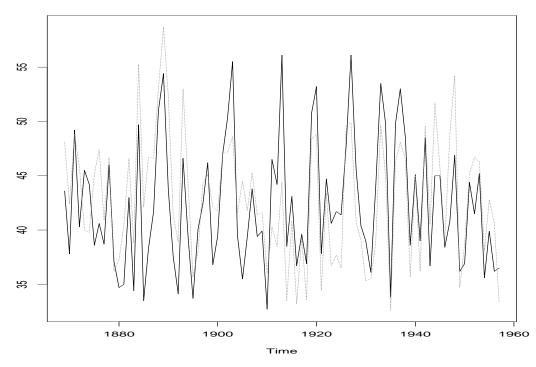
Model identification for a rainfall difference series

Built into S-Plus are two time series *rain.nyc1* and *rain.nyc2*.

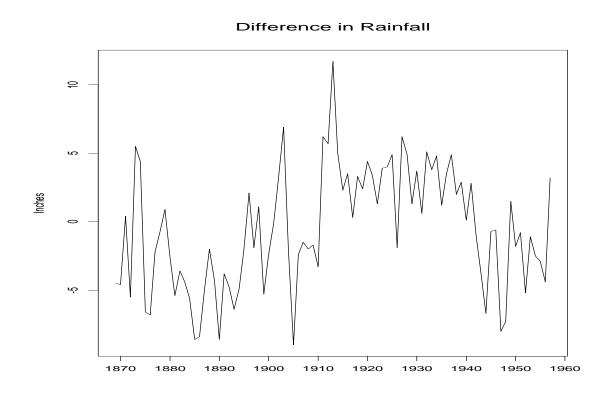
These series are each supposed to be annual rain falls in New York in inches. Here is a plot of the series:





S plotting, model identification and fitting:

This produces the following plot:

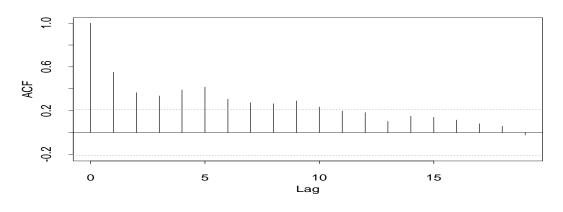


Now I plot the ACF and PACF:

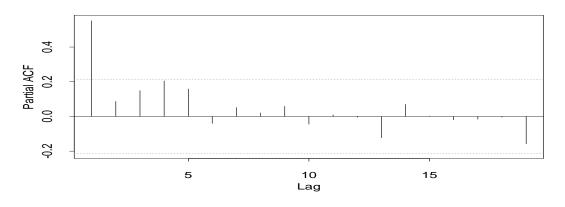
```
postscript(file="raindiff_acf.ps",horizontal=F)
par(mfrow=c(2,1))
acf(x)
acf(x,type="partial")
dev.off()
```

which gives me:

Series: x



Series: x



The PACF is more or less negligible after lag 1 and so I begin with an AR(1) fit

The same model can be fitted using the general ARIMA fitting function *arima.mle*:

```
#
#
    You must remove a mean from x or put
     in a regression term explicitly.
#
     model is specified by a list. Here
#
     I specify an ARIMA(1,0,0) model. Much
#
     more general models are possible.
#
#
> x.armlft <- arima.mle(x-mean(x),</pre>
              model=list(order=c(1,0,0)))
#
   The result is a list with many
#
   components including
#
#
> x.armlft$model
$order:
[1] 1 0 0
$ar:
[1] 0.5572896
$ndiff:
Γ11 0
```

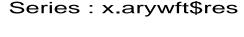
```
#
# You see that the autoregression
  coefficient is slightly different
   as is the estimated error variance
#
#
> x.armlft$sigma2
[1] 13.0793
#
#
  Finally the estimated variance of
    the fitted coefficient is
#
#
> x.armlft$var.coef
            ar(1)
ar(1) 0.007834412
```

