

# Phys102 Lecture 7/8

## Capacitors

### Key Points

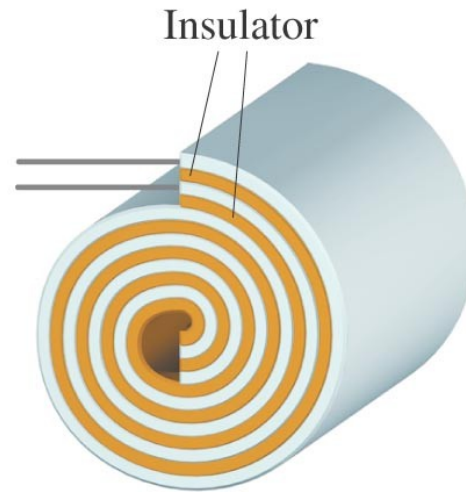
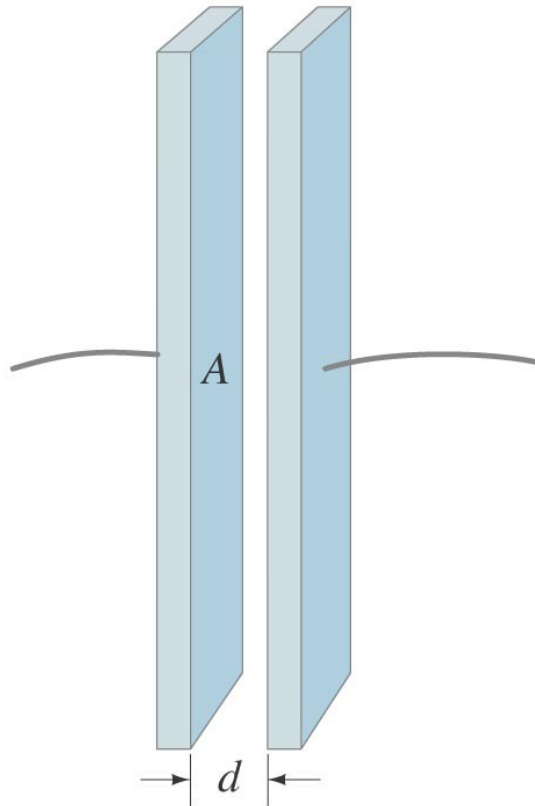
- Capacitors
- Determination of Capacitance
- Capacitors in Series and Parallel
- Electric Energy Storage
- Dielectrics

### References

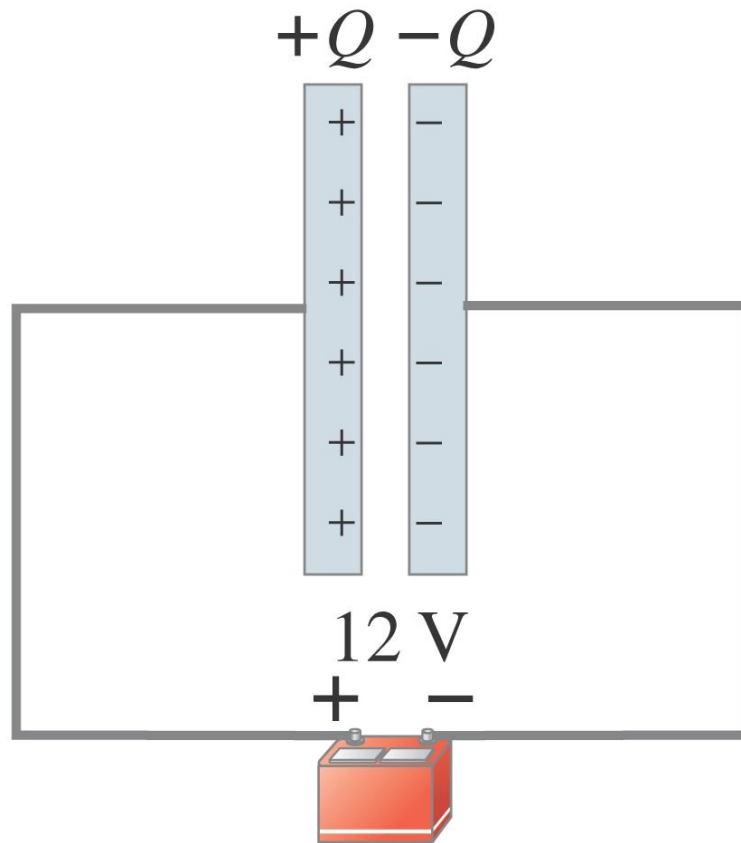
SFU Ed: 24-1,2,3,4,5,6.

