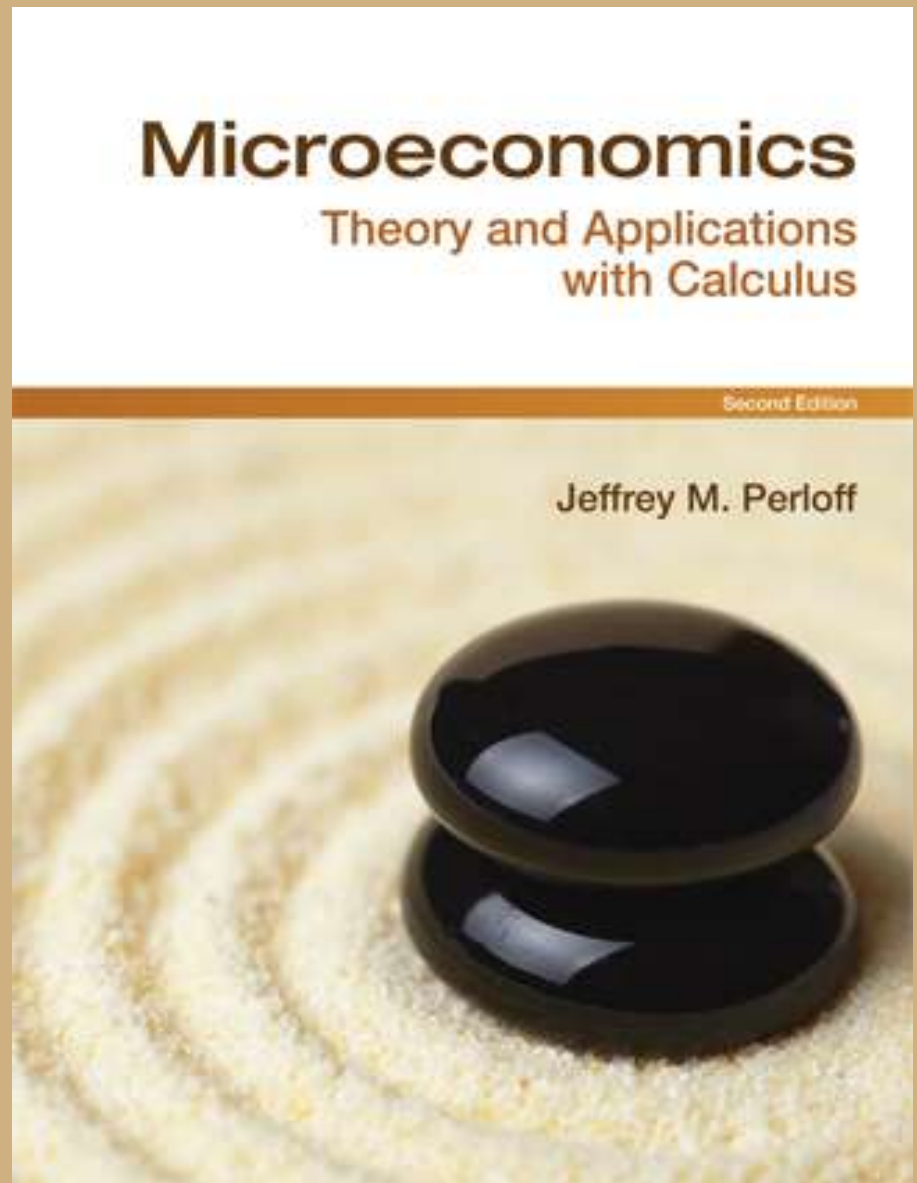


# Chapter 10

## General Equilibrium and Economic Welfare

*Capitalism is the astounding belief  
that the most wickedest of men will  
do the most wickedest of things for  
the greatest good of everyone.*

John Maynard Keynes



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# Chapter 10 Outline

10.1 General Equilibrium

10.2 General-Equilibrium Exchange Economy:  
Trading Between Two People

10.3 Competitive Exchange

10.4 Production and Trading

10.5 Efficiency and Equity

# Chapter 10 Introduction

- For a market equilibrium to be **efficient**, two conditions must be met:
  1. consumption must be efficient
    - Happens if goods cannot be reallocated among people so that at least someone is better off and no one is worse off
  2. production must be efficient
    - Happens if it is impossible to produce more output at current cost given current knowledge
- An allocation is ***Pareto efficient*** if any possible reallocation would harm at least one person.
- For a market equilibrium to be **equitable**, we need to be willing to make a value judgment about whether everyone has their fair share

# 10.1 General Equilibrium

- ***Partial-equilibrium analysis*** is an examination of equilibrium and changes in equilibrium in one market in isolation.
- By contrast, ***general-equilibrium analysis*** addresses how equilibrium is determined in all markets simultaneously.
  - This is especially important for markets that are closely related
  - Example:
    - discovery of oil deposit in a small country
    - citizens' income is raised
    - increased income affects all markets in that country simultaneously (*spillover effects*)

