Thermal Spreading Resistance of Arbitrary-Shape Heat Sources on a Half-Space: A Unified Approach
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Abstract—Thermal spreading/constriction resistance is an important phenomenon where a heat source/sink is in contact with a body. Thermal spreading resistance associated with heat transfer through the mechanical contact of two bodies occurs in a wide range of applications. The real contact area forms typically a few percent of the nominal contact area. In practice, due to random nature of contacting surfaces, the actual shape of microcontacts is unknown; therefore, it is advantageous to have a model applicable to any arbitrary-shape heat source. Starting from a half-space representation of the heat transfer problem, a compact model is proposed based on the generalization of the analytical solution of the spreading resistance of an elliptical source on a half-space. Using a “bottom-up” approach, unified relations are found that allow accurate calculation of spreading resistance over a wide variety of heat source shapes under both isoflux and isothermal conditions.

Index Terms—Elliptical heat source, half-space, spreading resistance, square root of area, superposition.

NOMENCLATURE

\( A \) Area (m\(^2\)).
\( a \) Major semi-axis (m).
\( B(\cdot, \cdot) \) Beta function.
\( b \) Minor semi-axis (m).
\( K(\cdot) \) Complete elliptic integral of the first kind (7).
\( k \) Thermal conductivity (W/m \( \cdot \) K).
\( L \) Characteristic length scale (m).
\( N \) Number of sides of a regular polygon.
\( n \) Geometric parameter for hyperellipse.
\( Q \) Heat flow rate (W).
\( q \) Heat flux (W/m\(^2\)).
\( R \) Thermal spreading resistance (K/W).
\( R_{\tau} \) Thermal spreading resistance, isothermal source (K/W).
\( r \) Radius (m).
\( \tau \) Average temperature (K).
\( T_0 \) Centroidal temperature (K).

Greek Letters

\( \alpha \) Angle (rad).
\( \beta \) Length ratio, \( b/a \).
\( \Gamma(\cdot) \) Gamma function.
\( \epsilon \) Aspect ratio.
\( l \) Length, \( x_c/r \).
\( r \) Distance in polar coordinate (m).
\( \varrho \) Angle (rad).
\( \rho \) Geometrical center of area.

Subscript

\( c \) Geometrical center of area.

I. INTRODUCTION

S PREADING resistance, also sometimes referred to as constriction resistance, is commonly encountered in thermal engineering whenever a concentrated heat source is in contact with a larger heat conducting surface. This phenomenon extends also to electric current and mass transfer problems. In this paper, we focus on thermal spreading resistance which often appears as a bottleneck in heat management, and is of relevance in applications such as integrated circuits and laser heating. In contacting bodies, real interaction between two surfaces occur only over microscopic contacts \[1\], \[2\]. The actual area of contact, i.e., the total area of all microcontacts, is typically less than 2% of the nominal contact area \[1\], \[2\]. Thus, heat flow is constricted and then spreads to pass from the contact area to contacting bodies. Thermal spreading resistance plays a vital role in the design of numerous thermal, electrical, and electronic devices and systems. Electronic equipment, aircraft structural joints, surface thermocouples, boundary lubrication, nuclear reactors, biomedical industries, and cryogenic liquid storage devices are only a few examples of such systems \[3\]–\[7\].

Assuming dimensions of microcontacts and/or heat sources are small compared with the distance separating them and with the dimensions of the body which heat spreads through, the heat source on a half-space hypothesis can be used \[8\]. As the microcontacts or heat sources increase in number and grow in size, a flux tube problem should be considered to account for...
for the interference between neighboring microcontacts/heat sources. For an in-depth review of flux tube solutions for spreading resistance see [4], [9]–[11]. Several researchers including Kennedy [6], Ellison [12], Karmalkar et al. [13], and Pawlik [14] focused on analyzing thermal spreading resistance in electronic devices.