6<sup>th</sup> Ed: 17-7,8,9,10+.

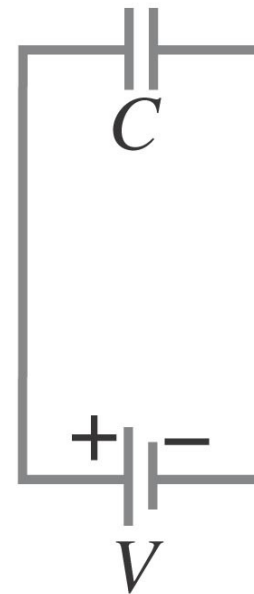
**A capacitor consists of two conductors that are close but not touching. A capacitor has the ability to store electric charge.**



**Parallel-plate capacitor connected to battery. (b) is a circuit diagram.**



(a)



(b)

# 24-1 Capacitors

**When a capacitor is connected to a battery, the charge on its plates is proportional to the voltage:**

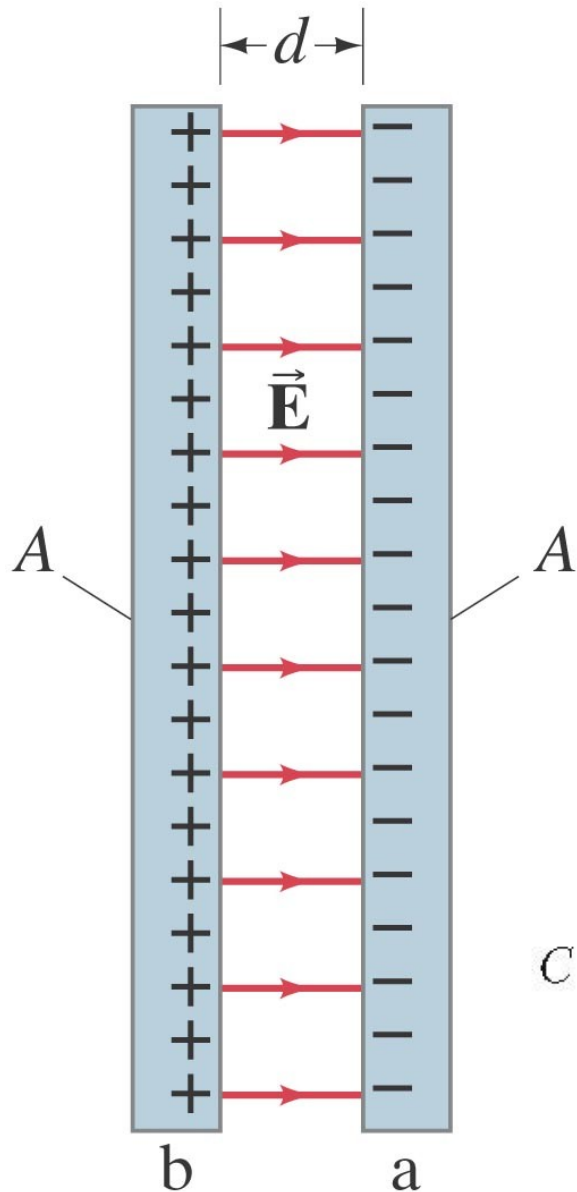
$$Q = CV.$$

**The quantity  $C$  is called the capacitance.**

**Unit of capacitance: the farad (F):**

$$1 \text{ F} = 1 \text{ C/V}.$$

# Determination of Capacitance



For a parallel-plate capacitor as shown, the field between the plates is

$$E = Q/\epsilon_0 A.$$

The potential difference:

$$V_{ba} = Ed = Qd/\epsilon_0 A.$$

This gives the capacitance:

$$C = \frac{Q}{V} = \epsilon_0 \frac{A}{d}.$$

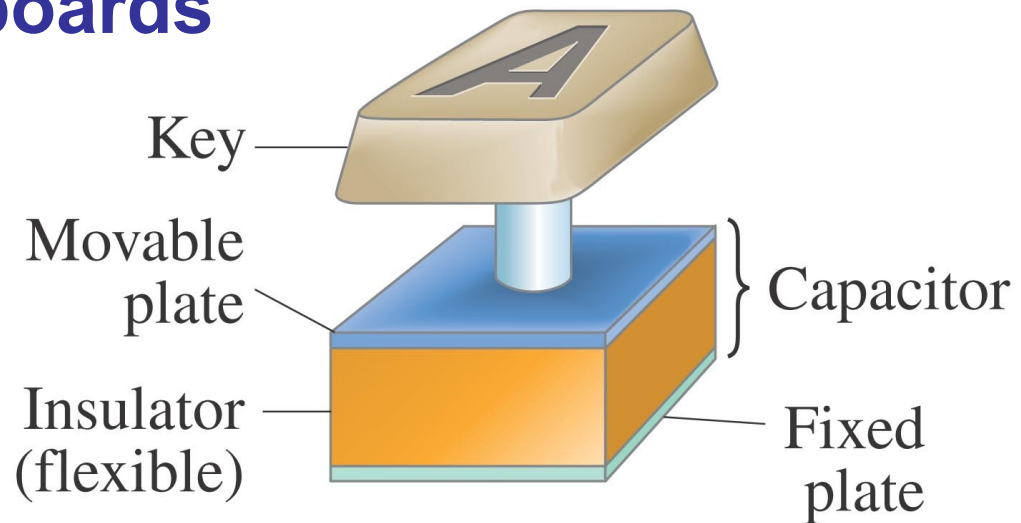
[parallel-plate capacitor]

## Example 24-1: Capacitor calculations.

(a) Calculate the capacitance of a parallel-plate capacitor whose plates are  $20\text{ cm} \times 3.0\text{ cm}$  and are separated by a  $1.0\text{-mm}$  air gap. (b) What is the charge on each plate if a  $12\text{-V}$  battery is connected across the two plates? (c) What is the electric field between the plates? (d) Estimate the area of the plates needed to achieve a capacitance of  $1\text{ F}$ , given the same air gap  $d$ .

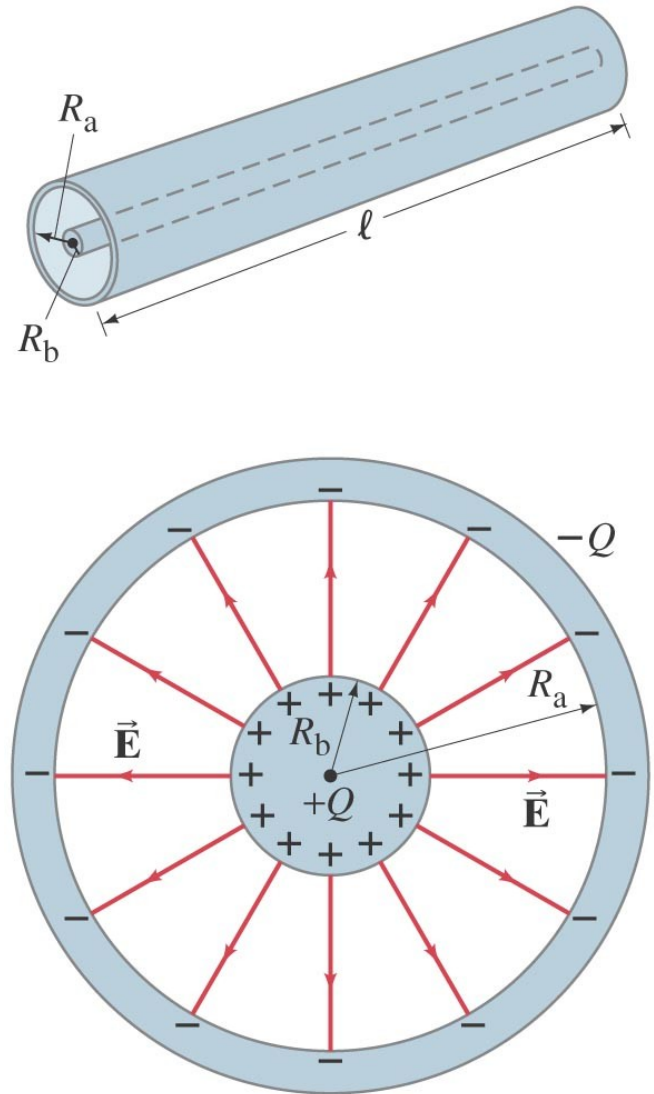
Capacitors are now made with capacitances of 1 farad or more, but they are not parallel-plate capacitors. Instead, they are activated carbon, which acts as a capacitor on a very small scale. The capacitance of 0.1 g of activated carbon is about 1 farad.