# 10.1 Competitive Equilibrium in Two Interrelated Markets

- Consider linear demand functions for two goods,  $Q_1$  and  $Q_2$ , as functions of their prices,  $p_1$  and  $p_2$ :

$$Q_1 = a_1 - b_1p_1 + c_1p_2 \qquad Q_2 = a_2 - b_2p_2 + c_2p_1$$

- The supply functions (with positive coefficients) are:

$$Q_1 = d_1 + e_1p_1 \qquad Q_2 = d_2 + e_2p_2$$

- What do we do with these equations?
  - Equate  $Q_d$  and  $Q_s$  in each market

# 10.1 Competitive Equilibrium in Two Interrelated Markets

- After equating  $Q_d$  and  $Q_s$ , two equations and two unknowns can be solved for the prices of both goods:

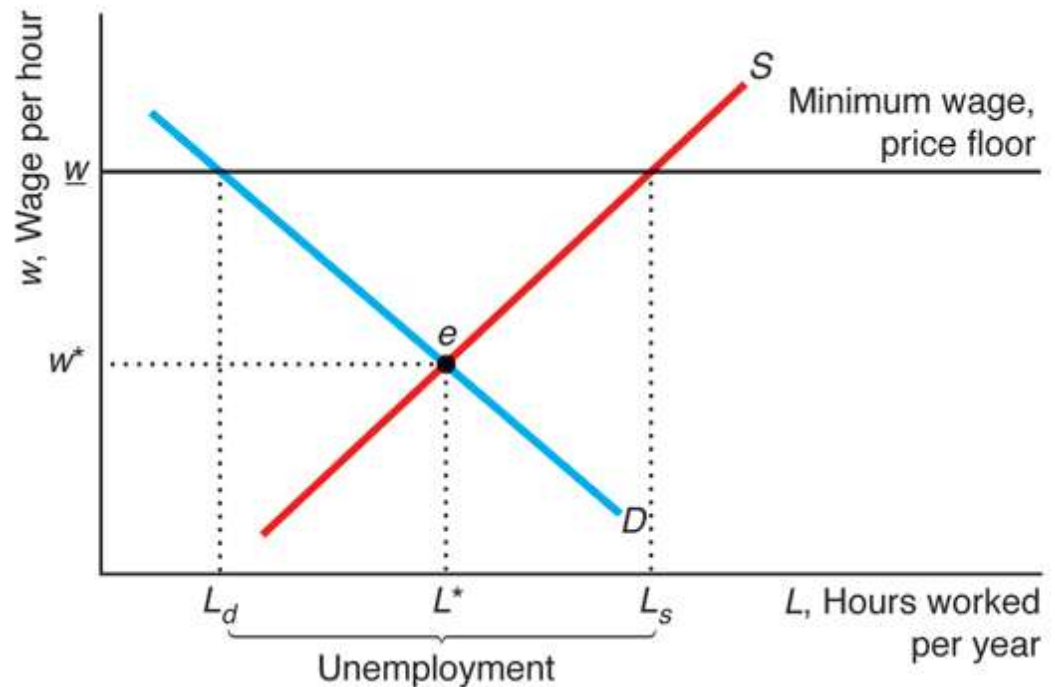
$$p_1 = \frac{(b_2 + e_2)(a_1 - d_1) + c_1(a_2 - d_2)}{(b_1 + e_1)(b_2 + e_2) - c_1c_2}$$

$$p_2 = \frac{(b_1 + e_1)(a_2 - d_2) + c_2(a_1 - d_1)}{(b_1 + e_1)(b_2 + e_2) - c_1c_2}$$

- These expressions for  $p_1$  and  $p_2$  can be substituted back into either demand or supply equations to yield a solution for  $Q_1$  and  $Q_2$ .
- Note that both prices and quantities are functions of ***all*** of the demand and supply coefficients.

# 10.1 Minimum Wages with Incomplete Coverage

- Partial-equilibrium analysis of minimum wage laws from Chapter 2 predicted unemployment:



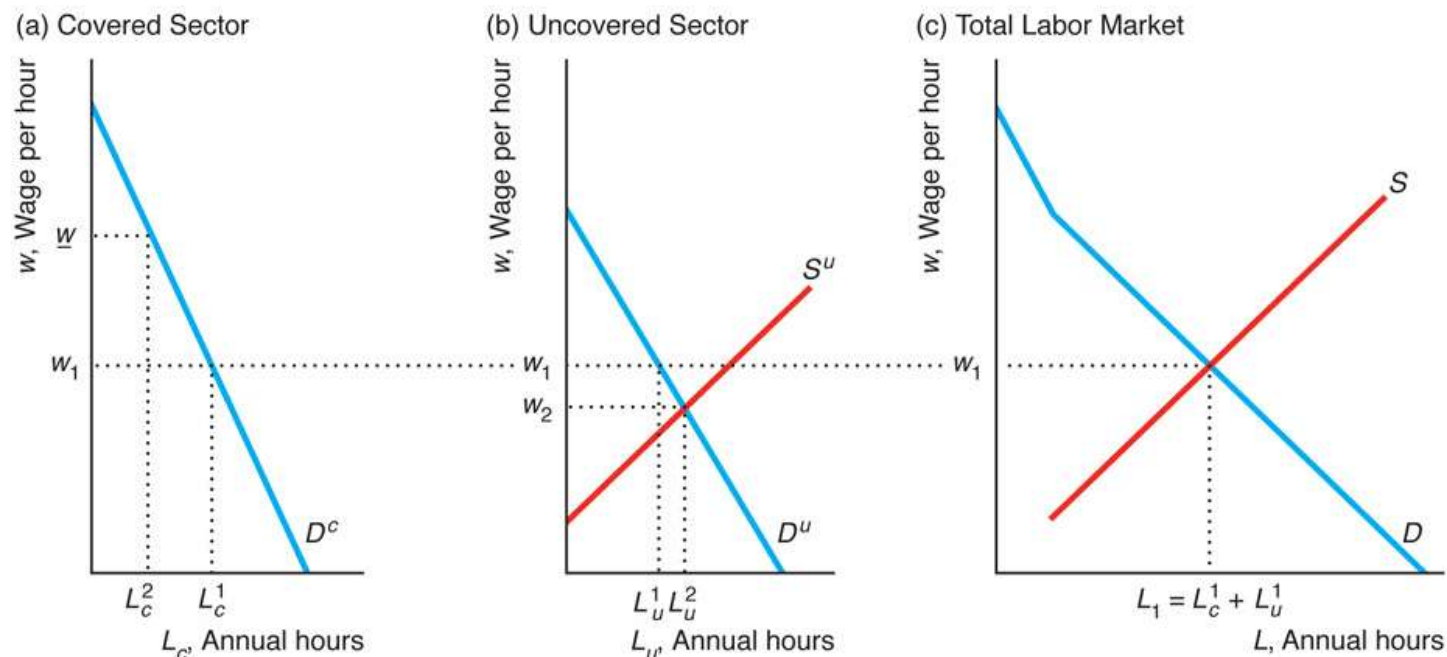
# 10.1 Minimum Wages with Incomplete Coverage

- General-equilibrium analysis of minimum wage laws that only cover workers in some sectors tells a different story.
- The increase in the wage in the covered sector causes a decrease in quantity demanded of labor in that sector.
- Displaced workers move from the covered to the uncovered sector, which drives down wages in the uncovered sector.
- Decreases in covered sector employment are (partially) offset by increases in uncovered sector employment.



# 10.1 Minimum Wages with Incomplete Coverage

- General-equilibrium analysis of minimum wage laws indicates that unemployment need not be created:



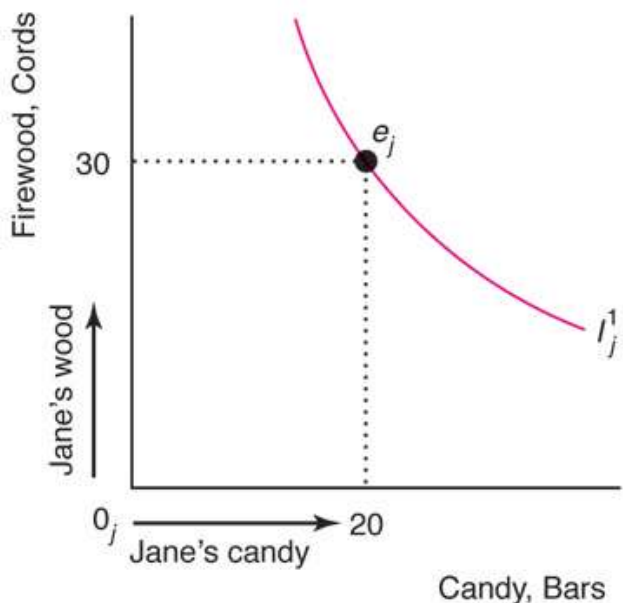
## 10.2 General-Equilibrium Exchange Economy: Trading Between Two People

- General-equilibrium model can be used to show that free trade is ***Pareto efficient***.
  - After all voluntary trades have occurred, we cannot reallocate goods so as to make one person better off without harming another.
- Consider example of neighbors, Jane and Denise, who each have an initial endowment of firewood and candy
  - Jane: 30 cords of firewood and 20 candy bars
  - Denise: 20 cords of firewood and 60 candy bars
- These endowments can be shown graphically using indifference curves.

