6-167 A tank initially contains saturated mixture of R-134a. A valve is opened and R-134a vapor only is allowed to escape slowly such that temperature remains constant. The heat transfer necessary with the surroundings to maintain the temperature and pressure of the R-134a constant is to be determined.

Assumptions **1** This is an unsteady process since the conditions within the device are changing during the process, but it can be analyzed as a uniform-flow process since the state of fluid at the exit remains constant. **2** Kinetic and potential energies are negligible. **3** There are no work interactions involved.

Analysis We take the tank as the system, which is a control volume since mass crosses the boundary. Noting that the microscopic energies of flowing and nonflowing fluids are represented by enthalpy h and internal energy u, respectively, the mass and energy balances for this uniform-flow system can be expressed as

Mass balance:

$$m_{\rm in} - m_{\rm out} = \Delta m_{\rm system}$$
$$- m_e = m_2 - m_1$$
$$m_e = m_1 - m_2$$

Energy balance:

$$\underbrace{E_{\text{in}} - E_{\text{out}}}_{\text{Net energy transfer}} = \underbrace{\Delta E_{\text{system}}}_{\text{Change in internal, kinetic, potential, etc. energies}}$$

$$Q_{\rm in} - m_e h_e = m_2 u_2 - m_1 u_1$$
$$Q_{\rm in} = m_2 u_2 - m_1 u_1 + m_e h_e$$

Combining the two balances:

$$Q_{\rm in} = m_2 u_2 - m_1 u_1 + (m_1 - m_2) h_e$$

The specific volume at the initial state is

$$v_1 = \frac{v}{m_1} = \frac{0.001 \,\mathrm{m}^3}{0.4 \,\mathrm{kg}} = 0.0025 \,\mathrm{m}^3/\mathrm{kg}$$

The initial state properties of R-134a in the tank are

$$T_{1} = 26^{\circ}\text{C}$$

$$\mathbf{v}_{1} = 0.0025 \text{ m}^{3}/\text{kg} \begin{cases} x_{1} = \frac{\mathbf{v}_{1} - \mathbf{v}_{f}}{\mathbf{v}_{fg}} = \frac{0.0025 - 0.0008313}{0.029976 - 0.0008313} = 0.05726 \\ u_{1} = u_{f} + x_{1}u_{fg} = 87.26 + (0.05726)(156.87) = 96.24 \text{ kJ/kg} \end{cases}$$
(Table A-11)

The enthalpy of saturated vapor refrigerant leaving the bottle is

$$h_e = h_{g@26^{\circ}C} = 264.68 \text{ kJ/kg}$$

The specific volume at the final state is

$$v_2 = \frac{v}{m_2} = \frac{0.001 \,\mathrm{m}^3}{0.1 \,\mathrm{kg}} = 0.01 \,\mathrm{m}^3/\mathrm{kg}$$

The internal energy at the final state is

$$T_{2} = 26^{\circ}\text{C}$$

$$v_{2} = 0.01 \text{ m}^{3}/\text{kg} \begin{cases} x_{2} = \frac{v_{2} - v_{f}}{v_{fg}} = \frac{0.01 - 0.0008313}{0.029976 - 0.0008313} = 0.3146 \\ u_{2} = u_{f} + x_{1}u_{fg} = 87.26 + (0.3146)(156.87) = 136.61 \text{ kJ/kg} \end{cases}$$
(Table A-11)

Substituting into the energy balance equation,

$$Q_{in} = m_2 u_2 - m_1 u_1 + (m_1 - m_2) h_e$$

= (0.1 kg)(136.61 kJ/kg) - (0.4 kg)(96.24 kJ/kg) + (0.4 - 0.1 kg)(264.68 kJ/kg)
= **54.6 kJ**

