

Lecture 25

Mon. Nov. 8, 2004

- Ray-tracing for spherical mirrors
 - to determine the location, size, orientation of the image of an object.

①. P. ray.

Concave: The parallel ray reflects through the focal point.

②. F ray. (for convex mirrors, the extrapolation of the reflected ray goes through F.)

The focal ray reflects parallel to the axis.

③. C ray.

The centre ray reflects back along its incoming path.

Any two rays will determine the image.

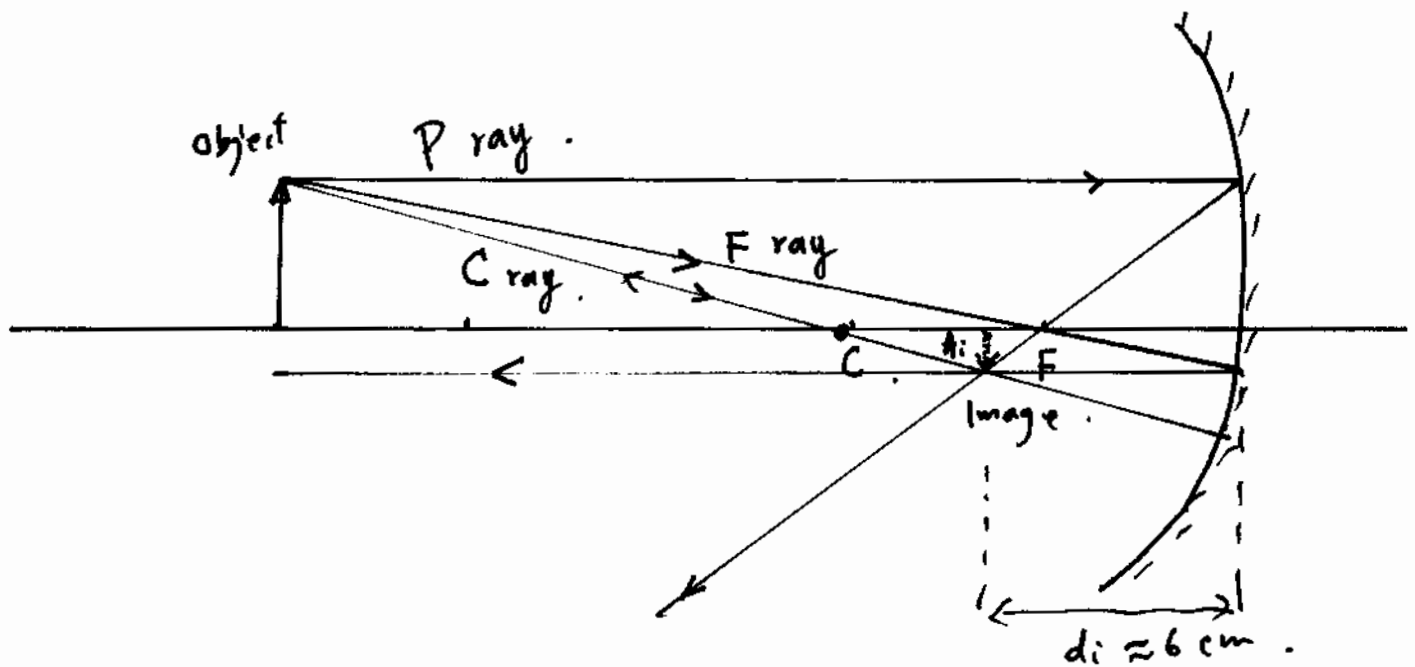
We can use the third as a check.

- Focal Point: $\begin{cases} f = \frac{1}{2}R & \text{— concave. in front of mirror} \\ f = -\frac{1}{2}R & \text{— convex. behind mirror.} \end{cases}$

e.g. A concave mirror. (9.861)
 $f = 5.00 \text{ cm}$ ($R = 10 \text{ cm}$).

An object with a height of 4.0 cm . (~~$h_o = 1.0 \text{ cm}$~~)
 is located 25 cm in front of the mirror. (~~$d_o = 25.0 \text{ cm}$~~)