Yovanovich and his coworkers [15]–[18] investigated a range of steady-state and transient thermal spreading resistance. They proposed thermomechanical models for contact, gap, and joint resistances of joints formed by conforming rough surfaces including singly and doubly connected heat sources such as: hyperellipse, semicircle, triangle, polygon, and annulus. They also introduced the use of the square root of the source area to nondimensionalize spreading resistance.

Analytical, experimental, and numerical models have been developed to predict thermal spreading resistance since the 1930s. Several hundred papers on thermal spreading resistance have been published which illustrates the importance of this topic.

In practice, due to the random nature of contacting surfaces, the actual shape of microcontacts is unknown; therefore, it would be beneficial to have a model applicable to any arbitrary-shape heat source. In spite of the rich body of literature on spreading resistance, there is yet no general model which can accurately estimate the spreading resistance of an arbitrary-shape heat source on a half-space due to the challenge of dealing with complex irregular geometries.

In this paper, a compact model is proposed based on the analytical solution of the spreading resistance of an elliptical source on a half-space. Using a “bottom-up” approach, it is shown that for a broad variety of heat source shapes, the proposed model is in agreement with the existing and/or developed analytical solutions.

II. PROBLEM STATEMENT

Consider steady-state heat transfer from an arbitrary-shape planar singly connected heat source on a half-space, Fig. 1. The temperature field within the half-space must satisfy Laplace’s equation, \( \nabla^2 T = 0 \).

\( \text{Fig. 1. Arbitrary-shape heat source on a half-space.} \)

\( \text{Fig. 2. (a) Point outside the heat source. (b) Point inside the heat source.} \)

Thermal spreading resistance \( R \) is defined as the difference between the temperature of heat source and the temperature of a heat sink far from it divided by the total heat flow rate through the contact area \( Q \), i.e., \( R = \Delta T/Q \) [19]. For convenience, the temperature far from the contact area may be assumed to be zero with no loss of generality, that is

\[ R = \frac{T}{Q} \]  

To evaluate the spreading resistance, the temperature distribution of the heat source is required. Yovanovich [15] developed a relationship for the temperature distribution at each point of an isoflux heat source plane by using the integral superposition technique

\[ T(x, y, 0) = \frac{q}{2\pi} \int_0^\infty \rho(\omega) d\omega \]  

where \( \rho \) and \( \omega \) are shown in Fig. 2 for points outside and inside of the heat source area. The reference temperature of heat sources is usually considered as the centroid or the average temperature. Substituting geometric center coordinates into (2), the centroid temperature can be found. For the average temperature, the temperature distribution is integrated over the heat source area

\[ T = \frac{1}{A} \int_A T(x, y, 0) dA \]  

For complicated shapes, the geometry is subdivided into simpler shapes, \( T(x, y, 0) \) is then computed from (2) for each subdivided shape and the values are added up. Once the temperature is determined, the spreading resistance is obtained through (1). To investigate the trend of different shapes and aspect ratios, it is more convenient to nondimensionalize spreading resistance in the form of \( R' = k \cdot \mathcal{L} \cdot R \), where \( k, \mathcal{L} \), and \( R \) are the thermal conductivity of half-space, a characteristic length scale, and the spreading resistance, respectively [16]. Parameters required to define spreading resistance are: reference temperature, characteristic length scale, and boundary condition, (see Fig. 3). The reference temperature can be the centroid or average temperature of the source. According to Yovanovich [16], spreading resistance values for hyper-elliptical sources vary over narrower bond when based on the centroidal temperature rather than when based on the average temperature. As shown later, there is a relationship...
between the average and the centroid based resistances; for convenience, the average temperature is used as the reference temperature. After examining several possible length scales, we concluded that the square root of the area is the best choice of characteristic length scale, as Yovanovich proposed [16]. The next parameter is boundary condition; two boundary conditions are considered: 1) isothermal and 2) isoflux. The isoflux boundary condition is easier to apply and solve for. Furthermore, a relationship between these boundary conditions can be established.

