

Phys102 Lecture 10 & 11

DC Circuits

Key Points

- EMF and Terminal Voltage
- Resistors in Series and in Parallel
- Circuits Containing Resistor and Capacitor (*RC* Circuits)

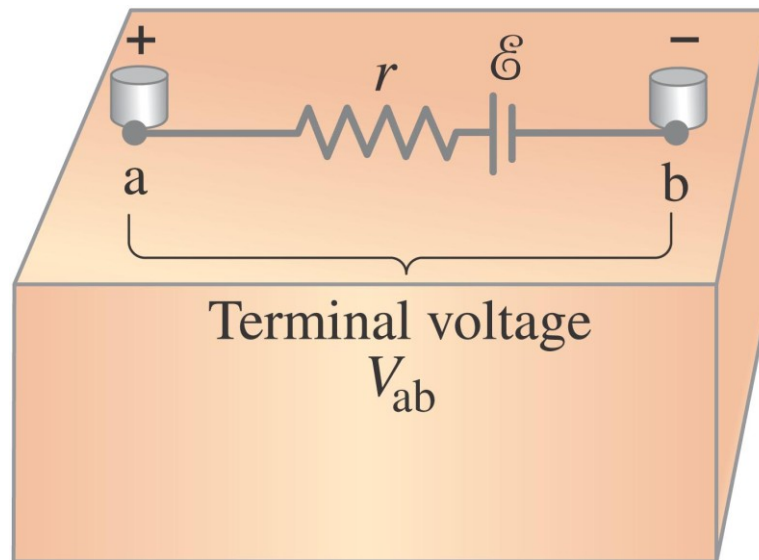
References

19-1,2,5,6.

EMF and Terminal Voltage

Electric circuit needs battery or generator to produce current – these are called sources of emf.

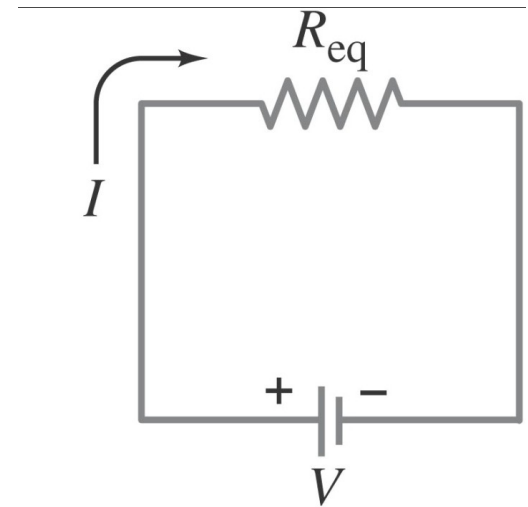
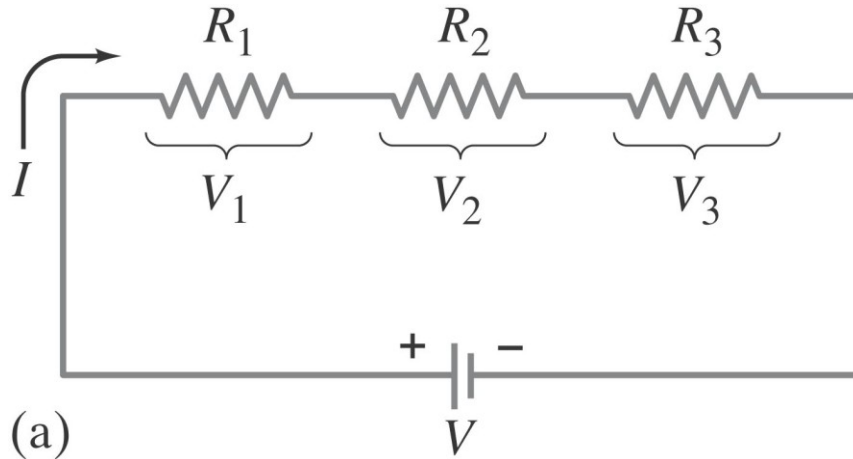
Battery is a nearly constant voltage source, but does have a small internal resistance (in series with the emf) , which reduces the actual voltage from the ideal emf:



$$V_{ab} = \mathcal{E} - Ir.$$

Resistors in Series

A series connection has a single path with the same current.



