

To solve this problem you can use different coordinate systems with arbitrary origin. Here we look at three of these coordinate systems

(I) $v_0 = 12.0 \text{ m/s}$, $x_0 = 70.0 \text{ m}$, $a = -9.8 \text{ m/s}^2$

(a) $x = x_0 + v_0 t + \frac{1}{2} a t^2$

$$0 = 70.0 \text{ m} + 12.0 \text{ m/s} (t) + \frac{1}{2} (-9.8 \text{ m/s}^2) t^2$$

$$\Rightarrow -4.9 t^2 + 12 t + 70 = 0$$

solutions of a quadratic equation:

$$t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-12 \pm \sqrt{12^2 - 4(-4.9)(70)}}{2(-4.9)}$$

$$\Rightarrow \begin{cases} t = -2.75 \rightarrow \text{This answer is not acceptable b/c it is negative} \\ \boxed{t = 5.2 \text{ s}} \end{cases}$$

(b) $v_f = v_0 + a t \Rightarrow v_f = 12 + (-9.8)(5.2) \Rightarrow v_f = 12 - 50.96$

$$\Rightarrow v_f = -38.96 \text{ m/s}$$

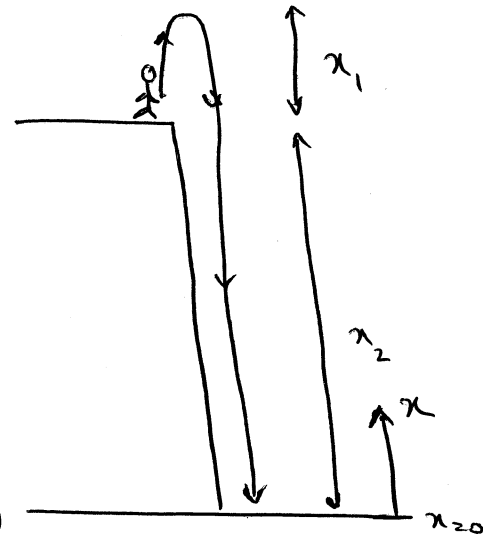
Speed is the magnitude of the velocity vector

$$\Rightarrow v = 39 \text{ m/s}$$

(c) $v_f^2 - v_0^2 = 2ad$

$$0 - 12^2 = 2(-9.8)(x_1) \Rightarrow x_1 = 7.35 \text{ m}$$

$$\Rightarrow \text{Total distance} = 2x_1 + x_2 = 2(7.35 \text{ m}) + 70 \text{ m} = 14.7 \text{ m} + 70 \text{ m} \Rightarrow \boxed{d = 84.7 \text{ m}}$$



(II)

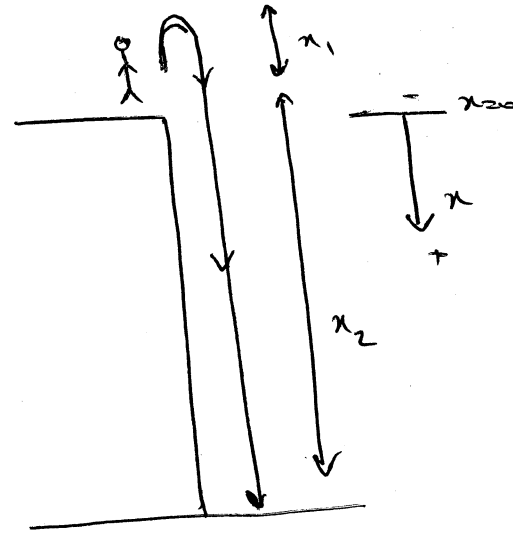
$$v_0 = -12.0 \text{ m/s}, \quad x_0 = 0 \text{ m}, \quad a = 9.8 \text{ m/s}^2$$

$$(a) \quad x = x_0 + v_0 t + \frac{1}{2} a t^2$$

$$+70 = 0 + (-12) \text{ m/s} (t) + \frac{1}{2} (9.8) t^2$$

$$\Rightarrow 4.9 t^2 - 12 t + (-70) = 0$$

$$\Rightarrow \begin{cases} t = -2.75 \text{ s} \rightarrow \text{not acceptable} \\ t = 5.20 \text{ s} \end{cases}$$



$$(b) \quad v_f = v_0 + at \Rightarrow v_f = -12.0 \text{ m/s} + 9.8(5.2) \Rightarrow v_f = 38.96 \text{ m/s}$$

$$\text{speed is the magnitude of velocity} \Rightarrow v = 39 \text{ m/s}$$

$$(c) \quad v_f^2 - v_0^2 = 2ad \Rightarrow 0 - (-12)^2 = 2(9.8) x_1 \Rightarrow x_1 = 7.35 \text{ m}$$

distance is the magnitude of displacement for the first part of the movement

$$\Rightarrow d = 70 + 2(7.35) = 84.7 \text{ m}$$

(III) $v_0 = 12 \text{ m/s}$, $x_f = -70 \text{ m}$, $x_0 = 0$

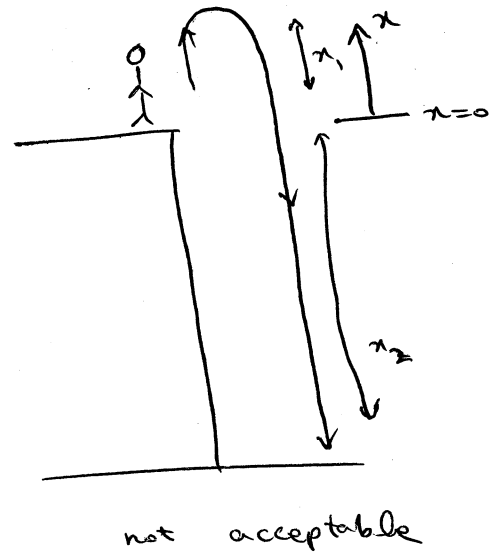
$a = -9.8 \text{ m/s}^2$

(a) $x_f = x_0 + v_0 t + \frac{1}{2} a t^2$

$-70 \text{ m} = 0 + 12(t) + \frac{1}{2}(-9.8)t^2$

$\Rightarrow -4.9t^2 + 12t + 70 = 0$

$t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \Rightarrow \begin{cases} t = -2.75 \\ \boxed{t = 5.2 \text{ s}} \end{cases}$



(b) $v_f = v_0 + at \Rightarrow v_f = 12 + (-9.8)(5.2) \Rightarrow v_f = -38.9 \text{ m/s}$

Speed is the magnitude of the velocity $\Rightarrow v = 39 \text{ m/s}$

(c) $v_f^2 - v_0^2 = 2ad$

$0 - (12)^2 = 2(-9.8)(x_1) \Rightarrow x_1 = 7.35 \text{ m}$

$\Rightarrow \text{Total distance} = 2x_1 + x_2 = 2(7.35 \text{ m}) + 70 \text{ m} \Rightarrow \boxed{d = 84.7 \text{ m}}$