Some computer keyboards use capacitors; depressing the key changes the capacitance, which is detected in a circuit.



## Example 24-2: Cylindrical capacitor.

A cylindrical capacitor consists of a cylinder (or wire) of radius  $R_b$  surrounded by a coaxial cylindrical shell of inner radius  $R_a$ . Both cylinders have length  $\ell$  which we assume is much greater than the separation of the cylinders, so we can neglect end effects. The capacitor is charged (by connecting it to a battery) so that one cylinder has a charge  $+Q$  (say, the inner one) and the other one a charge  $-Q$ . Determine a formula for the capacitance.

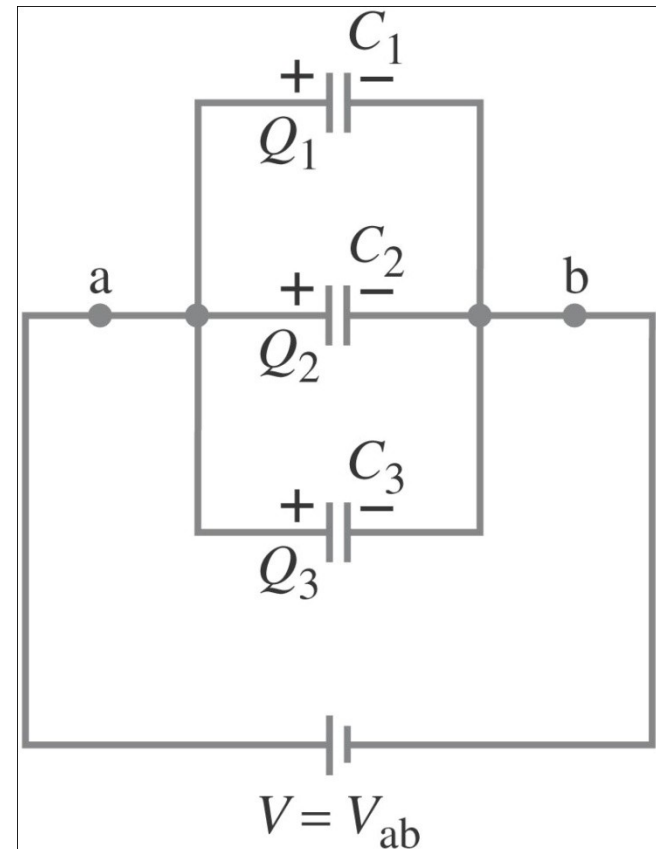




# Capacitors in Series and Parallel

Capacitors in parallel have the same voltage across each one. The equivalent capacitor is one that stores the same charge when connected to the same battery:

$$C_{\text{eq}} = C_1 + C_2 + C_3.$$

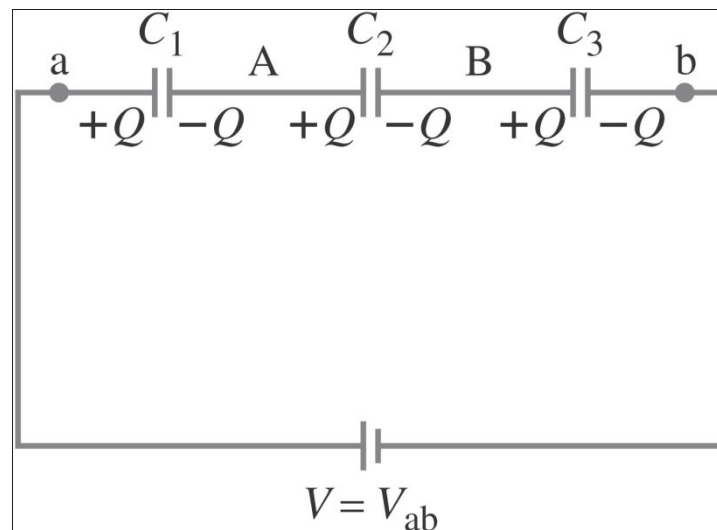


[parallel]

# Capacitors in Series and Parallel

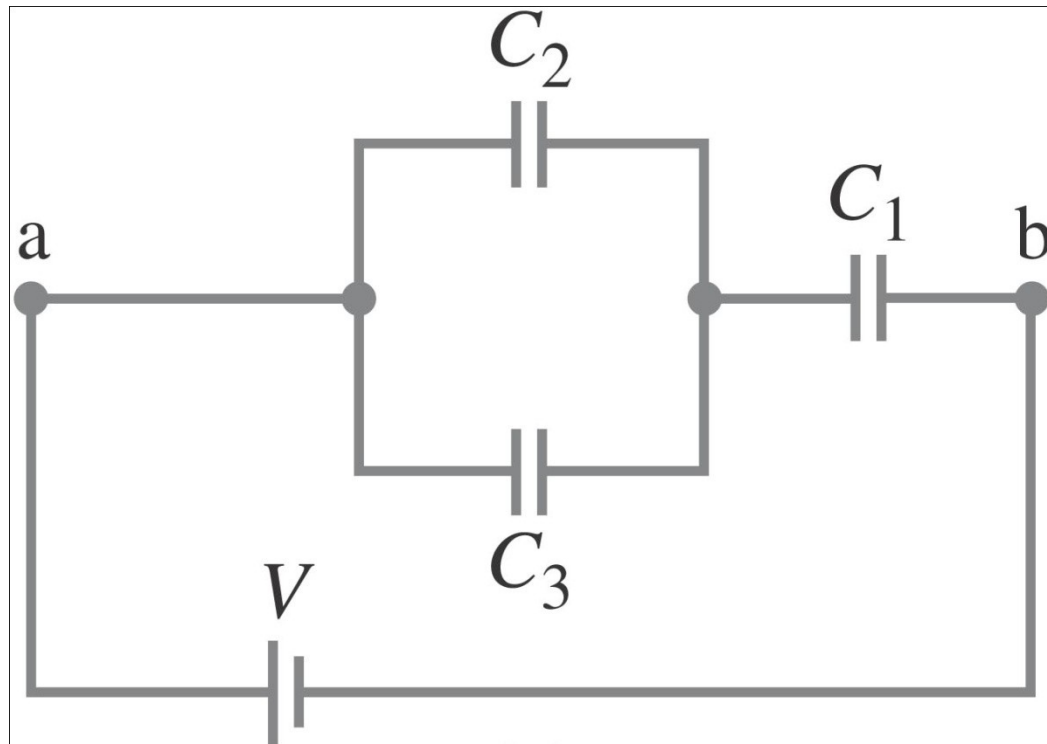
**Capacitors in series have the same charge. In this case, the equivalent capacitor has the same charge across the total voltage drop. Note that the formula is for the inverse of the capacitance and not the capacitance itself!**

$$\frac{1}{C_{\text{eq}}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}. \quad [\text{series}]$$



