

# Phys102 Lecture 13/14

## DC Circuits

### Key Points

- EMF and Terminal Voltage
- Resistors in Series and in Parallel
- Circuits Containing Resistor and Capacitor (*RC* Circuits)

### References

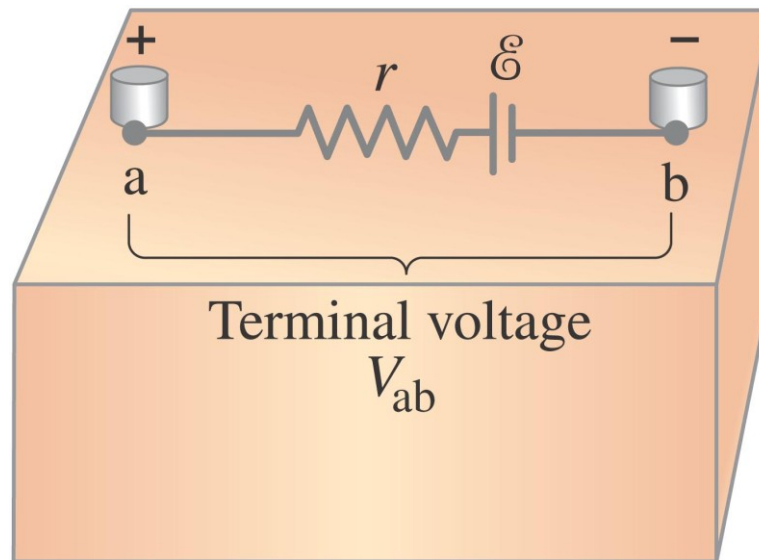
SFU Ed: 26-1,2,5.

6<sup>th</sup> Ed: 19-1,2,5,6.

# 26-1 EMF and Terminal Voltage

Electric circuit needs battery or generator to produce current – these are called sources of emf.

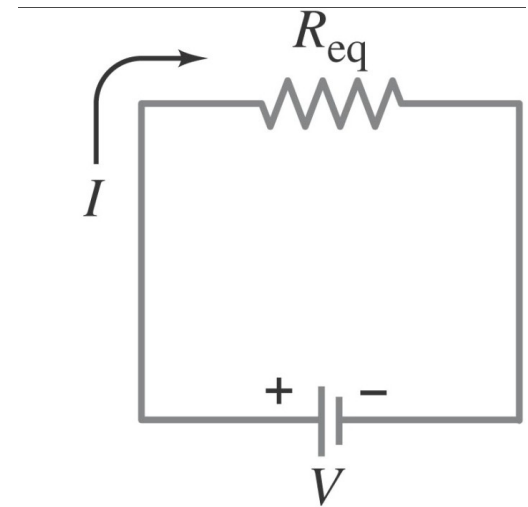
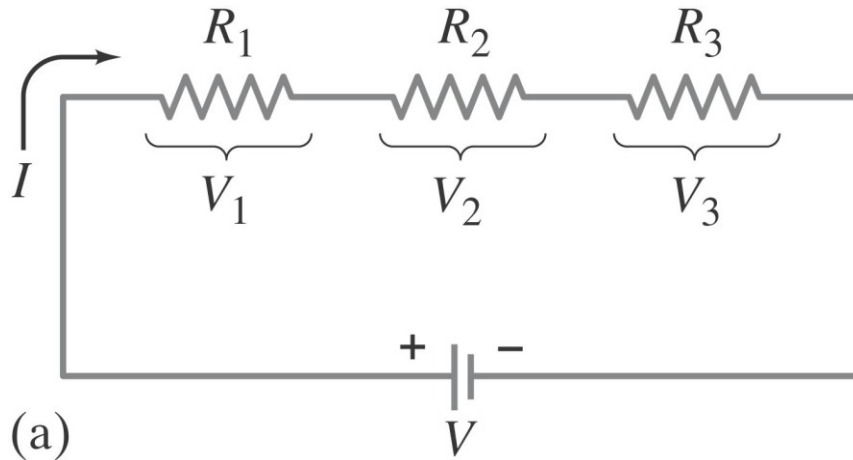
Battery is a nearly constant voltage source, but does have a small internal resistance (in series with the emf) , which reduces the actual voltage from the ideal emf:



$$V_{ab} = \mathcal{E} - Ir.$$

# Resistors in Series

**A series connection has a single path with the same current.**



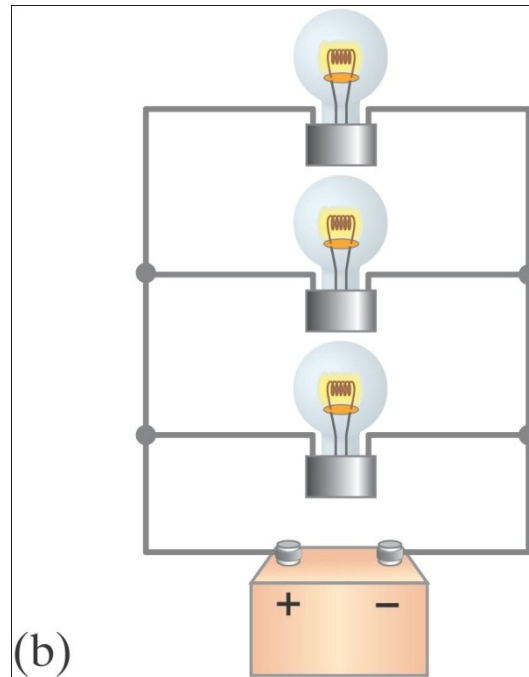
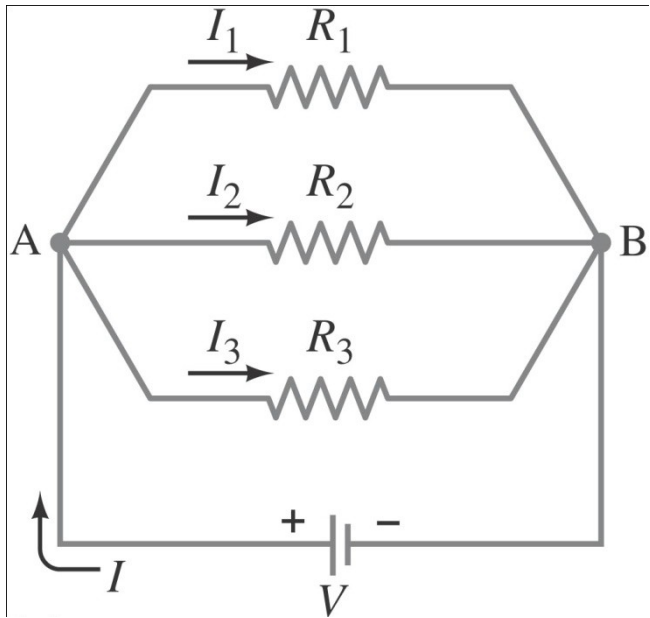
**The sum of the voltage drops across the resistors equals the battery voltage**

$$V = V_1 + V_2 + V_3 = IR_1 + IR_2 + IR_3. \quad [\text{series}]$$

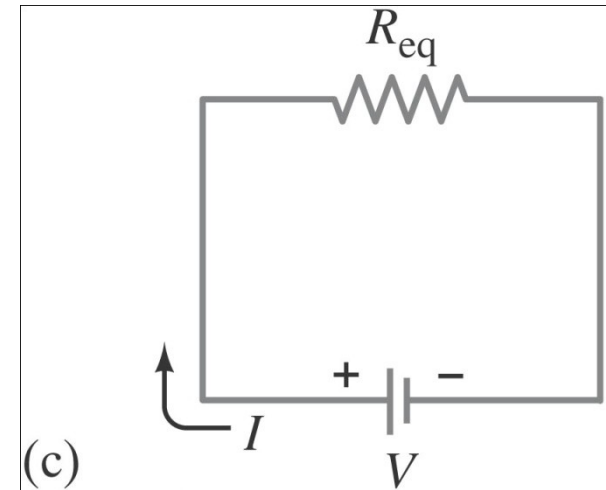
$$R_{\text{eq}} = R_1 + R_2 + R_3. \quad [\text{series}]$$