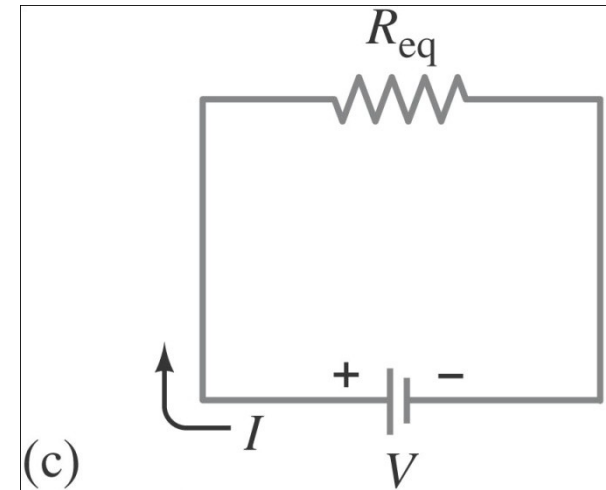
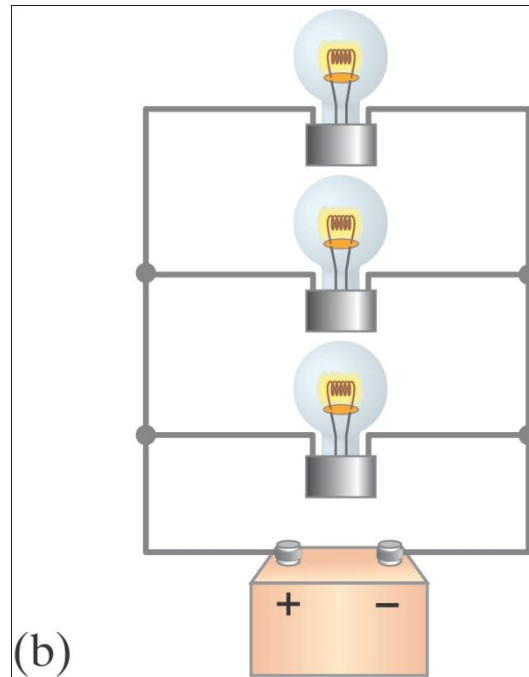
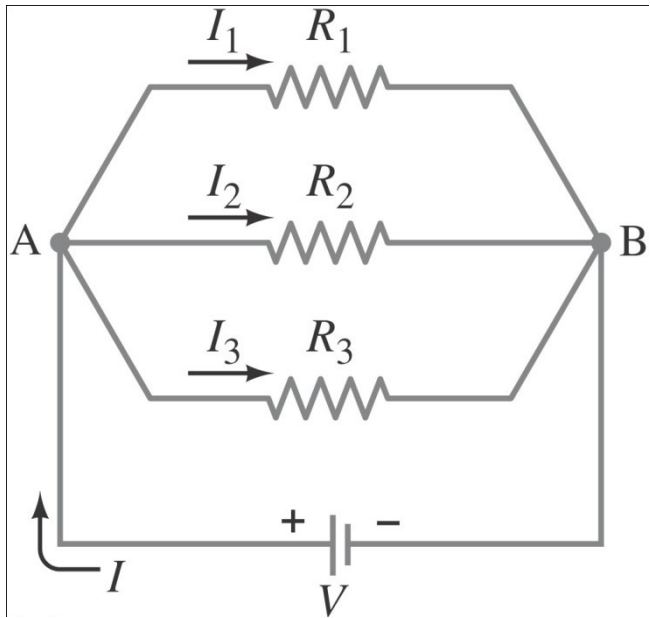
The sum of the voltage drops across the resistors equals the battery voltage

$$V = V_1 + V_2 + V_3 = IR_1 + IR_2 + IR_3. \quad [\text{series}]$$

$$R_{\text{eq}} = R_1 + R_2 + R_3. \quad [\text{series}]$$

Resistors in Parallel

A parallel connection splits the current; the voltage across each resistor is the same:



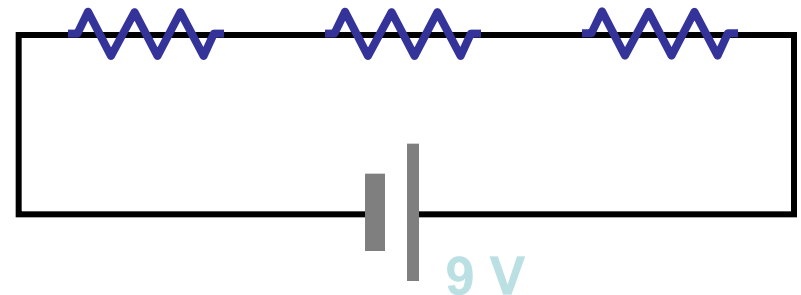
$$I = I_1 + I_2 + I_3$$
$$\frac{V}{R_{eq}} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}.$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$



Assume that the voltage of the battery is 9 V and that the three resistors are identical. What is the potential difference across each resistor?

