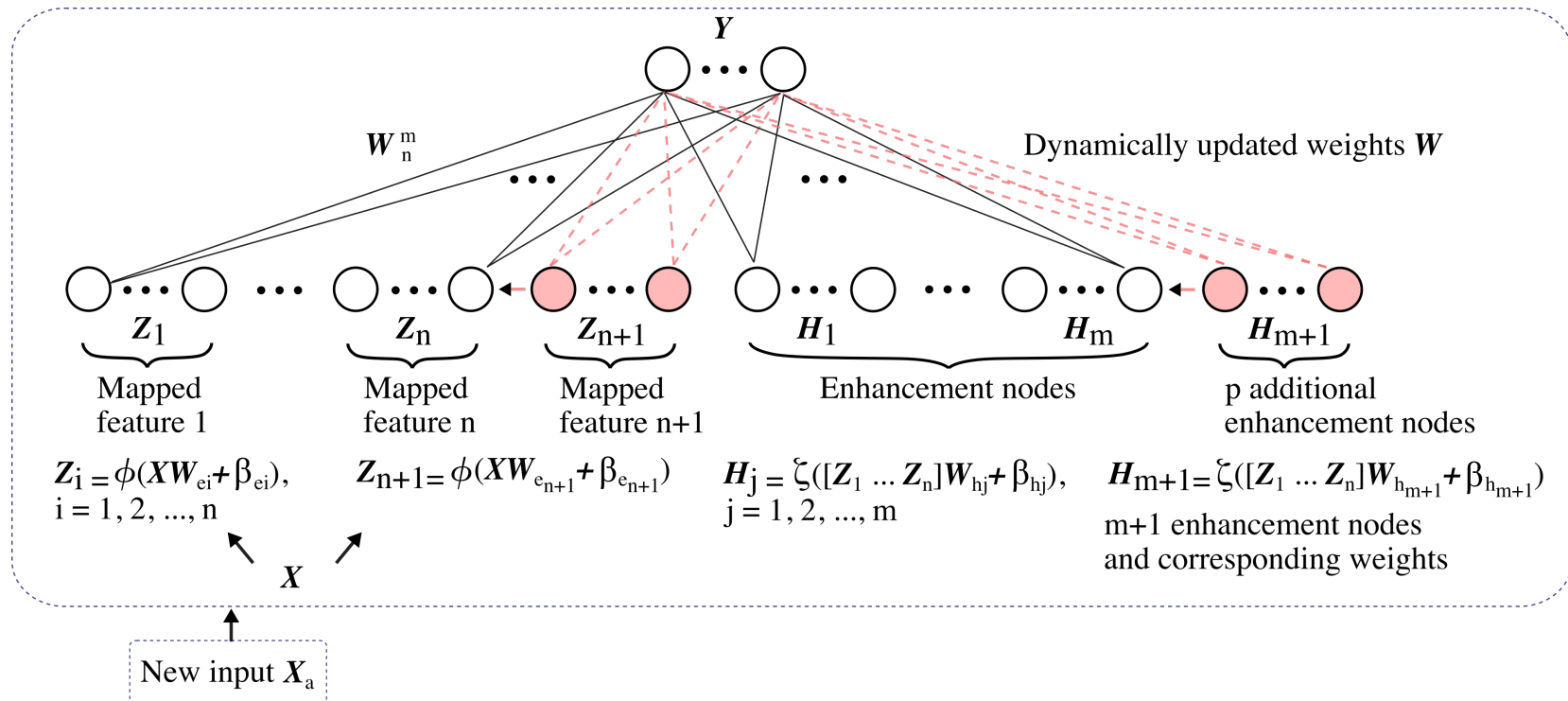


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Broad Learning System: BLS

- Module of the Broad Learning System (BLS) algorithm with increments of mapped features, enhancement nodes, and new input data:





Original BLS

- Matrix \mathbf{A}_x is constructed from groups of mapped features \mathbf{Z}^n and groups of enhancement nodes \mathbf{H}^m as:

$$\begin{aligned}\mathbf{A}_x &= [\mathbf{Z}^n \mid \mathbf{H}^m] \\ &= [\phi(\mathbf{X}\mathbf{W}_{ei} + \beta_{ei}) \mid \xi(\mathbf{Z}_x^n \mathbf{W}_{hj} + \beta_{hj})],\end{aligned}$$

where: $i = 1, 2, \dots, n$ and $j = 1, 2, \dots, m$

- ϕ and ξ : projection mappings
- \mathbf{W}_{ei} , \mathbf{W}_{hj} : weights
- β_{ei} , β_{hj} : bias parameters