# Resistors in Parallel

**A parallel connection splits the current; the voltage across each resistor is the same:**



(b)



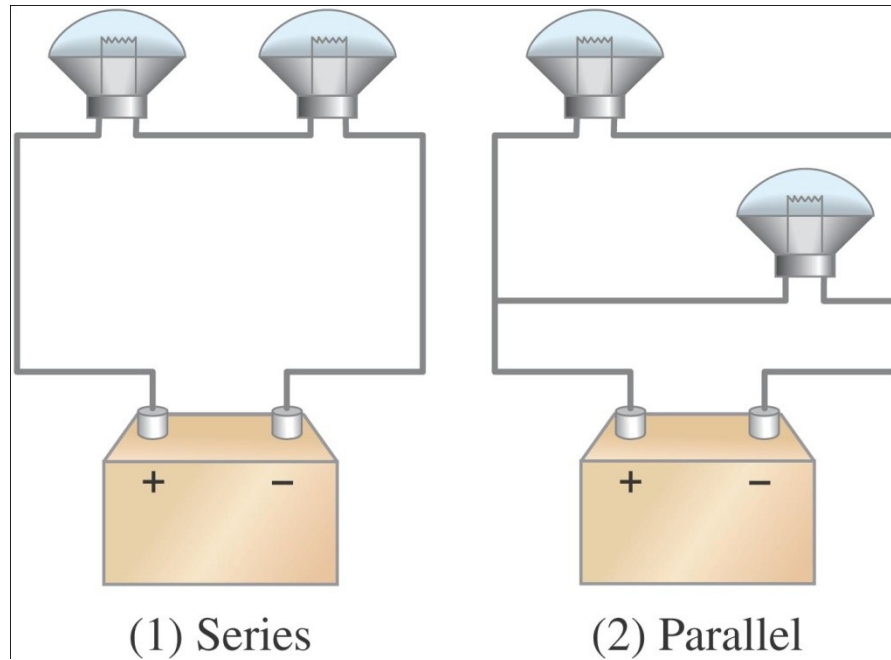
(c)

$$I = I_1 + I_2 + I_3$$
$$\frac{V}{R_{eq}} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}.$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

## Conceptual Example 26-2: Series or parallel?

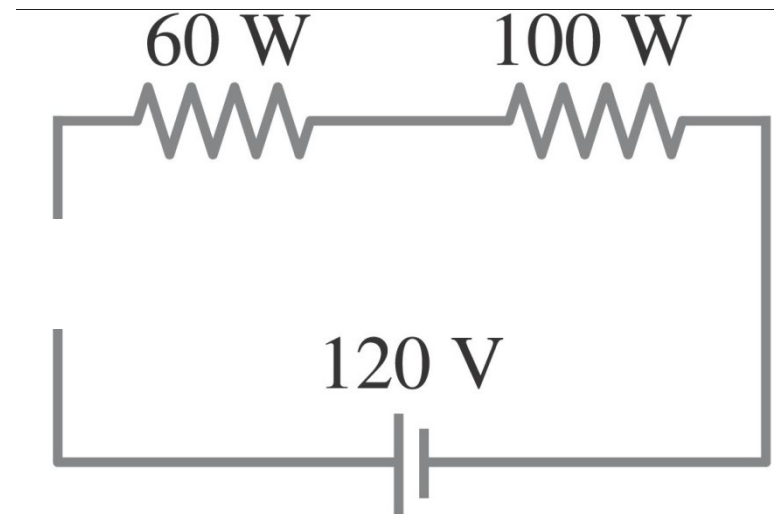
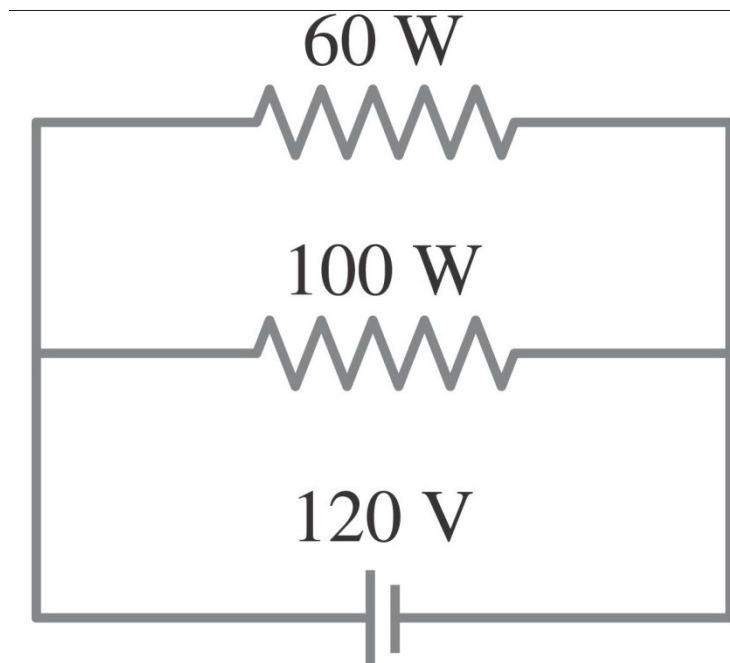
(a) The lightbulbs in the figure are identical. Which configuration produces more light? (b) Which way do you think the headlights of a car are wired? Ignore change of filament resistance  $R$  with current.