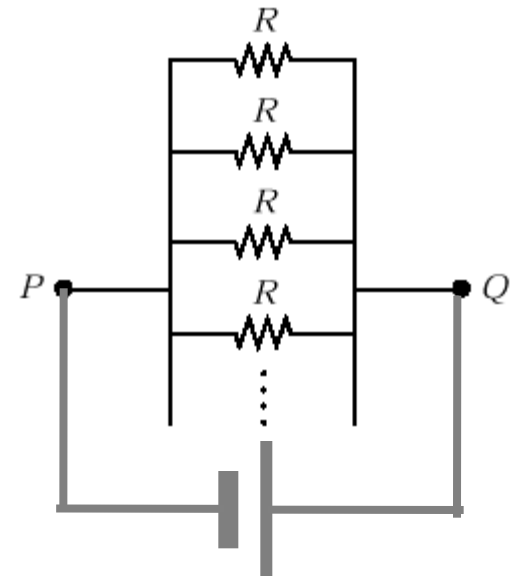
- A) 12 V
- B) zero
- C) 3 V
- D) 4 V
- E) you need to know the actual value of R





Points P and Q are connected to a battery of fixed voltage. As more resistors R are added to the parallel circuit, what happens to the total current in the circuit?

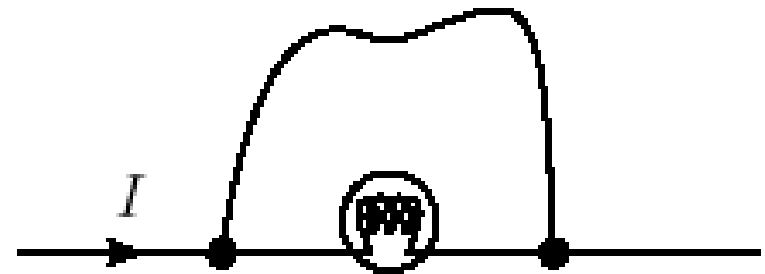
- A) increases
- B) remains the same
- C) decreases
- D) drops to zero





Current flows through a lightbulb. If a wire is now connected across the bulb, what happens?

- A) all the current continues to flow through the bulb
- B) half the current flows through the wire, the other half continues through the bulb
- C) all the current flows through the wire
- D) none of the above



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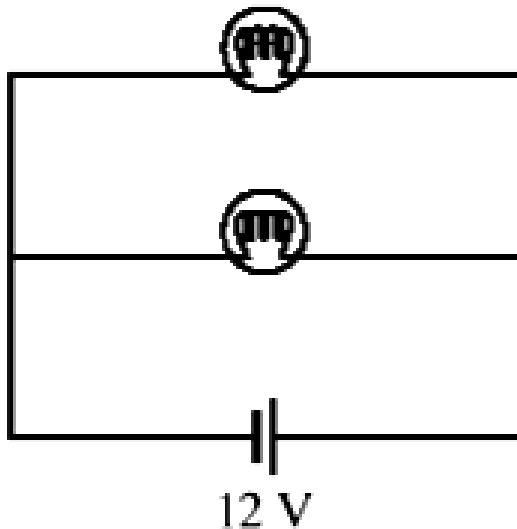
Circuits



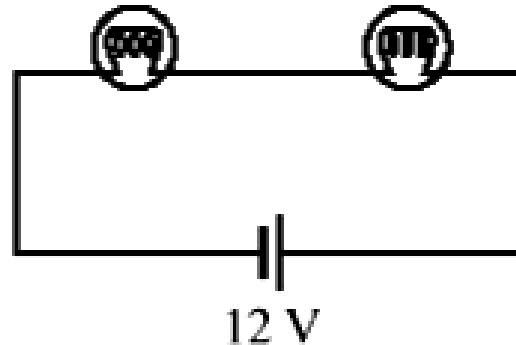
The lightbulbs in the circuits below are identical with the same resistance R . Which circuit produces more light? (brightness \iff power)