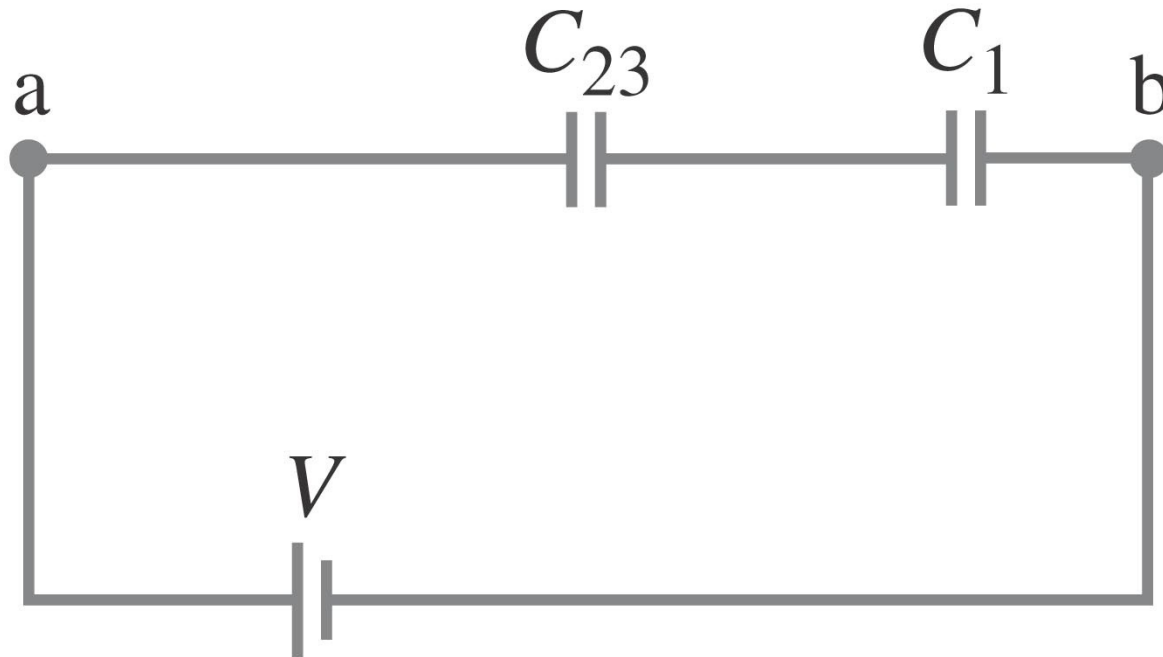
## Example 24-5: Equivalent capacitance.

Determine the capacitance of a single capacitor that will have the same effect as the combination shown.



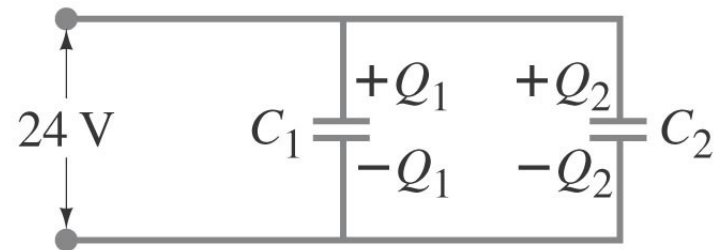
## Example 24-6: Charge and voltage on capacitors.

Determine the charge on each capacitor and the voltage across each, assuming  $C = 3.0 \mu\text{F}$  and the battery voltage is  $V = 4.0 \text{ V}$ .

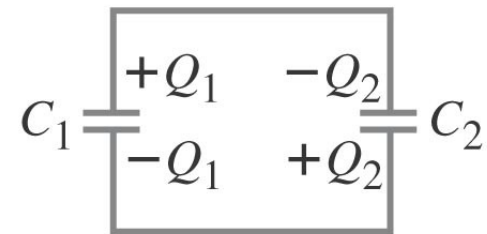


## Example 24-7: Capacitors reconnected.

Two capacitors,  $C_1 = 2.2 \mu\text{F}$  and  $C_2 = 1.2 \mu\text{F}$ , are connected in parallel to a 24-V source as shown. After they are charged they are disconnected from the source and from each other and then reconnected directly to each other, with plates of opposite sign connected together. Find the charge on each capacitor and the potential across each after equilibrium is established.