Modified to include additional **mapped features** \mathbf{Z}_{n+1} , **enhancement nodes** \mathbf{H}_{m+1} , and/or **input nodes** \mathbf{X}_a



RBF-BLS Extension

- The **RBF function** is implemented using Gaussian kernel:

$$\xi(x) = \exp\left(-\frac{\|x - c\|^2}{\gamma^2}\right)$$

- Weight vectors of the output \mathbf{HW} are deduced from:

$$\begin{aligned}\mathbf{W} &= (\mathbf{H}^T \mathbf{H})^{-1} \mathbf{H}^T \mathbf{Y} \\ &= \mathbf{H}^+ \mathbf{Y},\end{aligned}$$

where:

- $\mathbf{W} = [\omega_1, \omega_2, \dots, \omega_k]$: output weights
- $\mathbf{H} = [\xi_1, \xi_2, \dots, \xi_k]$: hidden nodes
- \mathbf{H}^+ : pseudoinverse of \mathbf{H}



Cascades of Mapped Features

- **Cascade of mapped features (CFBLS):**
the new group of mapped features is created by using the previous group ($k - 1$).
- Groups of mapped features are formulated as:

$$\begin{aligned} \mathbf{Z}_k &= \phi(\mathbf{Z}_{k-1} \mathbf{W}_{ek} + \beta_{ek}) \\ &\triangleq \phi^k(\mathbf{X}; \{\mathbf{W}_{ei}, \beta_{ei}\}_{i=1}^k), \text{ for } k = 1, \dots, n \end{aligned}$$



Cascades of Enhancement Nodes

- The first enhancement node in **cascade of enhancement nodes (CEBLS)** is generated from mapped features.
- The subsequent enhancement nodes are generated from previous enhancement nodes creating a cascade:

$$H_u \triangleq \xi^u(\mathbf{Z}^n; \{\mathbf{W}_{hi}, \beta_{hi}\}_{i=1}^u), \text{ for } u = 1, \dots, m,$$
where:

- \mathbf{W}_{hi} and β_{hi} : randomly generated



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Experimental Procedure

- **Step 1:** Normalize training and test datasets.
- **Step 2:** Train the RNN models and BLS using 10-fold validation. Tune parameters of the RNN and BLS models.
- **Step 3:** Test the RNN and BLS models.
- **Step 4:** Evaluate models based on:
 - Accuracy
 - F-Score

RNN: recurrent neural network
BNN: board learning system



Number of **BLS** Training Parameters

Parameters	Code Red I	Nimda	Slammer	NSL-KDD
Mapped features	100	500	100	100
Groups of mapped features	1	1	25	5
Enhancement nodes	500	700	300	100
Incremental learning steps	10	9	2	3
Data points/step	100	200	100	3,000
Enhancement nodes/step	10	10	50	60



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Training Time: RNN Models

Datasets

LSTM₂

LSTM₃

LSTM₄

GRU₂

GRU₃

GRU₄

Python (CPU)

Time (s)

BGP (Slammer)

224.52

259.91

819.78

54.12

60.76

759.82

NSL-KDD

4,481.73

4,614.66

11,478.62

1,108.31

1,161.80

11,581.30

Python (GPU)

Time (s)

BGP (Slammer)

30.74

34.94

38.82

31.03

35.46

40.22

NSL-KDD

344.93

355.86

394.55

317.53

345.04

369.86



Training Time: BLS Models

Datasets		BLS	RBF-BLS	CFBLS	CEBLS	CFEBLS
Python (CPU)						
Time (s)	BGP (Slammer)	21.53	18.68	18.89	32.36	32.13
	NSL-KDD	99.47	98.27	98.13	108.23	108.14
MATLAB (CPU)						
Time (s)	BGP (Slammer)	1.36	1.20	1.03	5.49	5.98
	NSL-KDD	6.91	6.24	6.55	8.88	8.95

LSTM Models: BGP Datasets (Python)

Model	Training Dataset	Accuracy (%)			F-Score (%)
		Test	RIPE (regular)	BCNET (regular)	Test
LSTM ₂	Code Red I	94.08	83.75	60.49	68.89
	Nimda	78.36	47.15	48.61	87.87
	Slammer	92.98	92.99	85.97	72.42
LSTM ₃	Code Red I	88.54	79.38	58.82	55.96
	Nimda	85.57	39.10	40.28	92.22
	Slammer	90.90	92.01	84.38	67.29
LSTM ₄	Code Red I	86.96	75.00	57.01	51.53
	Nimda	92.00	26.94	35.21	95.83
	Slammer	92.49	92.22	86.18	70.72