- A) circuit I
- B) circuit II
- C) both the same
- D) it depends on R

circuit I



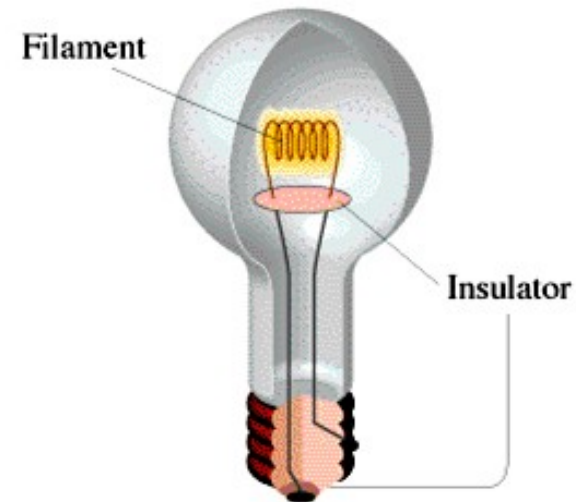
circuit II





Two lightbulbs operate at 120 V, but one has a power rating of 25 W while the other has a power rating of 100 W. Which one has the greater resistance?

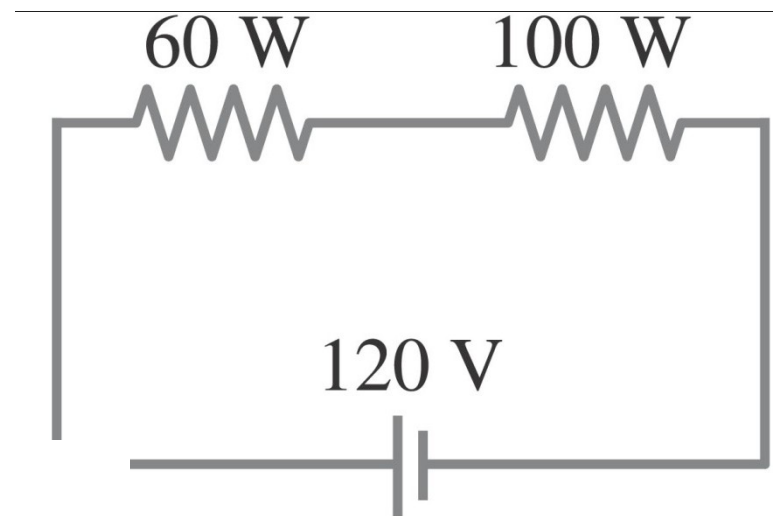
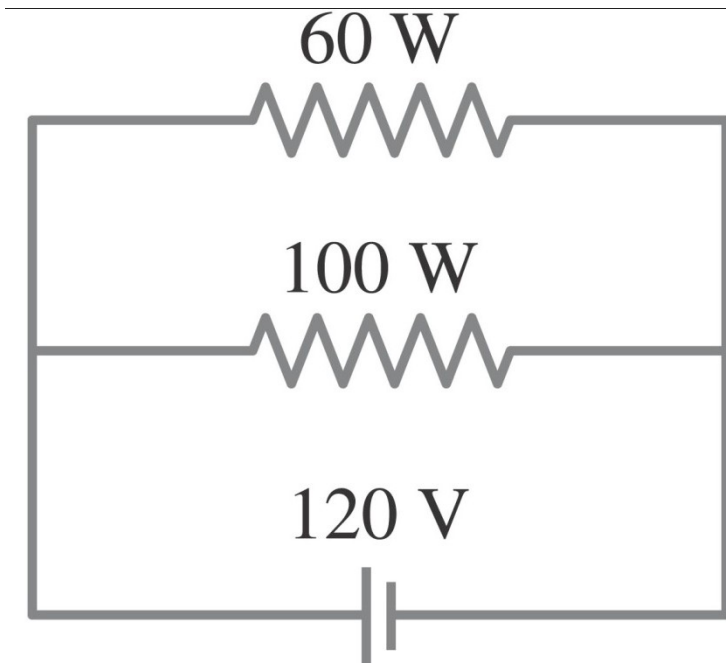
- A) the 25 W bulb
- B) the 100 W bulb
- C) both have the same
- D) this has nothing to do with resistance