III. CHARACTERISTIC LENGTH SCALE

To nondimensionalize the spreading resistance, a characteristic length scale is required. Different characteristic length scales are examined in this section. These include perimeter P, hydraulic diameter (Dh = 4A/P), an arbitrarily chosen dimension a, and the square root of the source area \( \sqrt{A} \).

An analytical solution exists for hyperellipse shapes in the literature [16]. To compare different characteristic length scales, a hyperellipse source covering a wide variety of geometries is selected. A hyperellipse, in the first quadrant, is described by

\[
y = b \left(1 - \left(\frac{x}{a}\right)^{2/n}\right)^{1/n}
\]

where \( a \) and \( b \) are characteristic dimensions along the x and y axes, respectively, see Fig. 4. The effect of parameter \( n \) on the shape of the hyperellipse source is also shown in Fig. 4. When \( n = 1 \), the hyperellipse yields a rhombic source \((a > b)\), or a square \((a = b)\); for \( n = 2 \), the source is elliptical \((a > b)\), or circular \((a = b)\); \( n > 3 \), yields a rectangle \((a > b)\) or a square \((a = b)\) source with rounded corners; and for \( n \rightarrow \infty \), the shape approaches a full rectangle/square source [16].

Yovanovich [16] calculated the spreading resistance for hyperelliptical sources. For instance, the nondimensional spreading resistance with \( \sqrt{A} \) as the characteristic length scale is [16]

\[
A_{\text{sd}} = \frac{1}{\pi} \sqrt{\frac{\pi}{2}} \left(1 + \frac{1}{n}\right) \int_{0}^{1} \frac{1}{\sqrt{1 - \frac{1}{n}}} \frac{\sin^2 \omega + \epsilon^{-2} \cos^2 \omega} {\sin^2 \omega + \epsilon^2 \cos^2 \omega} d\omega
\]

where \( B(\cdot) \) is the beta function.

IV. PROPOSED MODEL

As shown previously, nondimensional spreading resistances of hyperelliptical sources with equal areas and aspect ratios are close for any value of \( 2 \leq n \leq \infty \). Thus, if we select one of these shapes in the model, the spreading resistance of the others can be predicted with good accuracy. The premise of the present model is that the solution for hyperelliptical source can be applied to estimate the spreading resistance of any shape of heat sources when the area and aspect ratio are the same as those of the hyperelliptical source. Since, the analytical solution of the elliptical source is more convenient, it is chosen as the basis of the model. Note that the isoflux rectangle could also be used as the basic model, but subsequent analysis has shown that the isoflux ellipse provides better overall agreement. According to the present model, an arbitrary-shape heat source is transformed to an elliptical shape where area and aspect ratio are maintained constant, (see Fig. 6).
analytical solution for the spreading resistance of an isoflux elliptical source on a half-space can be expressed using the general solution proposed by Yovanovich for a hyperellipse [15]

\[ k\sqrt{A}R_0 = \frac{2}{\sqrt{\pi}} K(1 - \frac{1}{\epsilon^2}) \]

where \( K(\cdot) \) is the complete elliptic integral of the first kind defined as

\[ K\left(1 - \frac{1}{\epsilon^2}\right) = \int_0^{\pi/2} dt \sqrt{\frac{1 - \left(1 - \frac{1}{\epsilon^2}\right) \sin^2 t}{}} \]

There are a number of possible ways of defining the aspect ratio for arbitrary shapes, and in this paper the following is adopted

\[ \epsilon = \frac{b}{a} \]

where \( a \) is the maximum length of the shape in arbitrary direction of \( x \), and \( b \) is the maximum length in the perpendicular
Fig. 7. Comparison of polygonal heat source with the model.