## 26-2 Resistors in Series and in Parallel

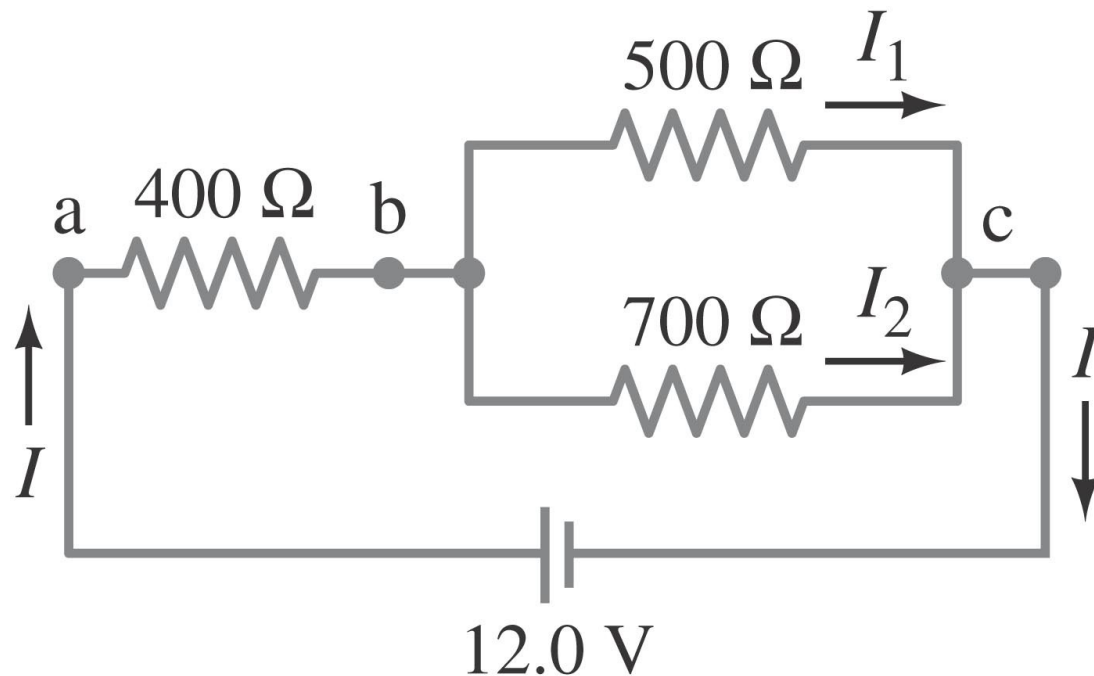
**Conceptual Example 26-3: An illuminating surprise.**

**A 100-W, 120-V lightbulb and a 60-W, 120-V lightbulb are connected in two different ways as shown. In each case, which bulb glows more brightly? Ignore change of filament resistance with current (and temperature).**