Resistors in Series and in Parallel

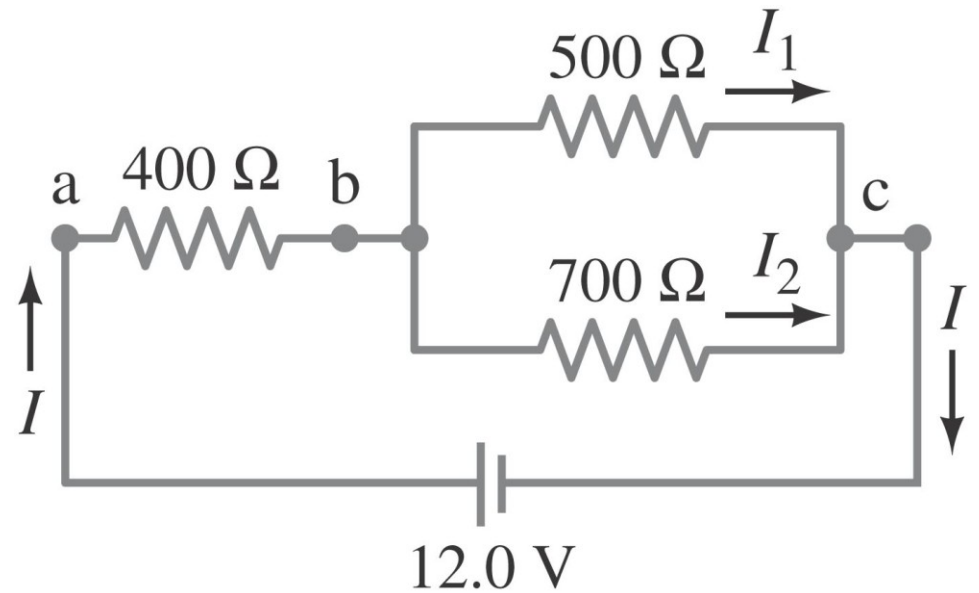
Conceptual Example: An illuminating surprise.

A 100-W, 120-V lightbulb and a 60-W, 120-V lightbulb are connected in two different ways as shown. In each case, which bulb glows more brightly? Ignore change of filament resistance with current (and temperature).



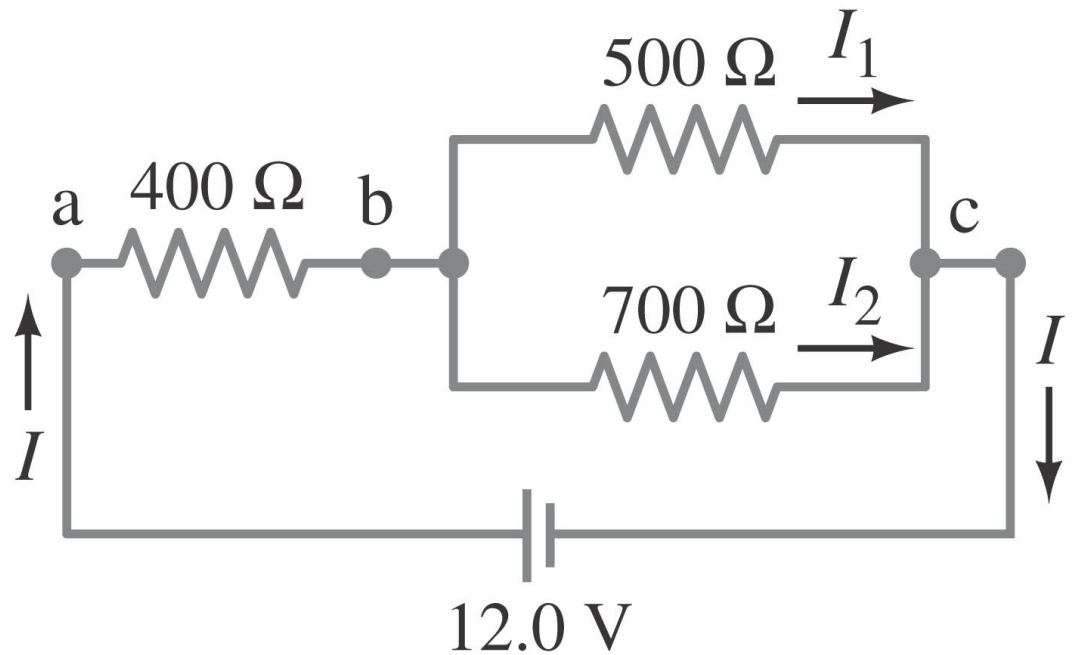
Example: Circuit with series and parallel resistors.

How much current is drawn from the battery shown?



Example: Current in one branch.

What is the current through the $500\text{-}\Omega$ resistor shown? (Note: This is the same circuit as in the previous problem.) The total current in the circuit was found to be 17 mA .

