

Using Poiseuille's equation:

$$Q = \frac{\pi R^4 \Delta P}{8 \eta_{\text{blood}} L} \Rightarrow \Delta P = \frac{8 \eta_{\text{blood}} L Q}{\pi R^4}$$

$$\text{Volumetric flow rate: } Q = \frac{4 \text{ cm}^3}{\text{min}} = \frac{4 \times 10^{-6}}{60} \frac{\text{m}^3}{\text{s}}$$

$$\text{Length of the needle: } L = 4 \text{ cm} = 0.04 \text{ m}$$

$$D_{\text{needle}} = 0.40 \text{ mm} \Rightarrow R = 0.20 \text{ mm} = 2 \times 10^{-4} \text{ m}$$

$$\eta_{\text{blood}} = 4 \times 10^{-3} \text{ Pa.s} \quad \text{and} \quad \rho_{\text{blood}} = 1.05 \times 10^3 \frac{\text{kg}}{\text{m}^3}$$

pressure at the entrance of the needle should be higher than  $18 \text{ torr} = 2.4 \times 10^3 \text{ N/m}^2$

$$\Rightarrow \Delta P = \frac{8 (4 \times 10^{-3} \text{ Pa.s}) (0.04 \text{ m}) \left( \frac{4 \times 10^{-6}}{60} \frac{\text{m}^3}{\text{s}} \right)}{\pi (2 \times 10^{-4})^4}$$

$$\Rightarrow \Delta P = 16985 \frac{\text{N}}{\text{m}^2} = 1.7 \times 10^4$$

$$P_1 + \Delta P = \rho_{\text{blood}} g h \Rightarrow h = \frac{1}{\rho_{\text{blood}} g} (2.4 \times 10^3 + 1.7 \times 10^4) \Rightarrow$$

$$h = 1.8 \text{ m}$$