

CAPA due date
extended to Friday
night 11:59 PM.

Lecture 15.

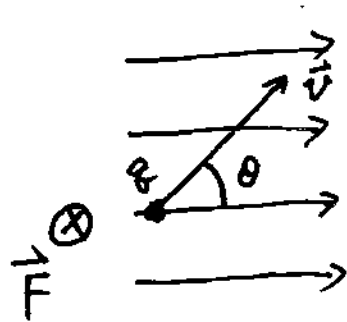
Wed. Oct. 13, 2004

- Magnetic force on a moving charge.

$$\vec{F} = q\vec{v} \times \vec{B}$$

Direction: right-hand rule

Magnitude: $F = qvB \cdot \sin\theta$



①. $\vec{F} \perp \vec{v}$.

\vec{B} field.

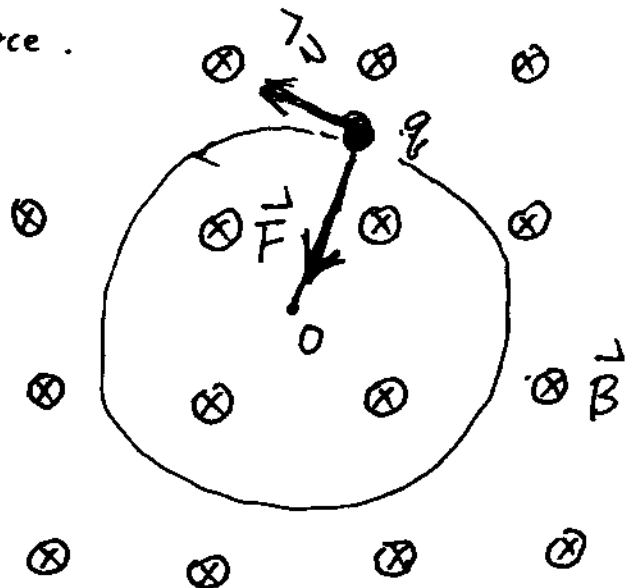
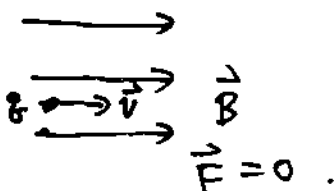
The force only changes the direction of motion of the moving charge.

i.e. it does not speed up or slow down the charge.

e.g. centripetal force.

②. $\vec{F} \perp \vec{B}$.

③. $\vec{F} = 0$ when $\vec{v} \parallel \vec{B}$



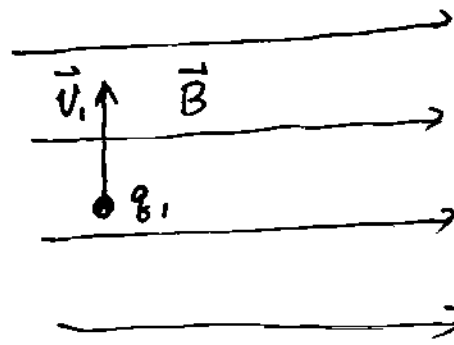
e.g. 22-1. p. 718.

uniform magnetic field \vec{B} .

$$q_1 = 3.60 \mu\text{C}$$

$$v_1 = 862 \text{ m/s.}$$

$$F_1 = 4.25 \times 10^{-3} \text{ N.}$$



Q1: direction of force on q_1 . — into the page. $\otimes \vec{F}$

Q2: $B = ?$

$$\vec{v}_1 \perp \vec{B} : \theta = 90^\circ.$$

$$\vec{F} = q_1 \vec{v}_1 \times \vec{B}. \quad F = q_1 v_1 B \sin \theta = q_1 v_1 B.$$

$$B = \frac{F}{q_1 v_1} = \frac{4.25 \times 10^{-3} \text{ N}}{3.60 \times 10^{-6} \text{ C} \times 862 \text{ m/s}} = 1.37 \text{ T}$$

Q2: $q_2 = 53.0 \mu\text{C}.$

$$v_2 = 1.30 \times 10^3 \text{ m/s.} \quad \text{Now: } \theta = 55.0^\circ.$$

$$\vec{F}_2 = ?$$

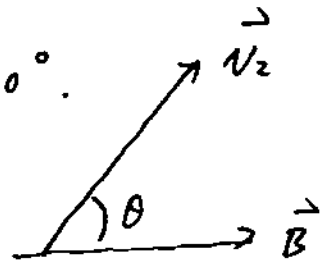
\vec{F}_2 : direction: still into page. \otimes

magnitude:

$$F_2 = q_2 v_2 B \sin \theta$$

$$= 5.3 \times 10^{-5} \times 1.3 \times 10^3 \times 1.37 \times \sin 55^\circ$$

$$= 0.0773 \text{ N.}$$



• Magnetic Torque on a Loop of current .

①. When the loop is in the plane $\parallel \vec{B}$, $\vec{A} \perp \vec{B}$

$$\vec{F}_2 = \vec{F}_4 = 0$$

$$\therefore \vec{v} \parallel \vec{B}$$

\vec{F}_3 — out of page

F_1 — into page .