Choosing a proper aspect ratio is important. The aspect ratio for an equilateral triangle is unity; hence, the aspect ratio that also satisfies the equilateral case is $\epsilon = \beta(2/\sqrt{3})$. The spreading resistance for isosceles triangular source is compared with the model in Fig. 8. Results show good agreement with the model and maximum error is less than 2.2% when $\epsilon > 0.1$.

C. Rhombic Source

A rhombus is a special case of hyperellipse with $n=1$. The spreading resistance for this shape can be evaluated from (5). A simpler method to calculate it, would be using the superposition technique. The nondimensional spreading resistance for a rhombic source can be written as

$$k\sqrt{A}R_0 = \frac{\sqrt{2}}{\pi} \sin(\omega_1) \ln[\tan(\frac{\pi}{4} + \frac{\omega_1}{2}) \tan(\frac{\pi}{4} + \frac{\omega_2}{2})]$$

where $\omega_1 = \tan^{-1}(3/2\beta)$, $\omega_2 = \pi/2 - \cot^{-1}(2\beta)$, $\omega_3 = \pi - \omega_1 - \omega_2$, and $\beta = b/a$.

Fig. 9 compares the rhombic heat source solution and the model, (6); except for small value of aspect ratio, $0 < \epsilon < 0.25$, the results agree with the model within 1.7%. The agreement for the lower aspect ratios is within 10%.

D. Trapezoidal Source

The trapezoidal cross-section is an important geometry which in the limit when the top side length goes to zero, yields an isosceles triangle. At the other limit when top and bottom sides are equal, it becomes a rectangle/square.

The spreading resistance for a trapezoidal source is found using superposition technique. The relationship for a trapezoidal source is unwieldy, and is therefore given in the appendix. The comparison of the results with the model for various trapezoidal sources is shown in Fig. 10; again there is good overall agreement with the model and the difference is less than 4% when $\epsilon > 0.1$.

E. Rectangular Source With Round Ends

Rectangular heat source with round ends is a combination of triangular and circular sector sources. Using superposition
Fig. 9. Comparison of rhombic heat source with the model.

Fig. 10. Comparison of different trapezoidal heat sources with the model.

technique, the exact solution for this source is

\[ k\sqrt{AR_0} = \frac{\sqrt\pi}{\pi} \frac{\beta \ln \left( \frac{\pi}{2} + \eta \right) + \eta \tan^{-1} \beta}{\sqrt{\left(1 + \eta^2 \right) \tan \beta}} \]

(12)

where \( \eta = (\pi/2) - \tan^{-1} \beta \), \( \beta = b/a \), and \( \epsilon = \beta/\sqrt{1 + \beta^2} \).

Fig. 11 shows the analytical solution compared with the model. It can be seen that the model can estimate the spreading resistance of this shape with the maximum error of 2% where \( \epsilon > 0 \).

F. Rectangular Source With Semicircular Ends

Rectangular heat source with semicircular ends is a combination of triangular and circular segment sources. Using superposition technique, the exact solution for this source is

\[ k\sqrt{AR_0} = \frac{1}{\pi \sqrt{\alpha}} \left[ \eta \sin \alpha \ln \left( \frac{\pi}{4} + \frac{\alpha_0}{2} \right) \tan \left( \frac{\pi}{4} + \frac{\alpha_0}{2} \right) \right. \\
+ \left. \int_{\omega_1}^{\omega_2} \left( \sqrt{1 - \eta^2 \sin^2 \omega - \eta \cos \omega} \right) d\omega \right] \]

(13)

where \( \eta = x_c/r = 2 \sin \alpha/3a \), \( \alpha_0 = \pi/2 - \alpha \), \( \alpha_2 = \tan^{-1} \left( (1 - \eta \cos \alpha)/(\eta \sin \alpha) \right) \), \( \alpha_0 = \pi - \alpha_1 - \alpha_2 \). The aspect ratio is defined as the ratio of maximum lengths in \( y \) and \( x \) directions, i.e., \( \epsilon = 2 \sin \alpha/r = 2 \sin \alpha \).

