

# STAT 270 Lecture 15

Fall 2015

14 October 2015

- We finished ‘Discrete Distributions’.
- In the text we have finished Chapter 4; it is up to you to read about Poisson processes.
- Problems from text: 4.12, 4.13, 4.14, 4.15, 4.17, 4.19, 4.22.
- Midterm Friday covers a bit of Chapter 3 and all of Chapter 4.
- Handwritten slides.
- Key jargon, ideas:
  - The Binomial Distribution:
    - \* Repeat some random experiment a fixed number,  $n$ , of times.
    - \* Each time record whether something happens (‘Success’, S) or doesn’t happen (‘Failure’, F).
    - \* Make sure the outcomes are *independent*.
    - \* Make sure  $p$ , the probability of S, is the same every time.
    - \* Let  $X$  be the number of Successes in the  $n$  trials.
    - \* Then  $X$  has a Binomial( $n, p$ ) distribution.
  - If  $X$  has a Binomial( $n, p$ ) distribution:
    - \*  $E(X) = np$ .
    - \*  $\text{Var}(X) = np(1 - p)$ . Sometimes we use the shorthand  $q = 1 - p$ .
    - \* We can write  $X = X_1 + \dots + X_n$  where the  $X_i$  are Bernoulli random variables. Use this to compute means and variances.
  - If we have a sequence  $X_n, n = 1, 2, \dots$  and each  $X_n$  has a Binomial distribution with  $n$  trials and success probability  $p_n$  such that

$$\lim_{n \rightarrow \infty} np_n = \mu$$

then

$$\lim_{n \rightarrow \infty} P(X_n = k) = \frac{\mu^k}{k!} e^{-\mu} \quad k = 0, 1, \dots$$

- The pmf

$$p(k) = \frac{\mu^k}{k!} e^{-\mu} \quad k = 0, 1, \dots$$

is called the Poisson distribution with mean  $\mu$ .

- If  $X$  has a Poisson( $\mu$ ) distribution then

$$E(X) = \mu$$

and

$$\text{Var}(X) = \mu.$$