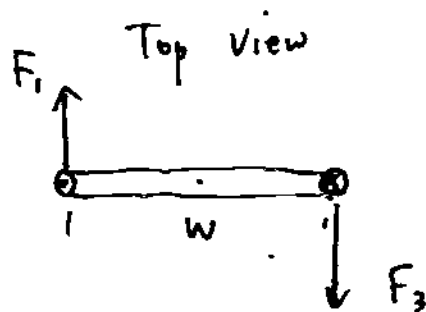
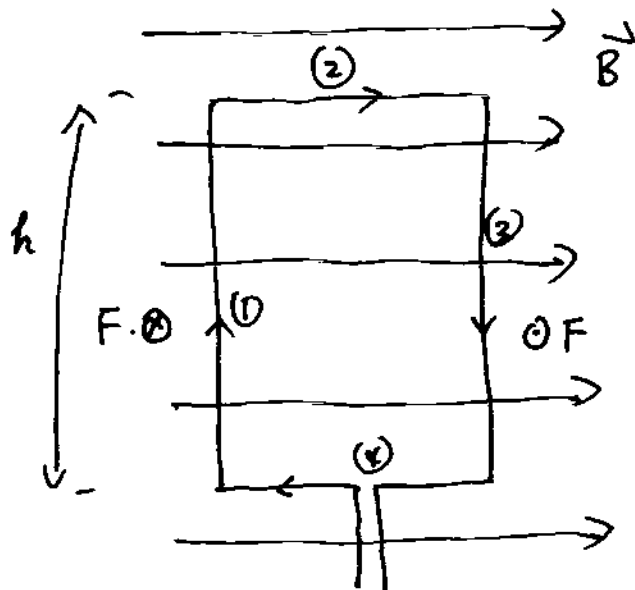
$$F_1 = F_3 = I h B$$

$$\tau = F_1 \frac{w}{2} + F_3 \frac{w}{2}$$

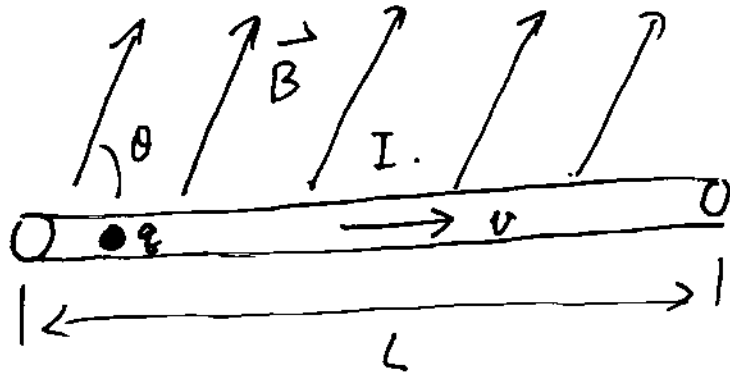
$$= I B h w$$

$$\tau = I B A$$

A — area .



- Magnetic force on a current-carrying wire



In time Δt , charge q has moved by a length of L .

The current:

$$I = \frac{q}{\Delta t}$$

Multiply both sides by L : $I \cdot L = \frac{q \cdot L}{\Delta t} = q \cdot v$.

$$(\because v = \frac{L}{\Delta t})$$

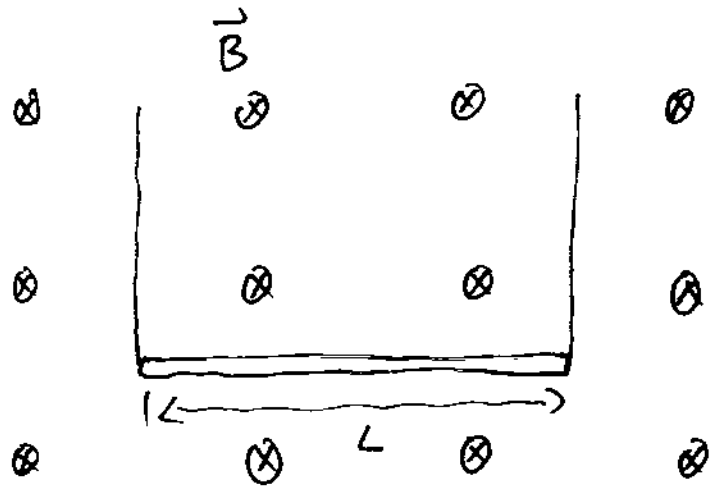
\therefore Magnetic force:

$$F = q v B \cdot \sin \theta = I L B \cdot \sin \theta$$

e.g. 22-4. p. 727

Uniform \vec{B} field.

A copper rod.
suspended from
2 thin wires.



$$L = 1.50 \text{ m}$$

$$m = 0.05 \text{ kg}$$

$$B = 0.55 \text{ T}$$

Want: Lift the copper rod by sending a current I through.

Q1. Direction of current I . \longrightarrow

Q2: magnitude of the current.

$$F = IL \cdot B \cdot \sin \theta = mg$$

$$I = \frac{F}{L \cdot B \sin \theta} = \frac{mg}{LB \sin \theta}$$

$$\theta = 90^\circ$$

$$I = \frac{mg}{LB} = 5.95 \text{ A}$$