

Physics 101
Lecture 28

Monday Mar. 15, 2004

Fluids.

Topics : Density
Pressure
Pascal's principle
Buoyancy

Ref: 15-1, 2, 3, 4, 5, 6.

- Fluids — Liquids and gases.
 - Density : (can flow and take on the shape of container)

$$\rho = M/V \quad \text{kg/m}^3$$
 - Pressure : How much force per unit area.

$$P = F/A \quad \text{N/m}^2 = \text{Pascal} \equiv \text{Pa}$$
- e.g: Popping a Balloon. Same force F , different A .



Large A .
small P



small A
large P .

- Pressure and depth at static equilibrium.

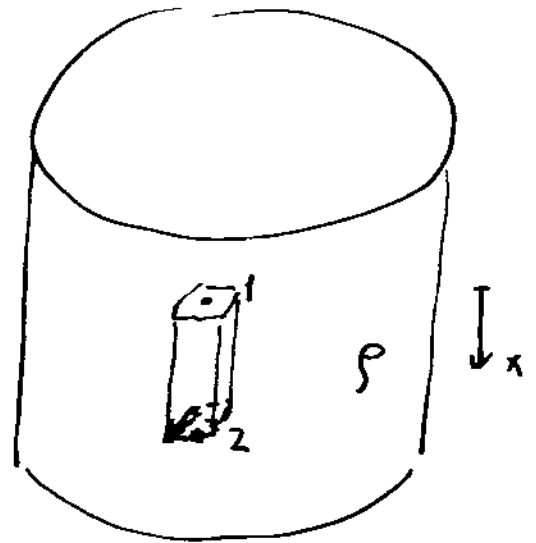
$$P_1 A - P_2 A + mg = 0$$

$$P_2 = P_1 + \frac{mg}{A}$$

$$= P_1 + \frac{\rho V g}{A}$$

$$\therefore P_2 = P_1 + \rho g h$$

OR: $P_2 - P_1 = \rho g h$



- Atmospheric pressure

— due to air in the atmosphere

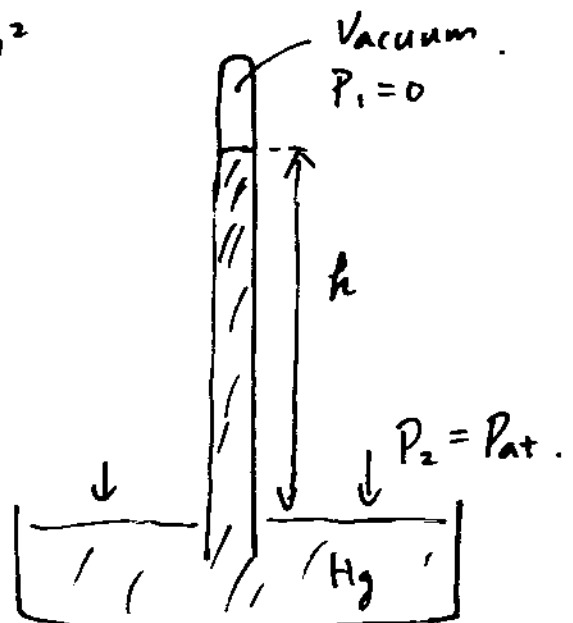
$$P_{\text{atmos}} = 1.01 \times 10^5 \text{ N/m}^2$$

$$= 1.01 \times 10^5 \text{ Pa}$$

- Barometer

$$P_{\text{at}} = P_2 = \rho g h$$

e.g: 