GRU Models: BGP Datasets (Python)

Model	Training Dataset	Test	Accuracy (%)		F-Score (%)
			RIPE (regular)	BCNET (regular)	Test
GRU ₂	Code Red I	87.47	80.07	60.21	52.97
	Nimda	70.71	48.96	58.26	82.83
	Slammer	91.88	93.33	90.90	69.42
GRU ₃	Code Red I	88.07	79.44	60.56	53.51
	Nimda	80.21	38.40	44.24	89.02
	Slammer	91.76	95.21	90.83	68.72
GRU ₄	Code Red I	91.84	77.50	60.07	63.87
	Nimda	87.36	35.00	39.38	93.25
	Slammer	92.14	92.15	90.35	70.11



BLS Models: BGP Datasets (Python)

Model	Training Dataset	Test	Accuracy (%)		F-Score (%)
			RIPE (regular)	BCNET (regular)	Test
BLS	Code Red I	94.97	69.79	65.21	66.38
	Nimda	76.57	70.69	54.93	86.73
	Slammer	87.65	75.62	68.40	57.68
RBF-BLS	Code Red I	95.92	90.69	73.96	70.07
	Nimda	57.92	70.63	57.22	73.36
	Slammer	91.21	90.55	70.76	64.57

BLS Models: BGP Datasets (Python)

Model	Training Dataset	Accuracy (%)			F-Score (%)
		Test	RIPE (regular)	BCNET (regular)	Test
CFBLS	Code Red I	95.16	69.38	61.74	71.08
	Nimda	55.71	68.06	58.26	71.56
	Slammer	89.28	71.25	61.81	60.99
CEBLS	Code Red I	94.94	70.69	60.35	65.22
	Nimda	66.43	74.10	54.51	79.83
	Slammer	91.01	87.71	82.43	66.38
CFEBLS	Code Red I	95.66	70.07	59.51	71.75
	Nimda	64.29	70.83	57.43	78.24
	Slammer	86.36	71.11	57.71	55.30



RNN and BLS Models: NSL-KDD Dataset (Python)

Model	Accuracy (%)		F-Score (%)	
	KDDTest ⁺	KDDTest ⁻²¹	KDDTest ⁺	KDDTest ⁻²¹
LSTM ₄	82.78	66.74	83.34	76.21
GRU ₃	82.87	65.42	83.05	74.06
CFBLS	82.20	67.47	82.23	76.29



Incremental BLS Model: BGP and NSL-KDD Datasets (MATLAB)

Test	Accuracy (%)	F-Score (%)	Time (s)
Code Red I	94.37	65.10	0.926
Nimda	91.64	95.64	2.757
Slammer	89.31	63.07	2.805
KDDTest ⁺	81.34	81.99	32.99
KDDTest ⁻²¹	78.70	88.06	29.71



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Conclusion

- We evaluated performance of:
 - **LSTM** and **GRU** deep recurrent neural networks with a variable number of hidden layers
 - **BLS** models that employ radial basis function (RBF), cascades of mapped features and enhancement nodes, and incremental learning
- **BLS** and **cascade combinations of mapped features and enhancement nodes** achieved comparable performance and shorter training time because of their wide and deep structure.



Conclusion

- BLS models:
 - consist of a small number of hidden layers and adjust weights using pseudoinverse instead of back-propagation
 - dynamically update weights in case of incremental learning
 - better optimized weights due to additional data points for large datasets (NSL-KDD)
- While increasing the number of mapped features and enhancement nodes as well as mapped groups led to better performance, it required additional memory and training time.