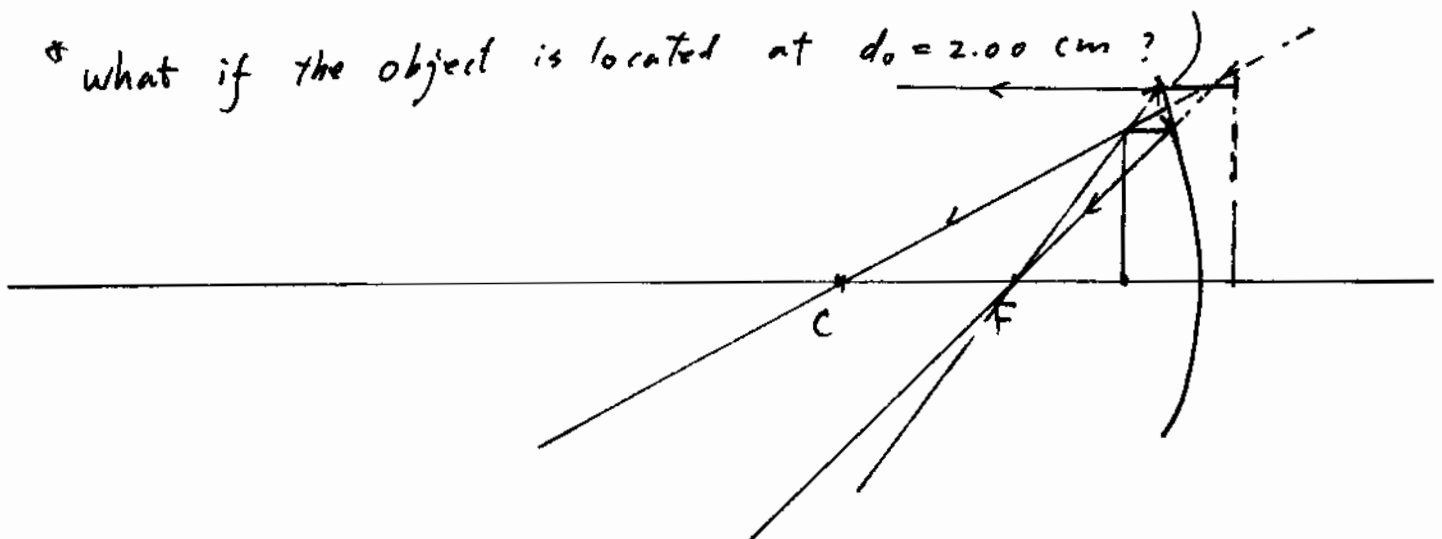
Where is the image?



$$d_i \approx 6 \text{ cm}$$

$$h_i \approx \overline{1.0} \text{ cm} \quad (-): \text{ inverted}$$

* What if the object is located at $d_o = 2.00 \text{ cm}$?



The Mirror Equation (p.859)

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}$$

$$f = \frac{1}{2} R$$

$$\frac{h_o}{-h_i} = \frac{d_o}{d_i}$$

Magnification:

$$M = \frac{h_i}{h_o} = -\frac{d_i}{d_o}$$

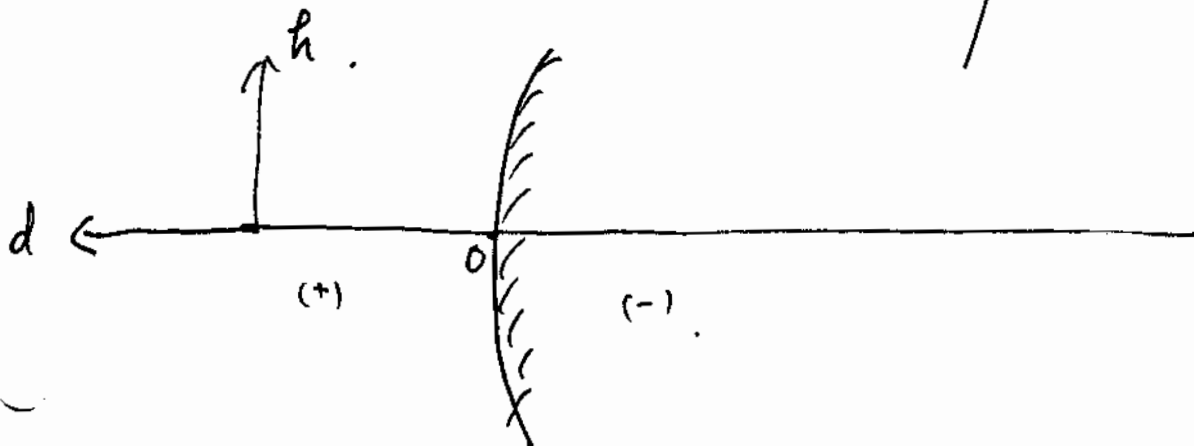
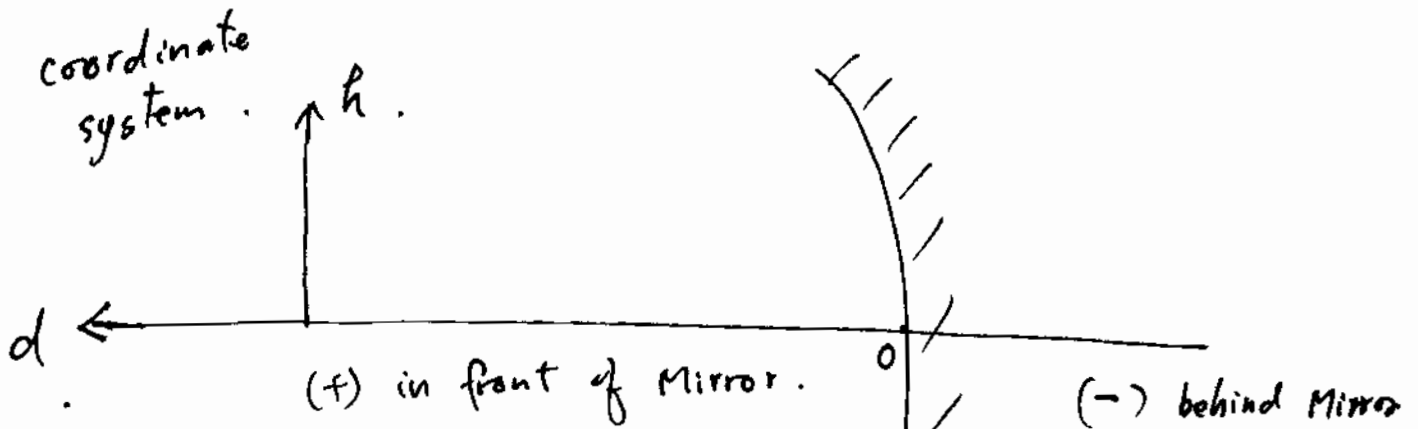
d_o — Mirror-object distance.