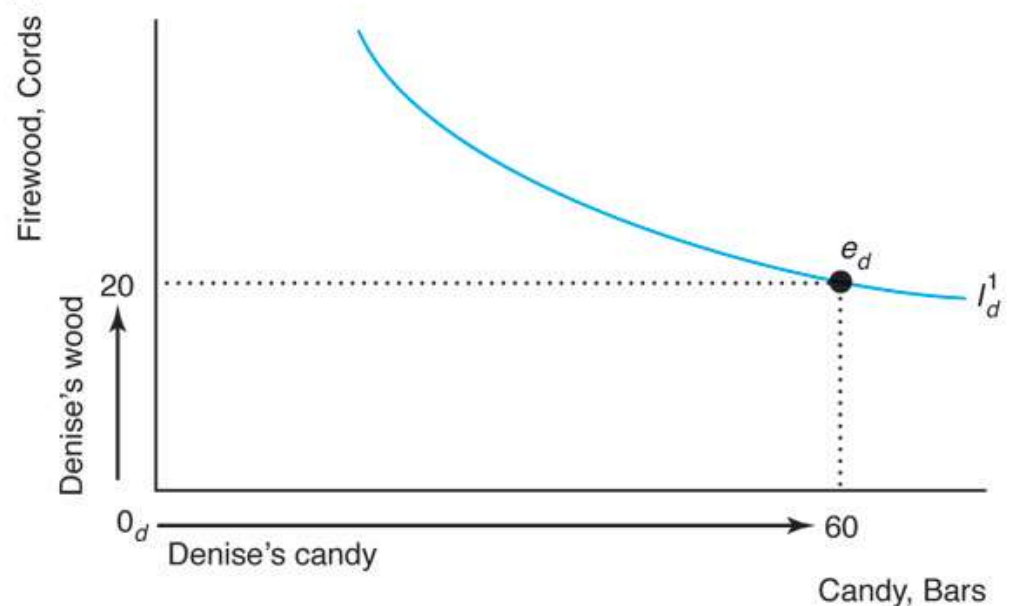
# 10.2 Trading Between Two People

- Jane and Denise before they engage in trade

(a) Jane's Endowment



(b) Denise's Endowment

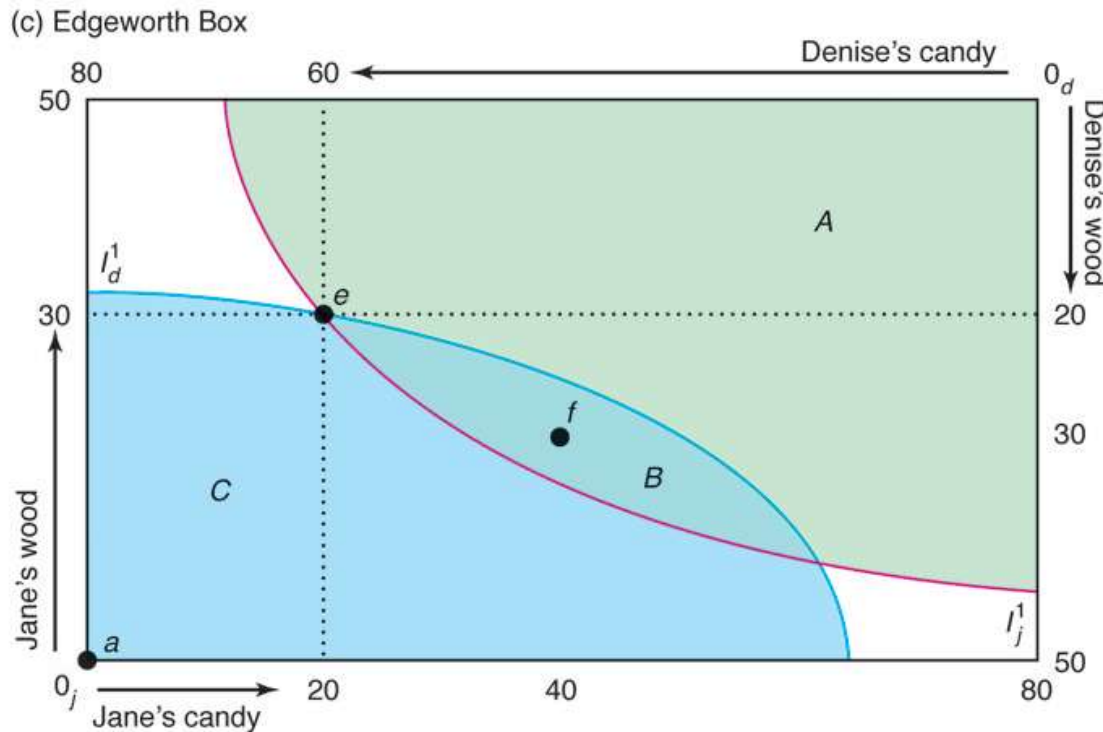


## 10.2 Trading Between Two People

- If Jane and Denise do not trade, they can each only consume their initial endowments.
- In order to see whether Jane and Denise would benefit from trading firewood and candy bars, we use an Edgeworth box.
  - An **Edgeworth box** illustrates trade between two people with fixed endowments of two goods.
  - An Edgeworth box is useful in general equilibrium models because both the firewood and candy bar markets are being affected simultaneously.

# 10.2 Trading Between Two People

- Initial endowments place Jane and Denise at point  $e$ , but area  $B$  holds more preferred bundles for both.