Initial configuration.



At the instant of reconnection only.



A short time later.

# 24-4 Electric Energy Storage

**A charged capacitor stores electric energy; the energy stored is equal to the work done to charge the capacitor:**

$$U = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} CV^2 = \frac{1}{2} QV.$$

# Electric Energy Storage

**Example 24-8: Energy stored in a capacitor.**

**A camera flash unit stores energy in a  $150\text{-}\mu\text{F}$  capacitor at  $200\text{ V}$ . (a) How much electric energy can be stored? (b) What is the power output if nearly all this energy is released in  $1.0\text{ ms}$ ?**



# 24-4 Electric Energy Storage

**Conceptual Example 24-9: Capacitor plate separation increased.**

**A parallel-plate capacitor carries charge  $Q$  and is then disconnected from a battery. The two plates are initially separated by a distance  $d$ . Suppose the plates are pulled apart until the separation is  $2d$ . How has the energy stored in this capacitor changed?**



## 24-4 Electric Energy Storage

The energy density, defined as the energy per unit volume, is the same no matter the origin of the electric field:

$$u = \text{energy density} = \frac{1}{2} \epsilon_0 E^2.$$

The sudden discharge of electric energy can be harmful or fatal. Capacitors can retain their charge indefinitely even when disconnected from a voltage source – be careful!

## 24-5 Dielectrics

A dielectric is an insulator, and is characterized by a dielectric constant  $K$ .

Capacitance of a parallel-plate capacitor filled with dielectric:

$$C = K\epsilon_0 \frac{A}{d}. \quad [\text{parallel-plate capacitor}]$$

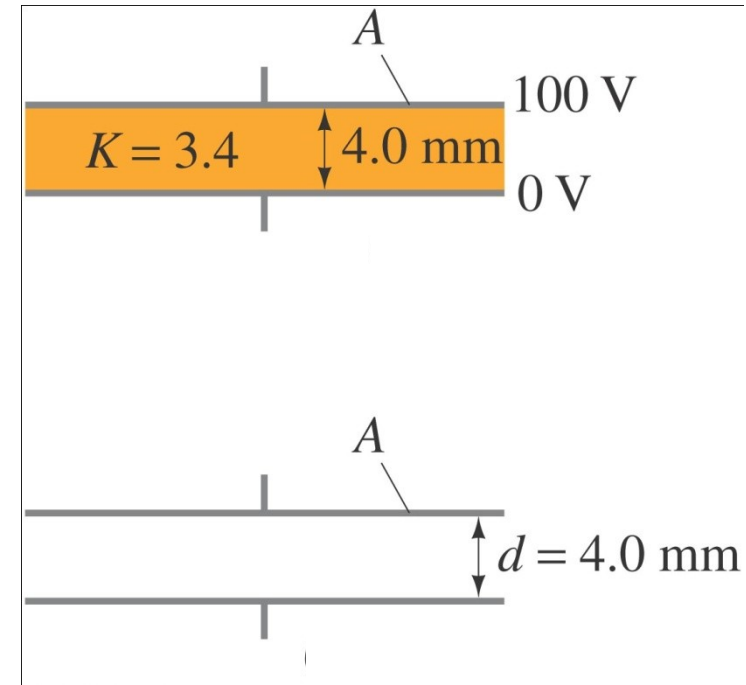
Using the dielectric constant, we define the permittivity:

$$\epsilon = K\epsilon_0.$$

# 24-5 Dielectrics

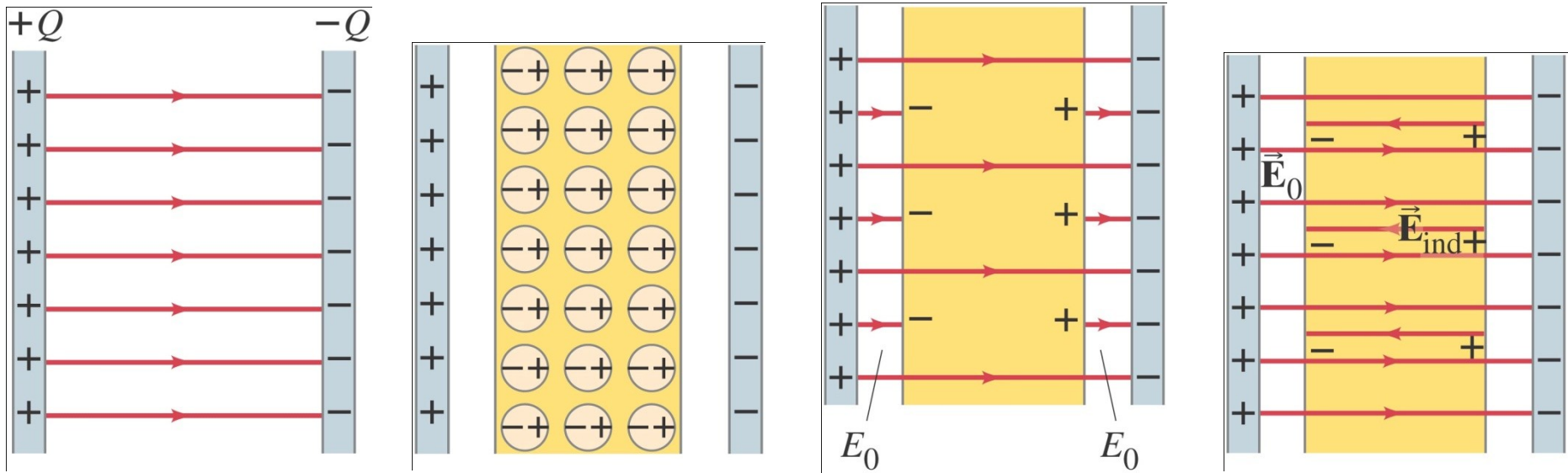
## Example 24-11: Dielectric removal.

A parallel-plate capacitor, filled with a dielectric with  $K = 3.4$ , is connected to a 100-V battery. After the capacitor is fully charged, the battery is disconnected. The plates have area  $A = 4.0 \text{ m}^2$  and are separated by  $d = 4.0 \text{ mm}$ . (a) Find the capacitance, the charge on the capacitor, the electric field strength, and the energy stored in the capacitor. (b) The dielectric is carefully removed, without changing the plate separation nor does any charge leave the capacitor. Find the new values of capacitance, electric field strength, voltage between the plates, and the energy stored in the capacitor.



# Molecular Description of Dielectrics

The molecules in a dielectric, when in an external electric field, tend to become oriented in a way that reduces the external field.



# Summary of Chapter 24

- **Capacitor: nontouching conductors carrying equal and opposite charge.**
- **Capacitance:**

$$Q = CV.$$

- **Capacitance of a parallel-plate capacitor:**

$$C = \frac{Q}{V} = \epsilon_0 \frac{A}{d}. \quad [\text{parallel-plate capacitor}]$$

# Summary of Chapter 24

- **Capacitors in parallel:**

$$C_{\text{eq}} = C_1 + C_2 + C_3. \quad [\text{parallel}]$$

- **Capacitors in series:**

$$\frac{1}{C_{\text{eq}}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}. \quad [\text{series}]$$

# Summary of Chapter 24

- **Energy density in electric field:**

$$u = \text{energy density} = \frac{1}{2} \epsilon_0 E^2.$$

- **A dielectric is an insulator.**
- **Dielectric constant gives ratio of total field to external field.**
- **For a parallel-plate capacitor:**

$$C = K \epsilon_0 \frac{A}{d} \qquad \text{[parallel-plate capacitor]}$$