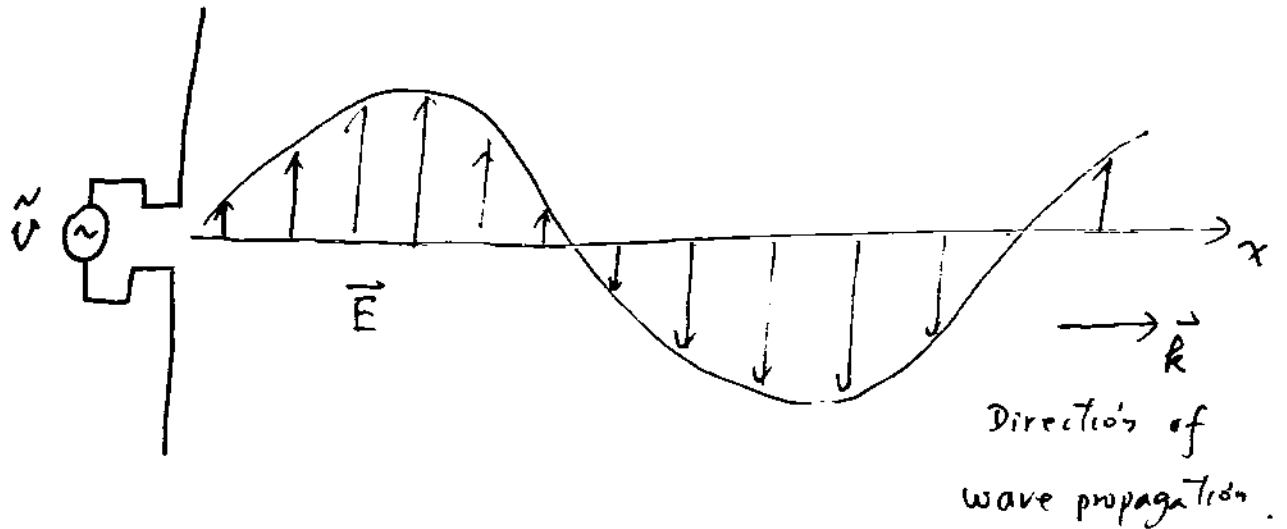


## Physics 102.

Lecture 22.

Monday, Nov. 1, 2004

- A way to generate an electromagnetic wave.

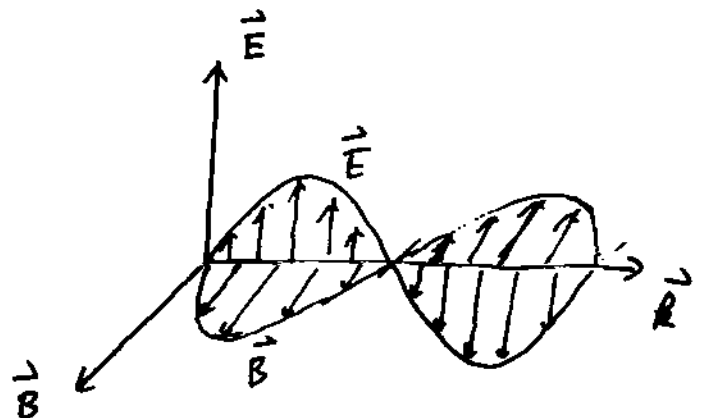


Relationship between the directions of  $\vec{E}$ ,  $\vec{B}$ ,  $\vec{k}$ :

$$\vec{E} \perp \vec{B}, \quad \vec{k} \perp \vec{E}, \quad \vec{k} \perp \vec{B}.$$

$$\vec{k} \parallel (\vec{E} \times \vec{B}) \quad \text{Right hand rule!}$$

- EM wave is a transverse wave.



- Note: Light is also an EM wave!

## • Polarization

In an EM wave, if  $\vec{E}$  oscillates in one direction only (such as in  $z$ -direction), the wave is linearly polarized (in  $z$ -direction).

## • Natural light is unpolarized

e.g., when a wave of natural light is propagating along  $x$ -direction, the  $\vec{E}$  vector <sup>is</sup> randomly distributed in the  $y$ - $z$  plane.

Why? A beam of light is typically generated by many atoms. Each atom is an independent light source. The  $\vec{E}$  direction generated by an ~~atom~~ atom can be arbitrary in the plane perpendicular to the  $\vec{k}$  vector.  
 ↑  
 direction of propagation.

## • Linear Polarizer.

Allows one direction of  $\vec{E}$  to get through  
 $\uparrow$   
 Transmission axis.

When a wave has an  $\vec{E}$  perpendicular to the transmission axis, it will be blocked (absorbed).