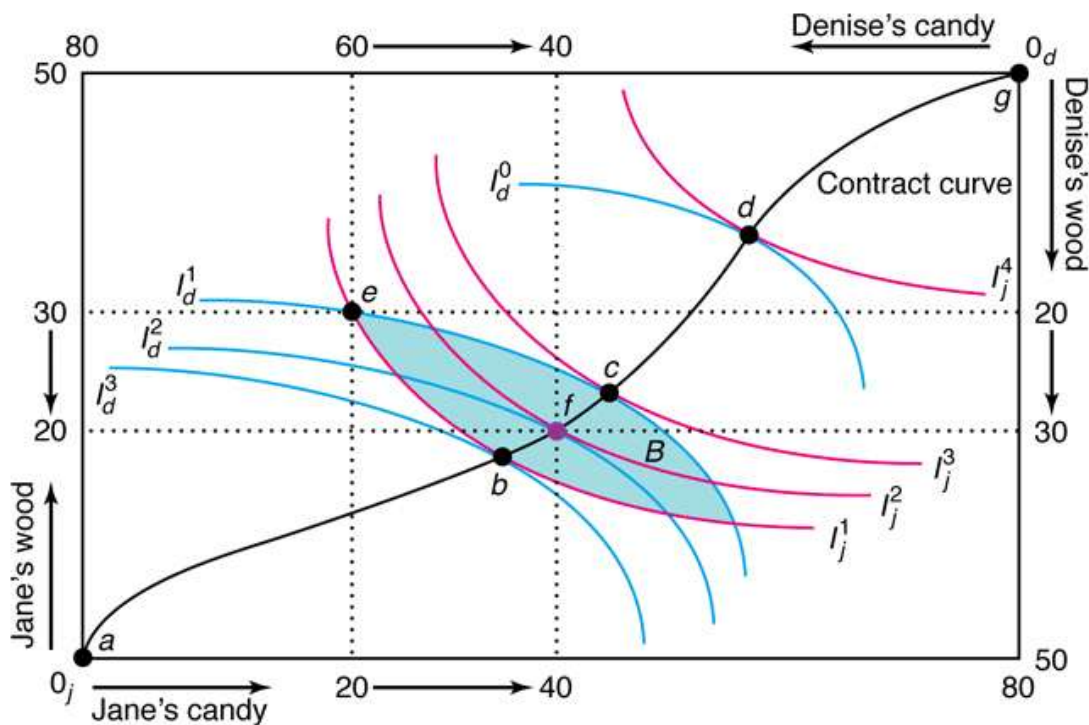


## 10.2 Trading Between Two People

- Should Jane and Denise trade? Yes.
- We make four assumptions about their tastes and behavior in order to answer this question:
  - 1.Utility maximization:** Each person maximizes her utility.
  - 2.Usual-shaped indifference curves:** Each person's indifference curves have the usual convex shape.
  - 3.Nonsatiation:** Each person has strictly positive marginal utility for each good (e.g. each wants as much of each good as possible).
  - 4.No interdependence:** Neither person's utility depends on the other's consumption and neither person's consumption harms the other person

# 10.2 Trading Between Two People

- No further trade is possible at a bundle like  $f$  because Jane's MRS is equal to Denise's MRS at point  $f$ .



## 10.2 Trading Between Two People

- The ***contract curve*** is the set of all Pareto-efficient bundles.
  - Name refers to the fact that Jane and Denise are unwilling to engage in further trades, or contracts, only at points along the contract curve.
  - These allocations are the final contracts.
- The contract curve is derived by maximizing Jane's utility subject to leaving Denise's utility unchanged (or vice versa).
  - Calculus can be used to show that this maximization problem boils down to points where their indifference curves have the same slopes:  $MRS_j = MRS_d$ .



# 10.3 Competitive Exchange

- Without knowledge of the trading process, we only know that Jane and Denise trade to some allocation on the contract curve.
- With knowledge of the exact trading process, we can determine their final allocation.
- General-equilibrium models can show that a competitive market has two desirable properties:
  1. Competitive equilibrium is efficient
    - *First Theorem of Welfare Economics*
  2. Any efficient allocations can be achieved by competition
    - *Second Theorem of Welfare Economics*