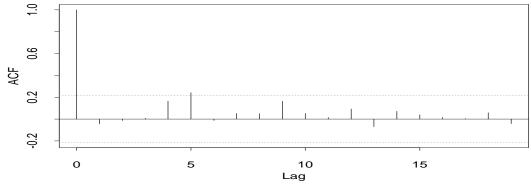
You get the same result from the code

some of whose output is

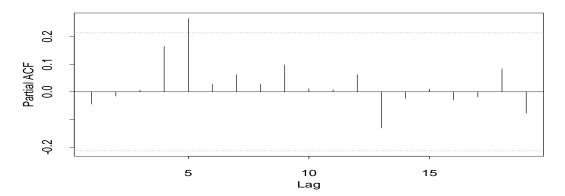
Next I plotted the autocorrelation function of the residuals which are part of the fit.

giving the plot:





Series: x.arywft\$res

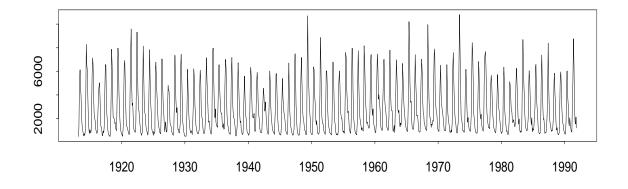


The plots suggest some problem at lag 5. This coefficient is not very significant however, and hard to attach any physical meaning to so I prefer to regard it as sampling variation.

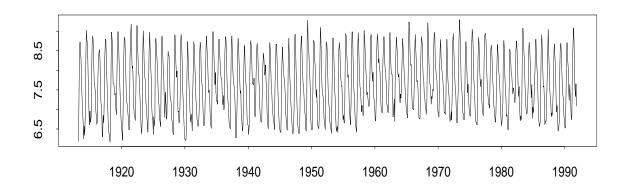
Model identification for Fraser River monthly flows

A data set measuring mean monthly Fraser River flows in cubic meters per second at Hope each month is available through statlib. Here is a plot of the series:

Mean Monthly Flow of Fraser River at Hope (cms)



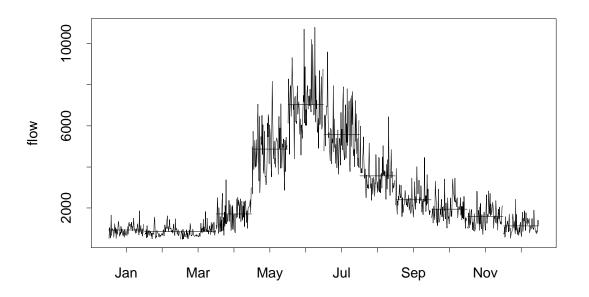
Log Flow



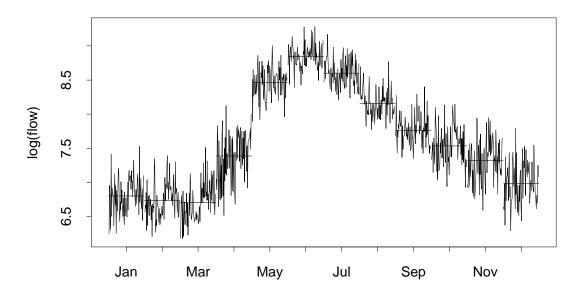
The top of the series appears more volatile than the bottom. To get a good look at this we may use the splus function monthplot:

The graphs on the next page suggest transformation is warranted.