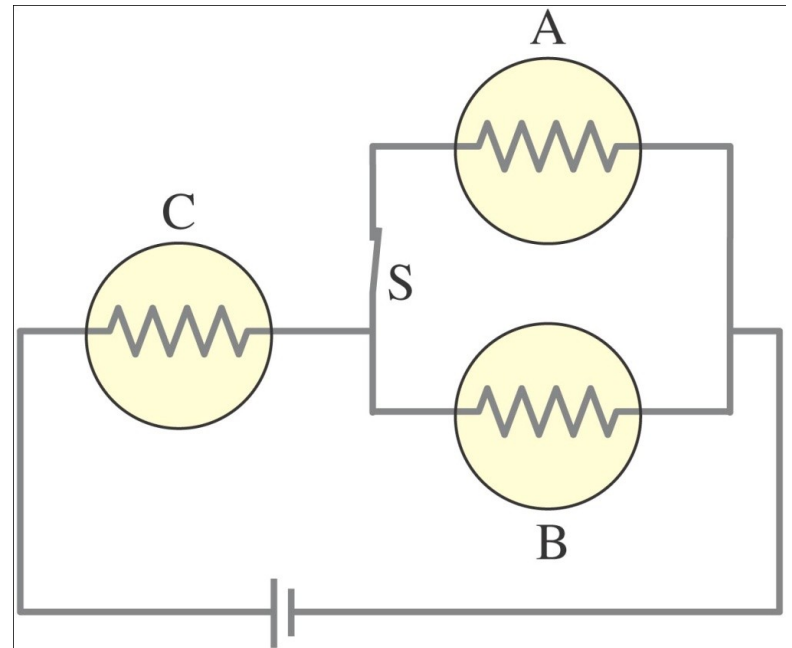


Conceptual Example: Bulb brightness in a circuit.

The circuit shown has three identical light bulbs, each of resistance R .

(a) When switch S is closed, how will the brightness of bulbs A and B compare with that of bulb C ?

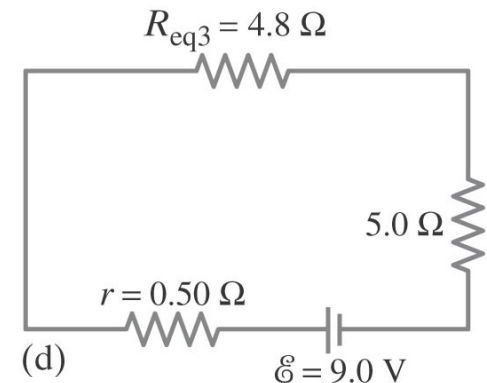
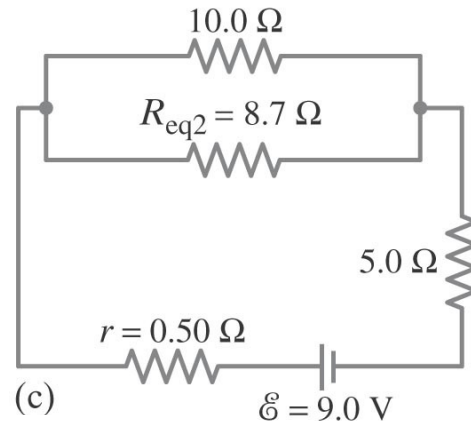
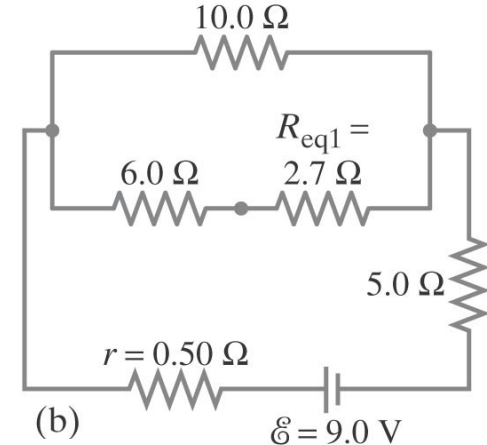
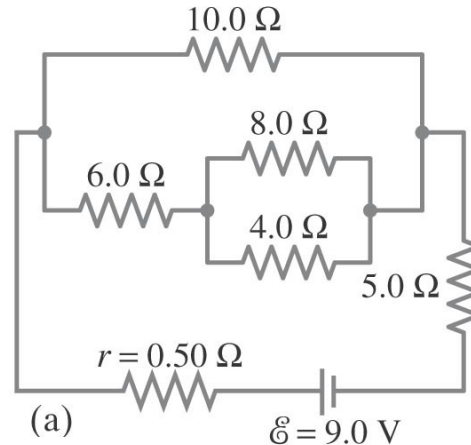
(b) What happens when switch S is opened? Use a minimum of mathematics in your answers.