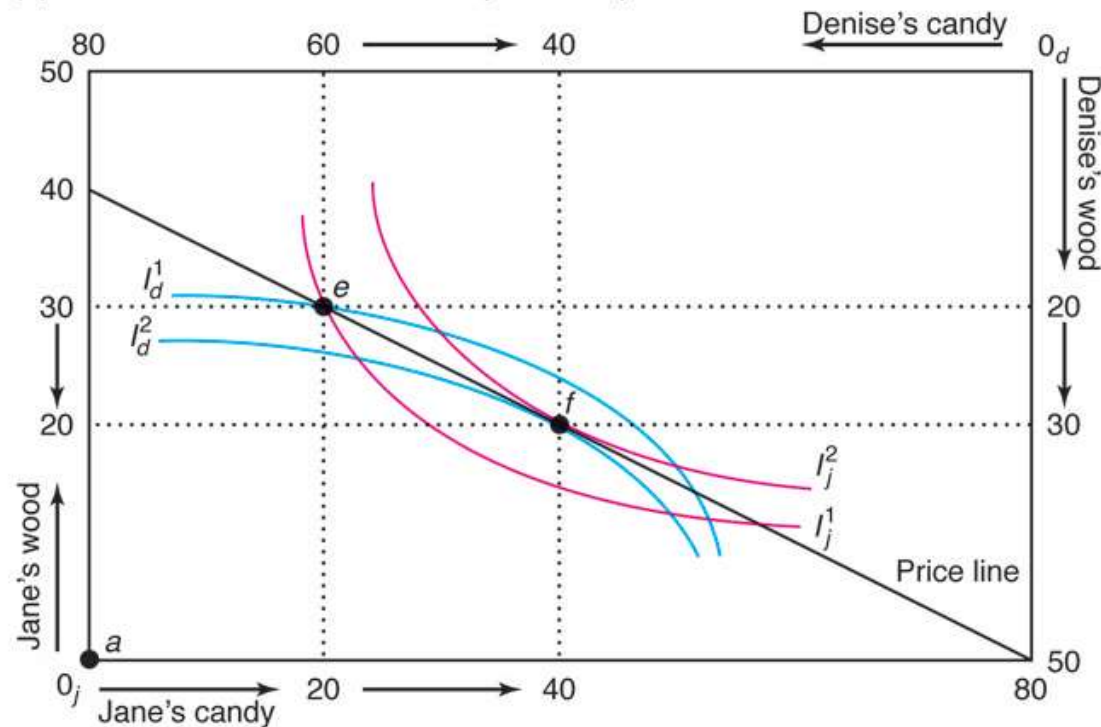
## 10.3 Competitive Exchange

- Given prices of the two goods, a price line can be added to the Edgeworth box.
  - The price line is all the combinations of goods that Jane could get by trading, given her endowment.
- If the price of firewood is \$2 and the price of a candy bar is \$1, then the price line indicates that Jane would choose to trade wood for candy and move from point *e* to *f*.
- Similarly, given those prices, Denise would prefer to trade candy for wood and move from point *e* to *f*.

# 10.3 Competitive Exchange

- Both Jane and Denise enjoy higher utility when they can afford to move to point  $f$ .

(a) Price Line That Leads to a Competitive Equilibrium



# 10.3 The Efficiency of Competition

- In a competitive equilibrium, the indifference curves of both types of consumers are tangent at the same bundle on the price line, thus:

$$MRS_j = -\frac{p_c}{p_w} = MRS_d$$

- If the competitive equilibrium must lie on the contract curve, we have demonstrated the *First Theorem of Welfare Economics*
  - Any competitive equilibrium is Pareto efficient
- By adjusting initial endowments so they lie along the price line, we demonstrate the *Second Theorem of Welfare Economics*
  - Any Pareto-efficient equilibrium can be obtained by competition given an appropriate endowment

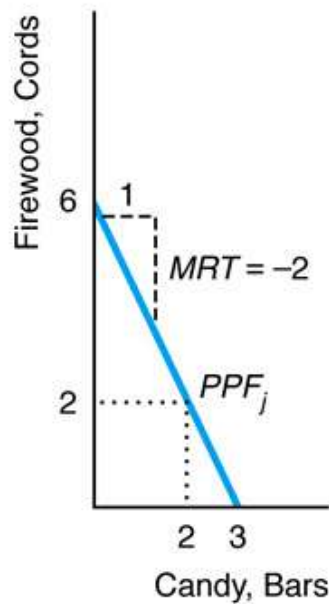
# 10.4 Production and Trading

- So far our discussion of trade has been entirely about consumption, but what about production?
- Production capabilities can be summarized with a ***production possibility frontier*** (PPF).
  - PPF shows the maximum combination of two outputs that can be produced from a given amount of input.
- In our example, assume:
  - Jane can use her labor to produce up to 3 candy bars or 6 cords of firewood in a day
  - Denise can use her labor to produce up to 6 candy bars or 3 cords of firewood in a day

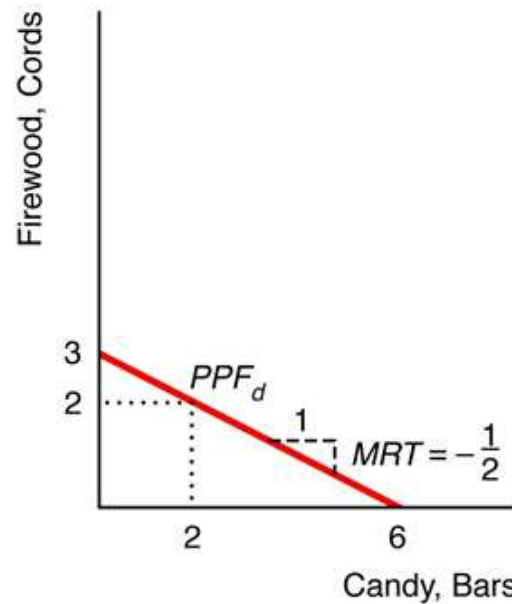
# 10.4 Production and Trading

- PPF curves can be combined to show joint productive capacity.