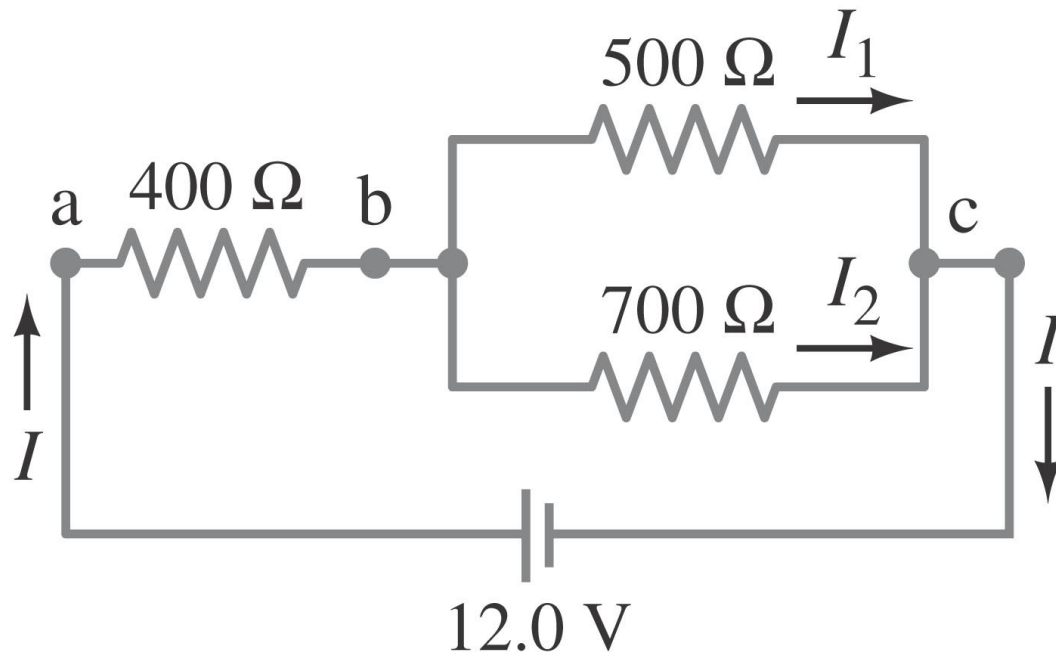
## Example 26-4: Circuit with series and parallel resistors.

How much current is drawn from the battery shown?



### Example 26-5: Current in one branch.

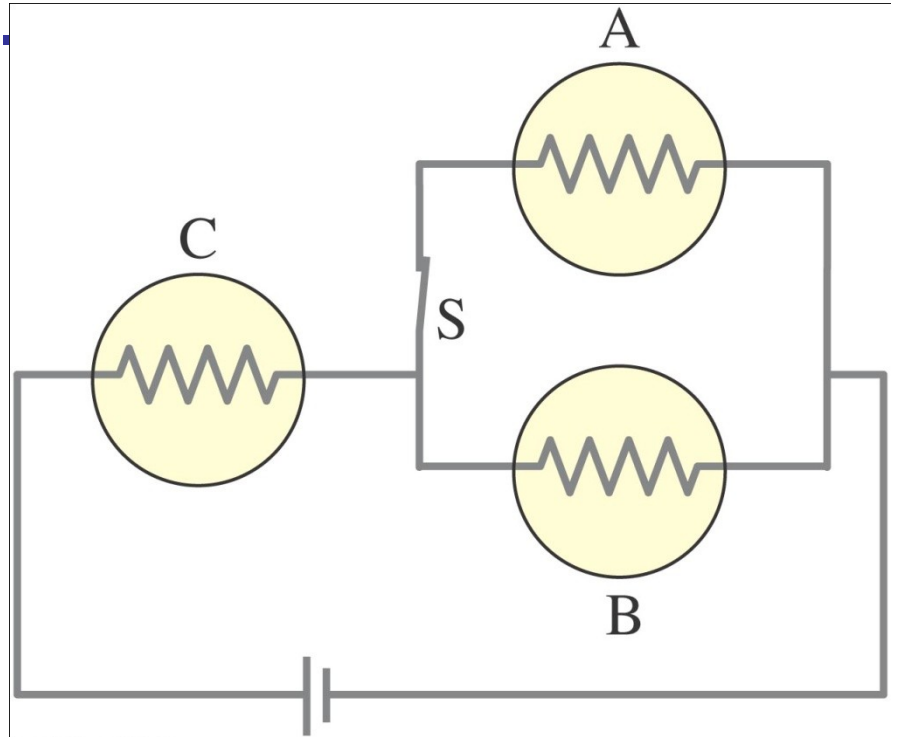
What is the current through the  $500\text{-}\Omega$  resistor shown? (Note: This is the same circuit as in the previous problem.) The total current in the circuit was found to be  $17\text{ mA}$ .