Fig. 11. Comparison of “rectangular heat source with round ends” with the model.

Fig. 12. Comparison of “rectangular heat source with semicircular ends” with the model.

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The relationship developed for the circular sector source is compared with the model in Fig. 13. Note that since \( \eta \) and \( \omega_1 \) are functions of \( \alpha \) only, and since \( a = \sin^{-1}(\epsilon/2) \), (14) can be plotted as a function of \( \epsilon \) only. It can be observed that for small values of aspect ratios, the error is more than 5%, but for \( \epsilon > 0.27 \) the error becomes less than 5%.

**H. Circular Segment Source**

A circular segment can be presented as a combination of right angle triangles and noncircular sector sources with the common vertex at the geometric center. Applying (2) and using superposition technique, the exact solution for the spreading resistance can be found

\[
k \sqrt{AR_0} = \frac{1}{\pi} \left\{ \frac{(\eta - \cos \alpha) \ln \left[ \tan \left( \frac{\pi}{4} + \frac{\omega_1}{2} \right) \right]}{\sqrt{1 - \eta^2 \cos^2 \omega_1 - \eta \cos \omega_1}} + \int_0^{\omega_1} \left( \sqrt{1 - \eta^2 \sin^2 \omega_1 - \eta \cos \omega_1} \right) d\omega_1 \right\}
\]

where \( x_c = (r/3)(2 \sin \alpha - \cos \alpha \sin 2\alpha) \), \( a = x_c/r \), \( \omega_1 = \tan^{-1} \left( \sin \alpha/(\eta - \cos \alpha) \right) \), and \( \omega_2 = \pi - \omega_1 \). The aspect ratio is defined as the ratio of maximum lengths in \( y \) and \( x \) directions.

For different value of \( \alpha \), the aspect ratio becomes

\[
\epsilon = \begin{cases} 
1 - \cos \alpha & \text{if } \alpha \leq \pi/2 \\
\frac{1 - \cos \alpha}{\pi} & \text{if } \pi/2 < \alpha \leq \pi
\end{cases}
\]

The exact solution of the circular segment source is compared with the model in Fig. 14. The results show good agreements with the model over the entire range of aspect ratio.

The examined geometries of a heat source on a half-space are compared with the model in Table I and Fig. 15. The definition of aspect ratio, proper criteria to use the model, and the maximum relative error with respect to the model is reported in Table I. The maximum error occurs in small values of aspect ratio, \( \epsilon \leq 0.01 \); if aspect ratio is greater than 0.1 the error decreases sharply. As seen in Table I and Fig. 15, the model shows good agreement with the analytical solutions for wide variety of shapes, especially when \( \epsilon > 0.1 \).

**VI. Reference Temperature**

Having established the accuracy of the proposed model provides for the centroidal temperature based spreading resistance of any arbitrary-shape isoflux heat source on a half-space, we turn our attention to developing a relationship between the centroid temperature and average temperature based spreading resistances. The latter is a commonly used reference and can also be applied to doubly-connected regions.

There is no analytical solution for the isothermal elliptical source in the literature, therefore, this problem was solved numerically in this paper. The results show that the ratio of nondimensional spreading resistances based on the average and centroid temperatures for elliptical source varies only
between 0.8485 and 0.8491; therefore, it remains approximately constant with an average value of 0.849:

\[ k\sqrt{AR} \frac{R}{R_0} \approx 0.849. \tag{17} \]

Yovanovich et al. [16], [17] already established this result for some specific shapes; the analysis presented here shows that in fact this is generally valid for a wide range of geometries. The nondimensional spreading resistance based on the average temperature for elliptical and rectangular sources is shown in Fig. 16. The predicted resistances are indeed very close. Since the ellipse and rectangle are the lower and the upper bounds for the hyperellipse within \(2 \leq n \leq \infty\), it can be concluded that the elliptical source result for nondimensional spreading resistance based on the average temperature can be used for hyperelliptical source within \(2 \leq n \leq \infty\). Also, (17) provides an excellent estimate of the ratio \(R/R_0\).