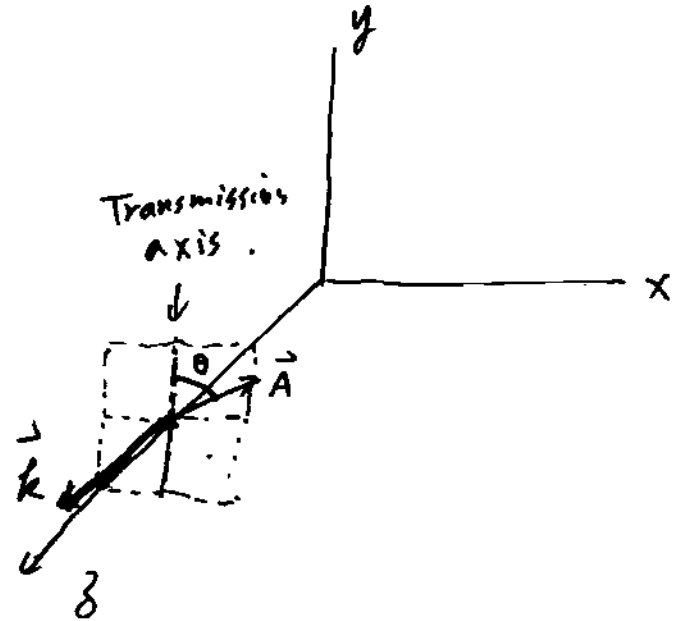
e.g.: When a light beam is propagating along  $z$ -direction, if we put a linear polarizer in front of it with the transmission axis along  $y$ .

①. If the wave is linearly polarized along  $y$ . (i.e.,  $\vec{E} \parallel y$ ).

Then, the wave gets through.  
 $(E_{out} = E_{in})$

②. If the wave is linearly polarized along  $x$  (i.e.,  $\vec{E} \parallel x$ ).

Then the wave is blocked.  
 $(E_{out} = 0)$ .



(3). If the wave is linearly polarized along  $\vec{A}$ ,  
Then only the y-component will get through.

And the wave becomes polarized along y.

(4). If the wave is unpolarized,  $\left( \begin{array}{l} E_{out} = E_{in} \cdot \cos \theta \\ I_{out} = I_{in} \cdot \cos^2 \theta \end{array} \right)$   $\left( \begin{array}{l} \because I \propto E^2 \end{array} \right)$

The wave will become linearly polarized along y.  $(E_{out} \text{ is along } y.)$

$\therefore$  No matter what, after the wave goes through the polarizer, it will become linearly polarized along the transmission axis direction).

• Polarization analyzer.

— to examine a wave and see if it is polarized.

A linear polarizer is a polarization analyzer at the same time because it can tell us if a wave is polarized.

Demo :

• Facts about EM waves.

①. Speed in vacuum (free space).

$$c = 3.00 \times 10^8 \text{ m/s} \cdot \left( = \frac{1}{\sqrt{\epsilon_0 \mu_0}} \right)$$

Regardless the motion of source or observer !!

That's the base of Einstein's Relativity Theory.

②. The Doppler effect.

$$f' = f \left( 1 \pm \frac{u}{c} \right)$$

$u$  — relative speed between source and observer.

+ — approaching. (higher  $f$ )

- — receding. (lower  $f$ ).

③. Energy.

Energy density:  $\vec{E}$ -field:  $u_E = \frac{1}{2} \epsilon_0 E^2$ .

$\vec{B}$ -field:  $u_B = \frac{1}{2} \mu_0 B^2$ .

Note:  $u_E = u_B$ .

$$\frac{1}{2} \epsilon_0 E^2 = \frac{1}{2} \mu_0 B^2$$

$$E = \frac{1}{\sqrt{\epsilon_0 \mu_0}} B = c \cdot B$$

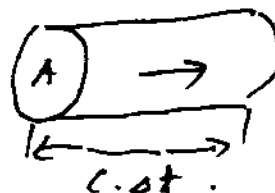
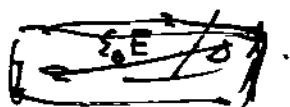
Total Energy density:  $U = U_E + U_B$

$$= \epsilon_0 E^2$$

$$= \frac{B^2}{\mu_0}$$

• Intensity:

$$I = \frac{\text{Power}}{\text{area}} = \frac{\text{Energy}/\Delta t}{\text{area}} = \frac{U \cdot \text{Volume}/\Delta t}{\text{area}}$$



$$\therefore I = \frac{\epsilon_0 E^2 \cdot (A \cdot c \cdot \Delta t) / \Delta t}{A} = \epsilon_0 E^2 c = Uc$$

$$= \frac{B^2}{\mu_0} c$$

• Momentum:

$$p = \frac{U}{c} = \frac{U \cdot (A \cdot c \cdot \Delta t)}{c} = UA \cdot \Delta t$$

• Pressure:

(absorption)

$$P_{av} = \frac{F_{av}}{\Delta t \cdot A} = U = \frac{I}{c}$$

$$P_r = 0$$

- The electromagnetic spectrum (you read) (25-3. p. 825)

wavelength :  $\lambda = \frac{c}{f}$  in vacuum.

$f$  - frequency

in a medium :  $\lambda = \frac{v}{f}$ .

$v$  — velocity of the wave.

$v \leq c$