## Conceptual Example 26-6: Bulb brightness in a circuit.

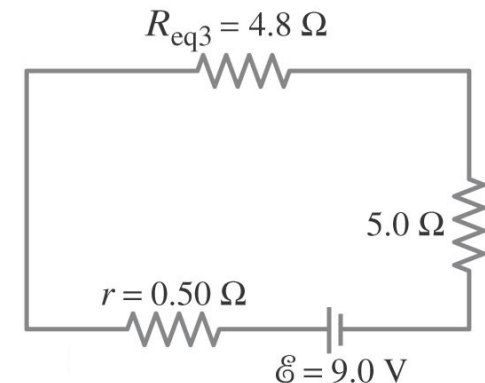
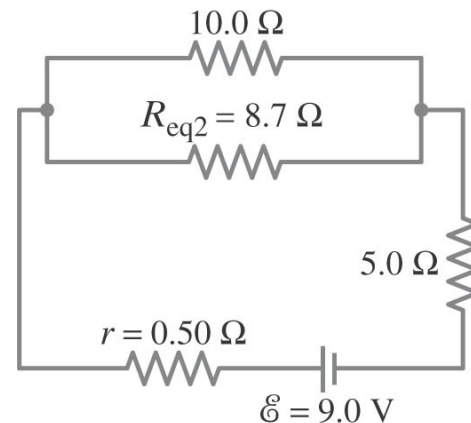
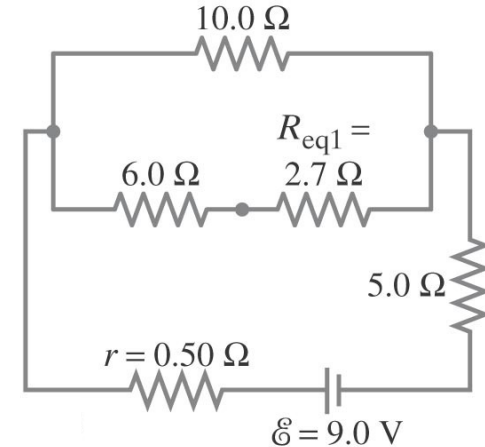
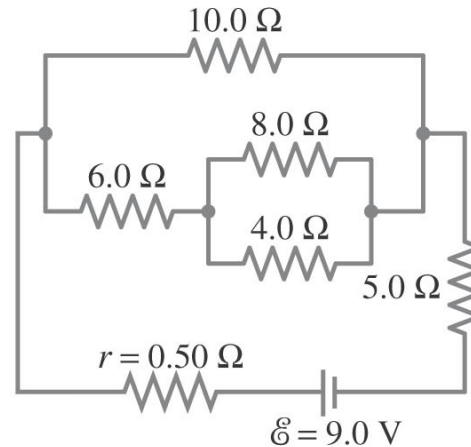
The circuit shown has three identical lightbulbs, each of resistance  $R$ . (a) When switch  $S$  is closed, how will the brightness of bulbs  $A$  and  $B$  compare with that of bulb  $C$ ? (b) What happens when switch  $S$  is opened? Use a minimum of mathematics in your answers.