Since the model provides a good estimate for centroidal temperature based spreading resistance, and (17) is approximately valid for hyperelliptical shapes covering a wide variety of geometries, (17) can be used with confidence to predict the ratio of spreading resistance based on the average and centroidal temperatures for a broad variety of heat source shapes. Thus, combining (6) and (17), the model for the average temperature
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VII. Boundary Condition

We have so far considered spreading resistance for any isoflux arbitrary-shape heat source on a half-space. Yovanovich [18] developed an analytical solution for an isothermal elliptical source

\[ k \sqrt{AR} = \frac{1.6974}{\pi \sqrt{\epsilon}} K \left( 1 - \frac{1}{\pi^2} \right) \sqrt{\epsilon} \]

(18)

Schneider [20] numerically solved Laplace’s equation for the rectangular source and reported a correlation of the form

\[ k \sqrt{AR} = \sqrt{\frac{\epsilon}{\pi K}} \left( 1 - \frac{1}{\epsilon^2} \right) \]

(19)

A comparison between the solutions of isothermal rectangular and elliptical sources indicates a maximum difference of 1.27% which occurs at \( \epsilon = 1 \), while the solutions are essentially identical for an aspect ratio \( \epsilon \) less than 0.4. Since the isoflux elliptical source which is proposed as the model predicts accurately spreading resistance of any isoflux arbitrary-shape heat source, this suggests that the solution for isothermal elliptical source can be used for a wide variety of isothermal heat sources. Thus, the general form of the model for any arbitrary-shape heat source on a half-space can be expressed as

\[ k \sqrt{AR} = \begin{cases} 
1.6974 \frac{K \left( 1 - \frac{1}{\pi^2} \right)}{\pi \sqrt{\epsilon} \sqrt{\epsilon}} & \text{isoflux (average temp.)} \\
\sqrt{\frac{\epsilon}{\pi K}} \left( 1 - \frac{1}{\epsilon^2} \right) & \text{isothermal.}
\end{cases} \]

(21)

VIII. Summary And Conclusion

Thermal spreading resistance is an important major phenomenon in thermal engineering problems, whenever temperature and cross-sectional area variations exist. In this paper, a model based on the generalization of the analytical solution of isoflux elliptical source has been proposed, and analytic solutions were obtained for a variety of complex shapes. The generalized model presented here provides a unified approach for calculating the spreading resistance for a large variety of geometries, and under both isoflux and isothermal conditions. The highlights of the model and results are as follows.

1) The most appropriate characteristic length scale for nondimensional spreading resistance is square root of area \( \sqrt{A} \).

2) The spreading resistance for arbitrarily singly connected shapes agrees with the proposed model.

3) The ratio of isothermal to isoflux spreading resistance is approximately 0.931 for a wide range of shapes for different aspect ratios.

APPENDIX

Isosceles Trapezoidal Source

The spreading resistance for an isosceles trapezoidal source is found using superposition technique. Considering the parameters shown in Fig. 18, the nondimensional spreading resistance based on the centroidal temperature is found as
must be replaced by Fig. 18. Cross-section of an isosceles trapezoidal heat source.

\[ k\sqrt{A}R_0 = \frac{1}{\pi} \frac{\partial (\Omega_2 + \omega_2)}{\partial \theta} + \frac{\partial \Omega_2}{\partial A} + \frac{\partial \omega_2}{\partial A} \sqrt{\pi} \]  \hspace{1cm} (22)

where \( \Omega_2 = \ln(\tan(\pi/4 + \omega_2/2)) \). For \( \theta > 0 \), \( \Omega_2 \) and \( \omega_2 \) must be replaced by \( -\Omega_2 \) and \( -\omega_2 \), respectively.

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