Resistors in Series and in Parallel

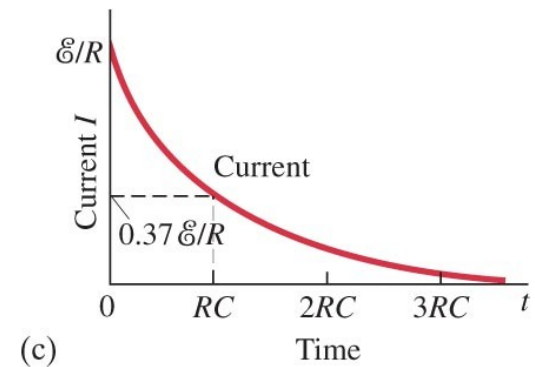
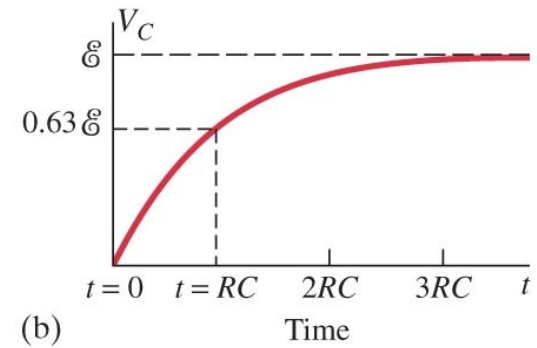
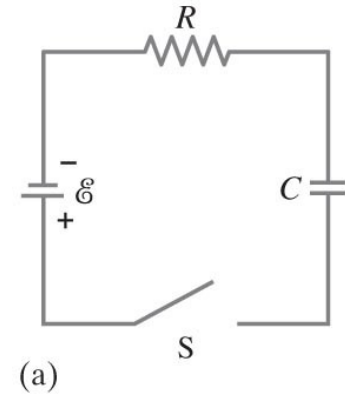
Example: Analyzing a circuit.

A 9.0-V battery whose internal resistance r is $0.50\ \Omega$ is connected in the circuit shown. (a) How much current is drawn from the battery? (b) What is the terminal voltage of the battery? (c) What is the current in the $6.0\text{-}\Omega$ resistor?



Circuits Containing Resistor and Capacitor (RC Circuits)

When the switch is closed, the capacitor will begin to charge. As it does, the voltage across it increases, and the current through the resistor decreases.



Circuits Containing Resistor and Capacitor (RC Circuits)

To find the voltage as a function of time, we write the equation for the voltage changes around the loop:

$$\mathcal{E} = IR + \frac{Q}{C}.$$

Since $Q = dI/dt$, we can integrate to find the charge as a function of time:

$$Q = C\mathcal{E}(1 - e^{-t/RC}).$$

Circuits Containing Resistor and Capacitor (RC Circuits)

The voltage across the capacitor is $V_C = Q/C$:

$$V_C = \mathcal{E}(1 - e^{-t/RC}).$$

The quantity RC that appears in the exponent is called the time constant of the circuit:

$$\tau = RC.$$

Circuits Containing Resistor and Capacitor (RC Circuits)

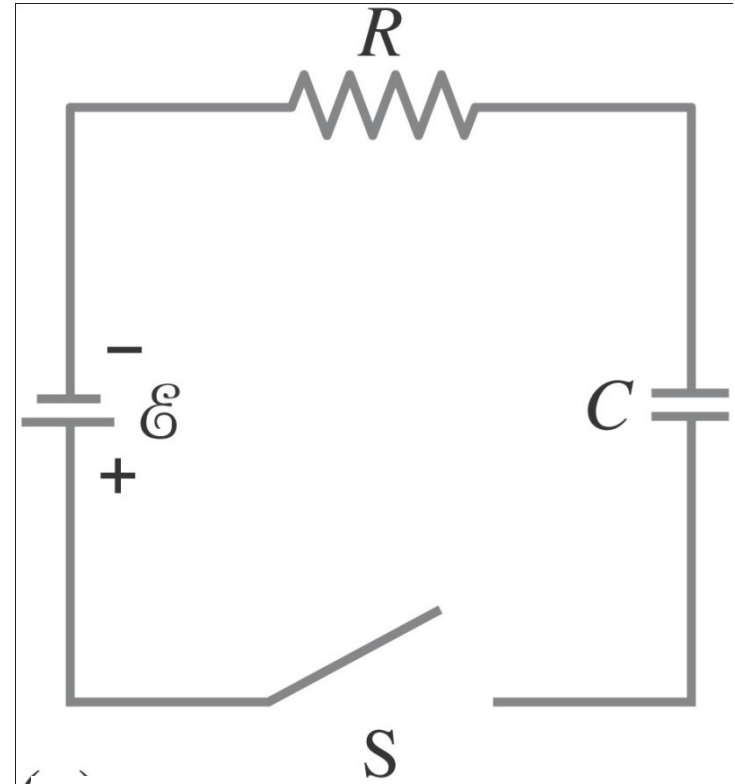
The current at any time t can be found by differentiating the charge:

$$I = \frac{dQ}{dt} = \frac{\mathcal{E}}{R} e^{-t/RC}.$$

Circuits Containing Resistor and Capacitor (RC Circuits)

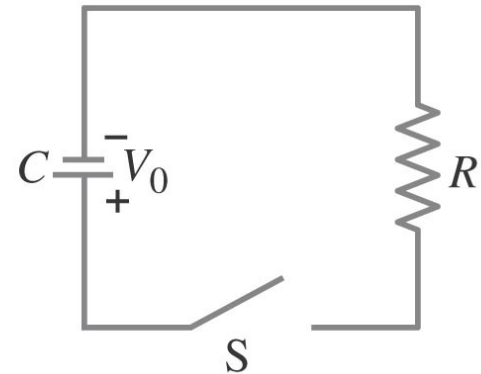
Example: RC circuit, with emf.

The capacitance in the circuit shown is $C = 0.30 \mu\text{F}$, the total resistance is $20 \text{ k}\Omega$, and the battery emf is 12 V . Determine (a) the time constant, (b) the maximum charge the capacitor could acquire, (c) the time it takes for the charge to reach 99% of this value, (d) the current I when the charge Q is half its maximum value, (e) the maximum current, and (f) the charge Q when the current I is 0.20 its maximum value.

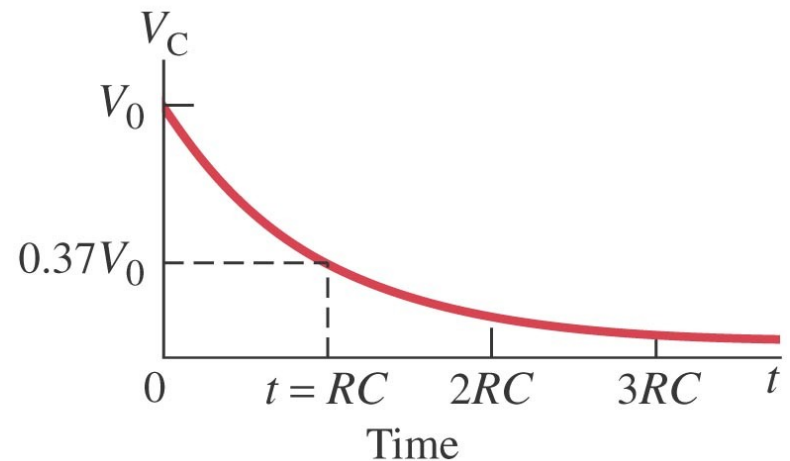


Circuits Containing Resistor and Capacitor (RC Circuits)

If an isolated charged capacitor is connected across a resistor, it discharges:



$$Q = Q_0 e^{-t/RC}.$$



Circuits Containing Resistor and Capacitor (RC Circuits)

Once again, the voltage and current as a function of time can be found from the charge:

$$V_C = V_0 e^{-t/RC}$$

and

$$I = -\frac{dQ}{dt} = \frac{Q_0}{RC} e^{-t/RC} = I_0 e^{-t/RC}.$$

Circuits Containing Resistor and Capacitor (RC Circuits)

Example: Discharging RC circuit.

In the RC circuit shown, the battery has fully charged the capacitor, so $Q_0 = C\mathcal{E}$. Then at $t = 0$ the switch is thrown from position a to b. The battery emf is 20.0 V, and the capacitance $C = 1.02 \mu\text{F}$. The current I is observed to decrease to 0.50 of its initial value in $40 \mu\text{s}$. (a) What is the value of Q , the charge on the capacitor, at $t = 0$? (b) What is the value of R ? (c) What is Q at $t = 60 \mu\text{s}$?