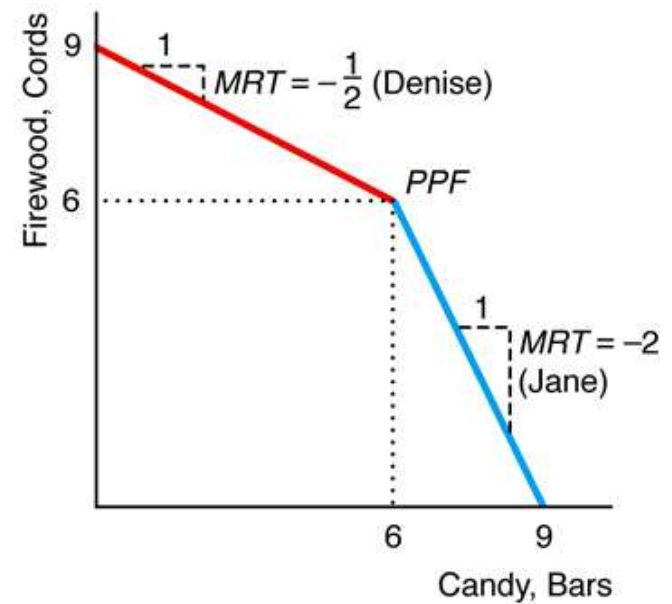
(a) Jane



(b) Denise



(c) Joint Production



# 10.4 Production and Trading

- The slope of the production possibility frontier is the ***marginal rate of transformation*** (MRT).
  - MRT tells us how much more wood can be produced if the production of candy is reduced by one bar.
  - More generally, MRT shows how much it costs to produce one good in terms of the forgone production of the other good.
- The ***comparative advantage*** in producing a good goes to the person who can produce the good at a lower opportunity cost.
  - Jane has comparative advantage in producing wood
  - Denise has comparative advantage in produce candy

# 10.4 Benefits of Trade

- Differences in MRTs imply that Jane and Denise can benefit from trade.
- Assume both like to consume wood and candy in equal proportions.
  - Without trade, each produces 2 candy bars and 2 cords of wood each day
  - With trade:
    - Denise specializes in candy production and makes 6 candy bars
    - Jane specializes in firewood production and makes 6 cords of wood
    - If production is split equally, each gets 3 candy bars and 3 cords of wood each day!
- Trade works when comparative advantage is followed.



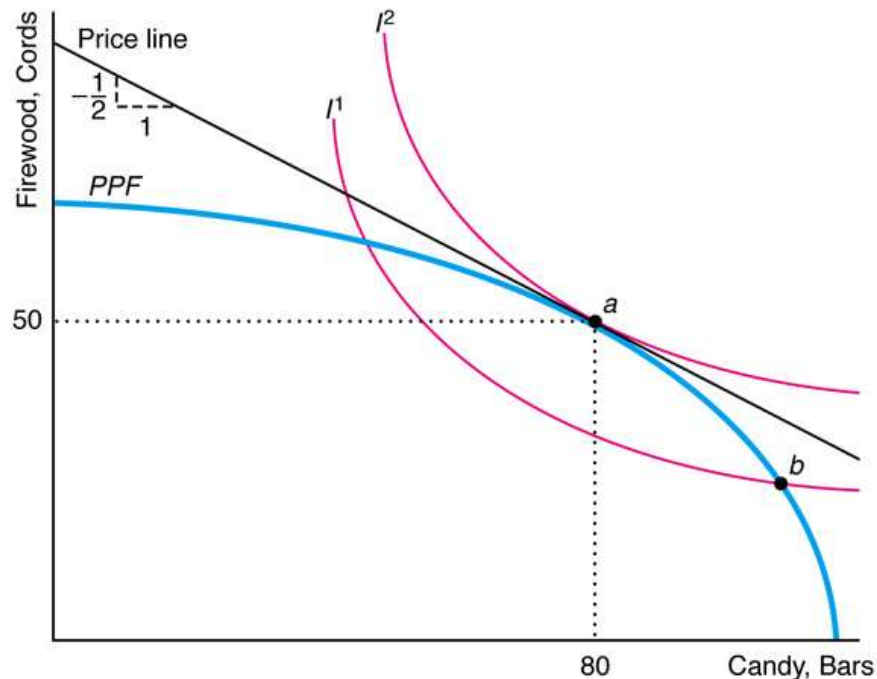
# 10.4 The Number of Producers

- With just two producers – Jane and Denise – the PPF has one kink.
- As other methods of production with different MRTs are added, the PPF gets more kinks.
- As the number of different producers gets very large, the PPF becomes a smooth curve that is concave to the origin.
- The MRT along this smooth PPF tells us about the marginal cost of producing one good relative to the other.

$$MRS_j = -\frac{p_c}{p_w} = MRS_d$$

# 10.4 Optimal Product Mix

- Individual's utility is maximized at point *a*, the point where the PPF touches the indifference curve (MRS = MRT).