Fraser River Flow

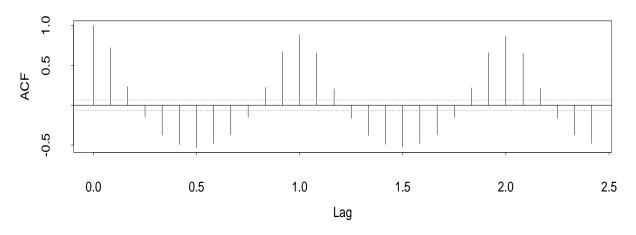


Log Fraser River Flow

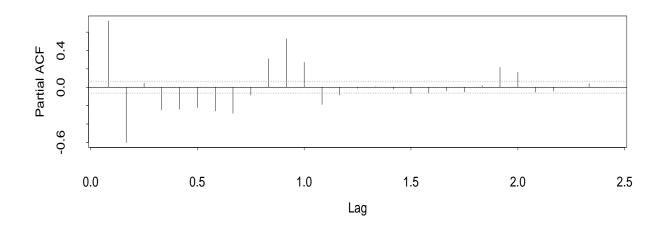


Here are the ACF and PACF:

Series: flow



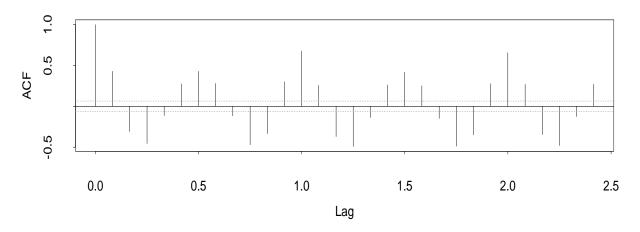
Series: flow



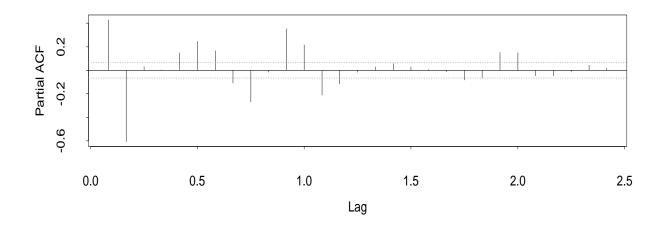
The acf is clearly periodic and I tried a simple sinusoid model:

Here are the ACF and PACF of the residuals:

Series: flow.deseason.1



Series: flow.deseason.1



There is still a clear periodic component so the annual cycle is not a simple sinusoid. Instead I built a matrix of indicators for the months

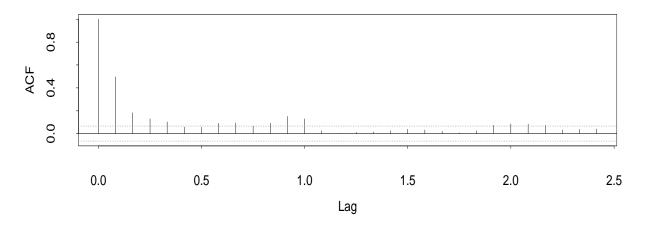
```
xrf <- diag(12)
xrf <- matrix(rep(xrf,78),ncol=12,byrow=T)
xrf <- rbind(xrf[3:12,],xrf)</pre>
```

This builds a matrix of 12 columns and 946 rows (there are 946 months of data) with a 1 in column i indicating the time period is month i. My next fit regressed flow on this matrix:

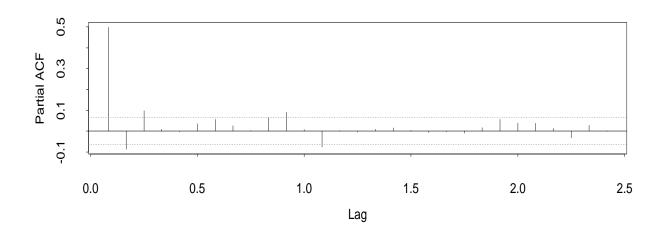
```
fit.1 <- lm(flow ~ xrf - 1)
flow.deseason.2 <- residuals(fit.1)</pre>
```

The ACF and PACF of these residuals are:

Series: flow.deseason.2



Series: flow.deseason.2



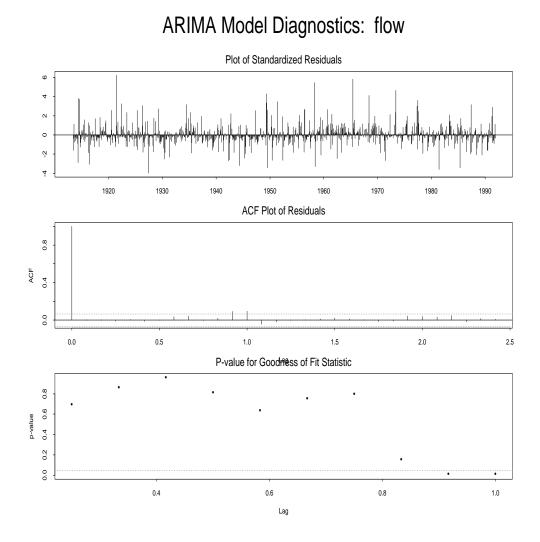
Plots do not provide a clear simple model but suggest we need something at lags 1, 2 3 and perhaps 12 or so.

Latter point motivated by idea that there is some effect of the previous years weather.

It is far from clear that such an effect should be summarized in terms of the flow precisely a year ago and you might instead consider coefficients at several lags in the previous year. I tried to begin by ignoring the effects of the previous year and just fit an AR(3).

Notice return to fitting models to original data permitting software to make allowance for correlation structure in fitting separate means for each month.

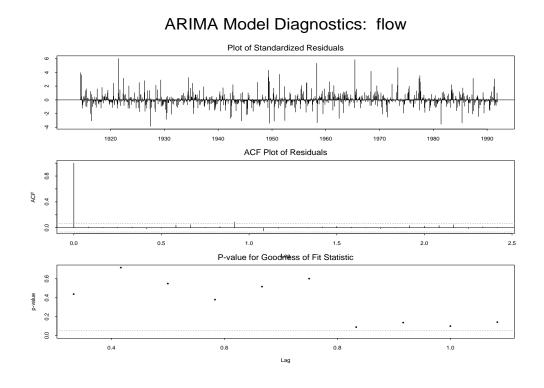
This fit produces the following diagnostic plot



Definite sign of problem near lag of 12 months.

I tried adding a seasonal AR component:

which produces the diagnostic plot:



The diagnostics are now satisfactory. The fitted model is described by

```
fit.3
> $model:
$model[[1]]:
$model[[1]]$order:
[1] 3 0 0
$model[[1]]$ar:
Γ17 0.54173142 -0.13568443 0.09147659
$model[[1]]$ndiff:
Γ17 0
$model[[2]]:
$model[[2]]$order:
[1] 1 0 0
$model[[2]]$period:
[1] 12
$model[[2]]$ar:
[1] 0.09917021
$model[[2]]$ndiff:
[1] 0
```

```
$var.coef:
```

ar(12) -6.39e-07 -5.29e-08 -3.97e-06 1.06e-03

\$method:

[1] "Maximum Likelihood"

\$series:

[1] "flow"

\$aic:

[1] 14646.29

\$loglik:

[1] 14614.29

\$sigma2:

[1] 384435.5

\$n.used:

[1] 931

\$n.cond:

[1] 15

```
$converged:
[1] T

$conv.type:
[1] "relative function convergence"

$reg.coef:
[1] 938.1983 868.5136 855.3402
[4] 1737.1811 4904.1479 7064.3307
[7] 5581.4333 3563.6286 2406.0266
[10] 1952.4763 1592.0973 1133.9484

$reg.series:
[1] "xrf"
```

WARNING: I had to do the following to get the algorithm to converge:

The use of fit.3\$model provides the output of the first fitting effort as starting values for the second fitting effort and the model now converges.

It might actually be better to transform the monthly flow since the variability of the series seems higher when the level is high.

I tried this but the fit was actually a bit worse after taking logs.