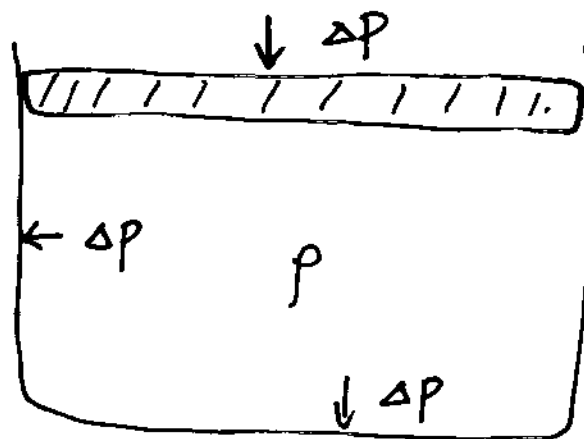
$$\text{Hg: } \rho = 13.6 \text{ kg/cm}^3 = 1.36 \times 10^4 \text{ kg/m}^3$$

$$h = 760 \text{ mm} = 0.76 \text{ m}$$

$$P_{\text{at}} = 1.36 \times 10^4 \times 0.76 \times 9.81 = 1.01 \times 10^5 \text{ N/m}^2 = 1.01 \times 10^5 \text{ Pa}$$

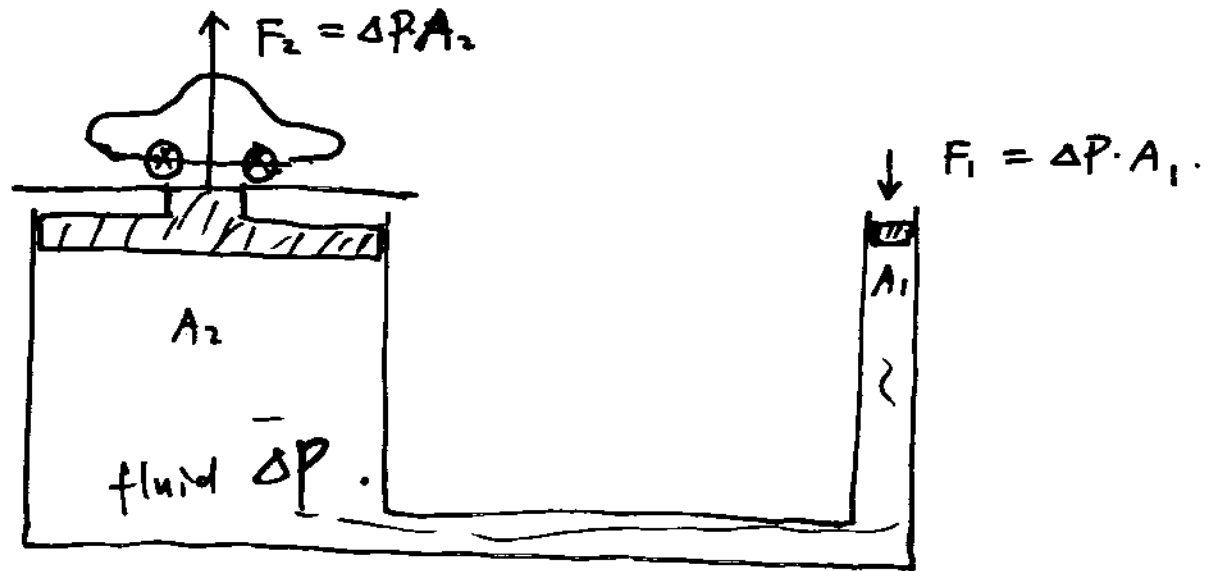
- The pressure in a fluid acts equally in all directions and acts perpendicularly to any surface.
- Pascal's Principle

An external pressure applied to an enclosed fluid is transmitted unchanged to every point in the fluid.



ΔP is the same everywhere.

e.g. Hydraulic Lift .



Since ΔP is the same everywhere

$$\frac{F_2}{A_2} = \frac{F_1}{A_1} .$$

$$F_2 = \frac{A_2}{A_1} F_1 \quad \text{if we make } A_2 \gg A_1$$

$$\text{Then } F_2 \gg F_1 .$$

You only need a small force F_1 to lift a car !

i.e., a hydraulic lift can "magnify" force F_1 .

• But No free lunch ! — We can't save work .

If we want to lift the car by a distance d_2 ,

We would have to apply F_1 by a longer distance d_1 ,

$$\therefore A_1 d_1 = A_2 d_2 \text{ (same Volume) } , d_1 = \frac{A_2}{A_1} d_2 \gg d_2$$

$$\text{Then, } F_1 d_1 = F_2 d_2 \text{ (same work !)}$$