# 26-2 Resistors in Series and in Parallel

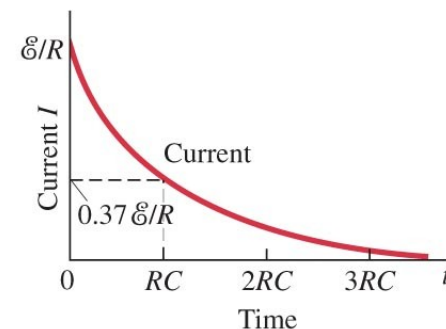
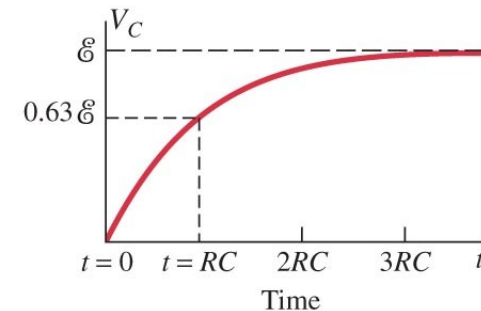
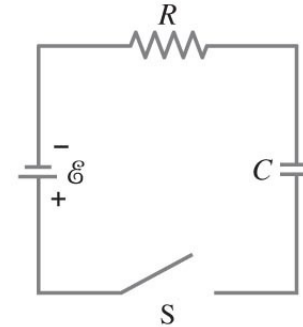
## Example 26-8: Analyzing a circuit.

A 9.0-V battery whose internal resistance  $r$  is  $0.50\ \Omega$  is connected in the circuit shown. (a) How much current is drawn from the battery? (b) What is the terminal voltage of the battery? (c) What is the current in the  $6.0\text{-}\Omega$  resistor?



# 26-5 Circuits Containing Resistor and Capacitor ( $RC$ Circuits)

When the switch is closed, the capacitor will begin to charge. As it does, the voltage across it increases, and the current through the resistor decreases.



## 26-5 Circuits Containing Resistor and Capacitor ( $RC$ Circuits)

To find the voltage as a function of time, we write the equation for the voltage changes around the loop:

$$\mathcal{E} = IR + \frac{Q}{C}.$$

Since  $Q = dI/dt$ , we can integrate to find the charge as a function of time:

$$Q = C\mathcal{E}(1 - e^{-t/RC}).$$

## 26-5 Circuits Containing Resistor and Capacitor ( $RC$ Circuits)

The voltage across the capacitor is  $V_C = Q/C$ :

$$V_C = \mathcal{E}(1 - e^{-t/RC}).$$

The quantity  $RC$  that appears in the exponent is called the time constant of the circuit:

$$\tau = RC.$$

## 26-5 Circuits Containing Resistor and Capacitor ( $RC$ Circuits)

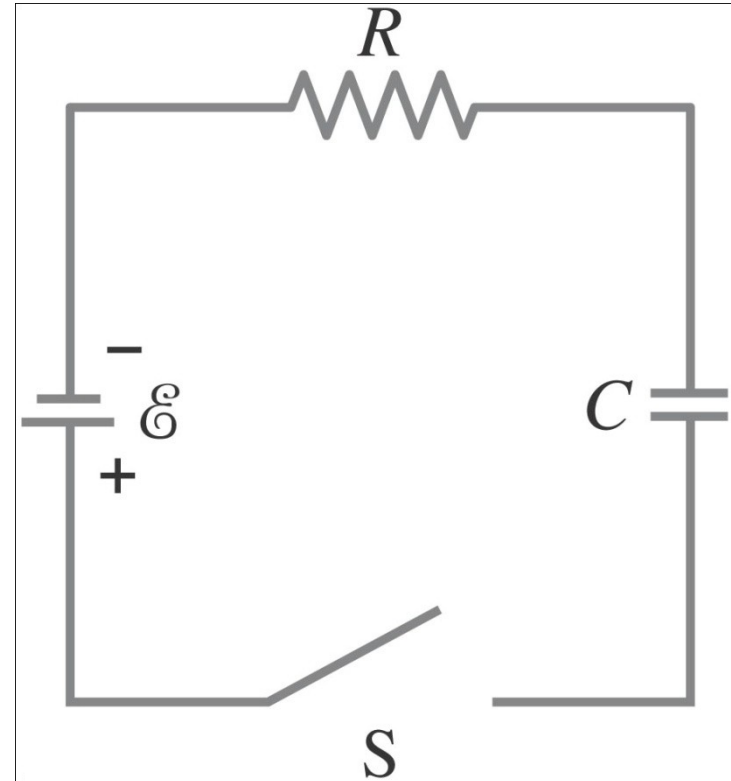
The current at any time  $t$  can be found by differentiating the charge:

$$I = \frac{dQ}{dt} = \frac{\mathcal{E}}{R} e^{-t/RC}.$$

# 26-5 Circuits Containing Resistor and Capacitor ( $RC$ Circuits)

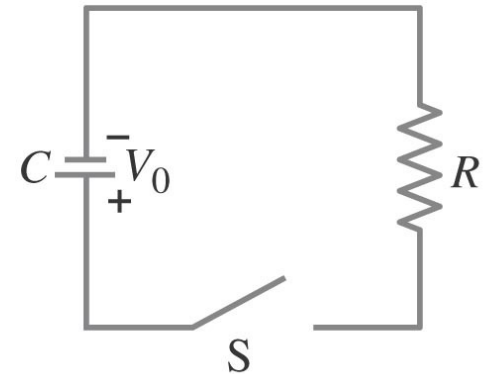
## Example 26-11: $RC$ circuit, with emf.

The capacitance in the circuit shown is  $C = 0.30 \mu\text{F}$ , the total resistance is  $20 \text{ k}\Omega$ , and the battery emf is  $12 \text{ V}$ . Determine (a) the time constant, (b) the maximum charge the capacitor could acquire, (c) the time it takes for the charge to reach 99% of this value, (d) the current  $I$  when the charge  $Q$  is half its maximum value, (e) the maximum current, and (f) the charge  $Q$  when the current  $I$  is 0.20 its maximum value.

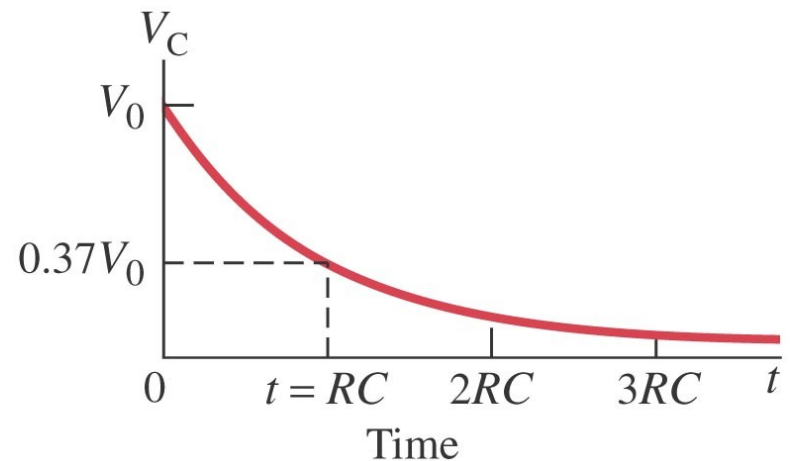


# 26-5 Circuits Containing Resistor and Capacitor ( $RC$ Circuits)

If an isolated charged capacitor is connected across a resistor, it discharges:



$$Q = Q_0 e^{-t/RC}.$$





# 20-5 Circuits Containing Resistor and Capacitor (*RC* Circuits)

Once again, the voltage and current as a function of time can be found from the charge:

$$V_C = V_0 e^{-t/RC}$$

and

$$I = -\frac{dQ}{dt} = \frac{Q_0}{RC} e^{-t/RC} = I_0 e^{-t/RC}.$$

## 26-5 Circuits Containing Resistor and Capacitor ( $RC$ Circuits)

### Example 26-12: Discharging $RC$ circuit.

In the  $RC$  circuit shown, the battery has fully charged the capacitor, so  $Q_0 = C\mathcal{E}$ . Then at  $t = 0$  the switch is thrown from position a to b. The battery emf is 20.0 V, and the capacitance  $C = 1.02 \mu\text{F}$ . The current  $I$  is observed to decrease to 0.50 of its initial value in  $40 \mu\text{s}$ . (a) What is the value of  $Q$ , the charge on the capacitor, at  $t = 0$ ? (b) What is the value of  $R$ ? (c) What is  $Q$  at  $t = 60 \mu\text{s}$ ?