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References: Datasets

- BCNET :
<http://www.bc.net/>
- RIPE RIS raw data:
<https://www.ripe.net/analyse/internet-measurements/routing-information-service-ris>
- NSL-KDD dataset:
<https://www.unb.ca/cic/datasets/nsf.html>
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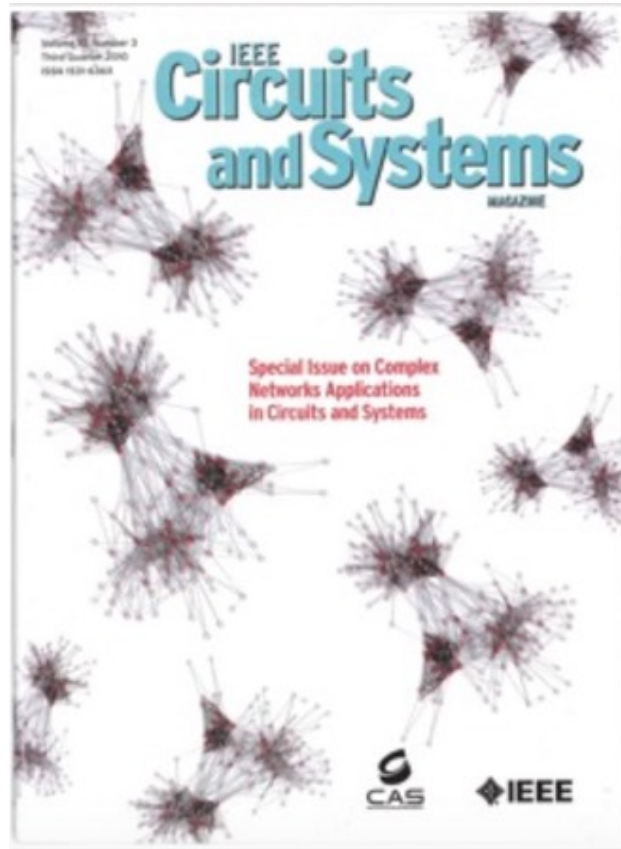
IWCSN: 2004 - 2019

- International Workshop on Complex Systems and Networks (IWCSN):
<http://iwcsn.eie.polyu.edu.hk/>



Publications

- *IEEE CAS Magazine* Special Issue on Applications of Complex Networks, vol. 10, no. 3, 2010.





Publications: <http://www.sfu.ca/~ljilja>

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- Z. Li, Q. Ding, S. Haeri, and Lj. Trajković, “Application of machine learning techniques to detecting anomalies in communication networks: Classification Algorithms” in *Cyber Threat Intelligence*, M. Conti, A. Dehghantanha, and T. Dargahi, Eds., Berlin: Springer, pp. 71-92, 2018.



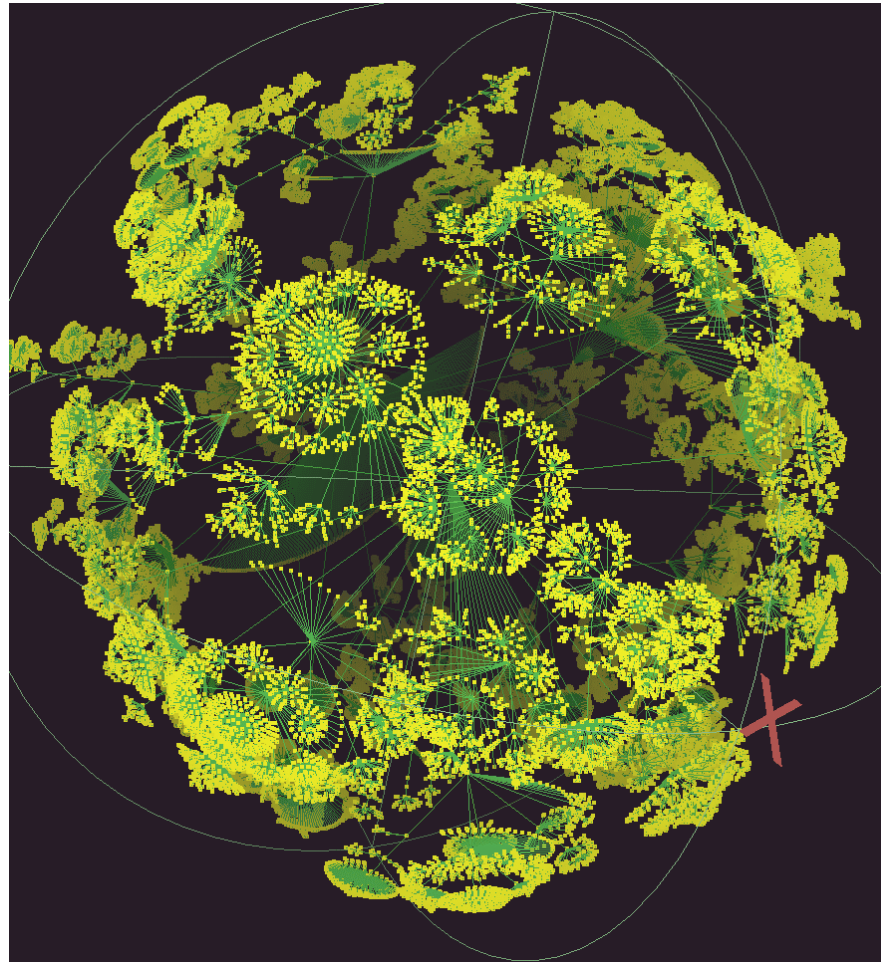
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lhr: 535,102 nodes and 601,678 links



<http://www.caida.org/home/>