d_i — Mirror-image distance.

f : $\begin{cases} (+) \text{ concave} \\ (-) \text{ convex} \end{cases}$

h_o, h_i — $\begin{cases} + \text{ upright} \\ - \text{ inverted} \\ \text{(downward)} \end{cases}$

M : $\begin{cases} (+) \text{ upright} \\ (-) \text{ inverted} \end{cases}$



e.g. #36. of ch.26. (p.883)

A concave mirror with a focal length of 36 cm produces an image whose distance from the mirror is one-third the object distance. Find the object and image distances:

given: $f = 36 \text{ cm}$, $d_i = \frac{1}{3} d_o$, $d_o = 3 d_i$.

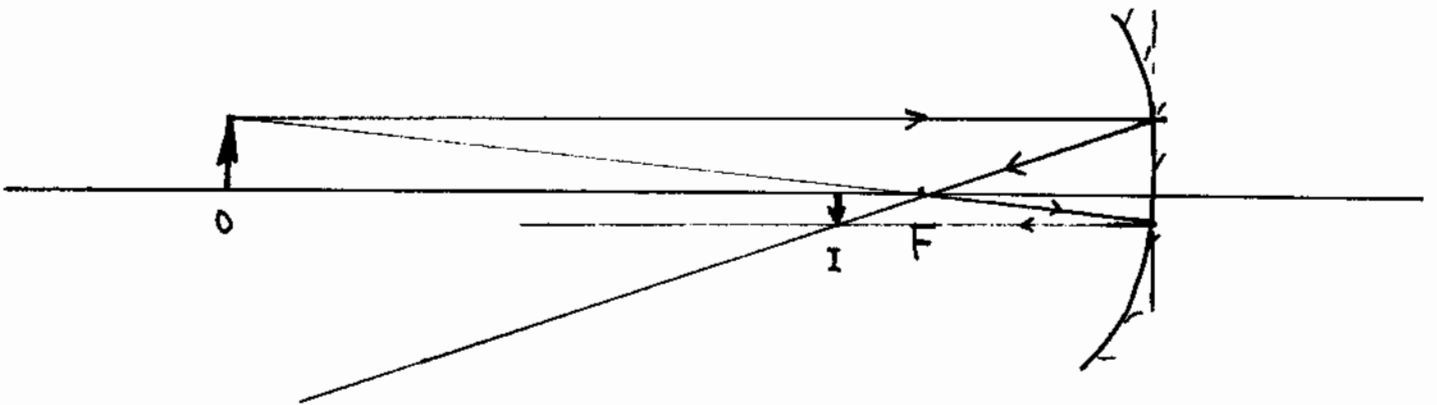
find: $d_i = ?$ $d_o = ?$

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}, \quad \frac{1}{3d_i} + \frac{1}{d_i} = \frac{1}{f}.$$

$$\frac{4}{3d_i} = \frac{1}{f}.$$

$$d_i = \frac{4}{3} f = \frac{4}{3} \times 36 = 48 \text{ cm}.$$

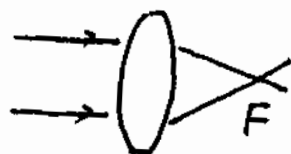
$$d_o = 3 d_i = 144 \text{ cm}.$$



Lenses.

25-5-

Converging : e.g.

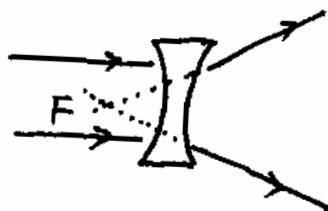


$$f > 0$$

double-convex

ray bent ~~away~~ toward the axis.

diverging. e.g.



$$f < 0$$

double-concave. Rays bent away.

Ray Tracing for thin lenses.

— lens is thin.

— Angles are small.

① P-ray : Will be bent and through F. (convex)
[concave : extrapolates through F]

② F-ray : bent to parallel

③ M-ray (Midpoint ray) : No bending when a ray goes through the centre of lens.