# 10.4 Competition

- Each price-taking consumer picks a bundle of goods such that:

$$MRS = -\frac{p_c}{p_w}$$

- If all relative prices are the same for all individuals in competitive equilibrium, all will have equal MRSs and no further trades can occur.
- The competitive equilibrium achieves **consumption efficiency**
  - Impossible to redistribute goods to make one person better off without making someone worse off.

# 10.4 Competition

- Each competitive firm sells a quantity of candy ( $c$ ) and wood ( $w$ ) such that price equals marginal cost:

$$p_c = MC_c \qquad p_w = MC_w$$

- Taking the ratio of these and combining with the fact that MRT is the ratio of marginal costs yields:

$$MRT = -\frac{p_c}{p_w}$$

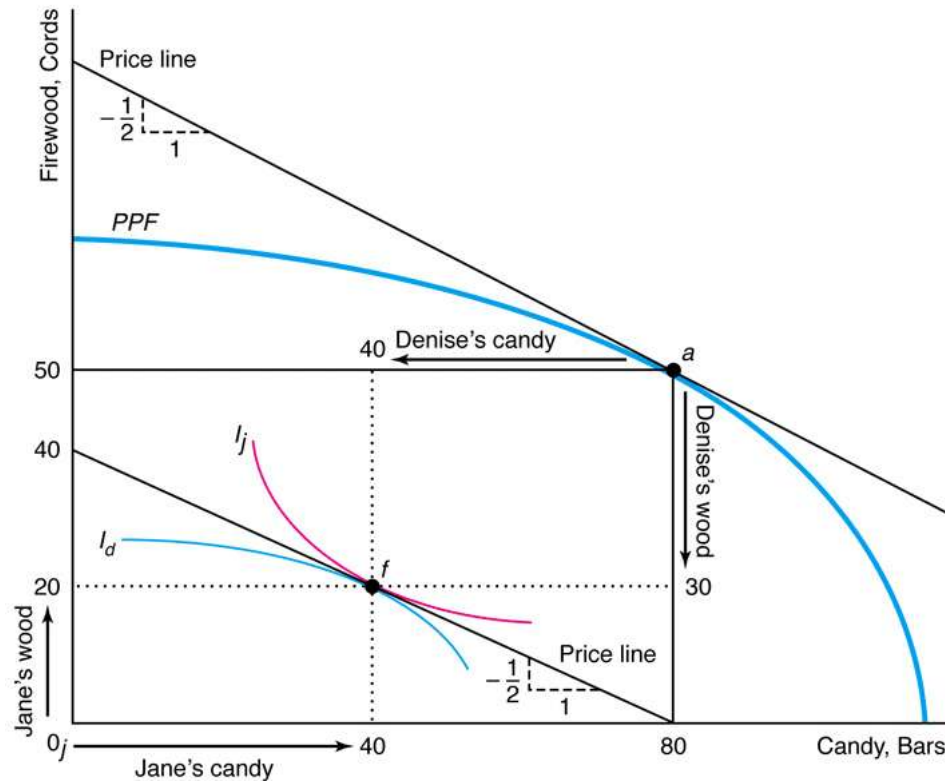
- Thus, competition insures an efficient product mix:

$$MRS = -\frac{p_c}{p_w} = MRT$$

- The rate at which firms can transform one good into another equals the rate at which consumers are willing to substitute between goods.

# 10.4 Competitive Equilibrium

- At the competitive equilibrium, the relative prices that firms and consumers face are the same.



# 10.5 Efficiency and Equity

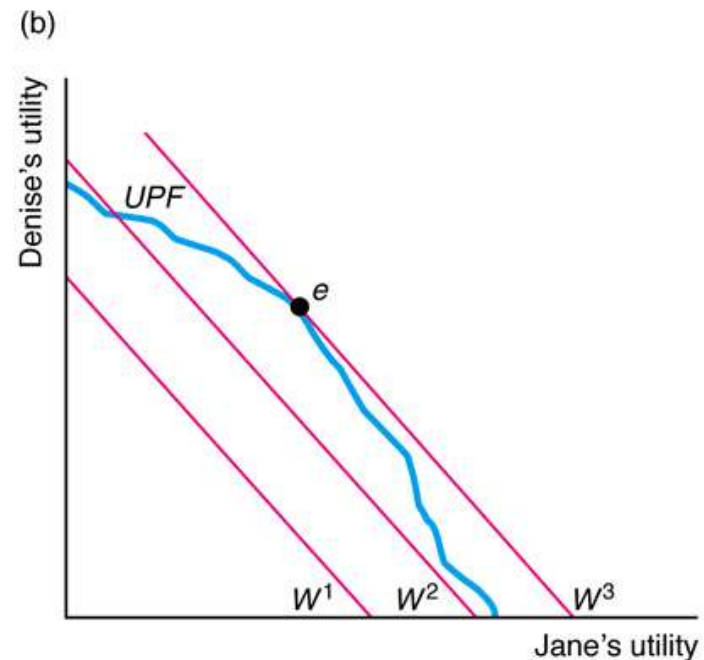
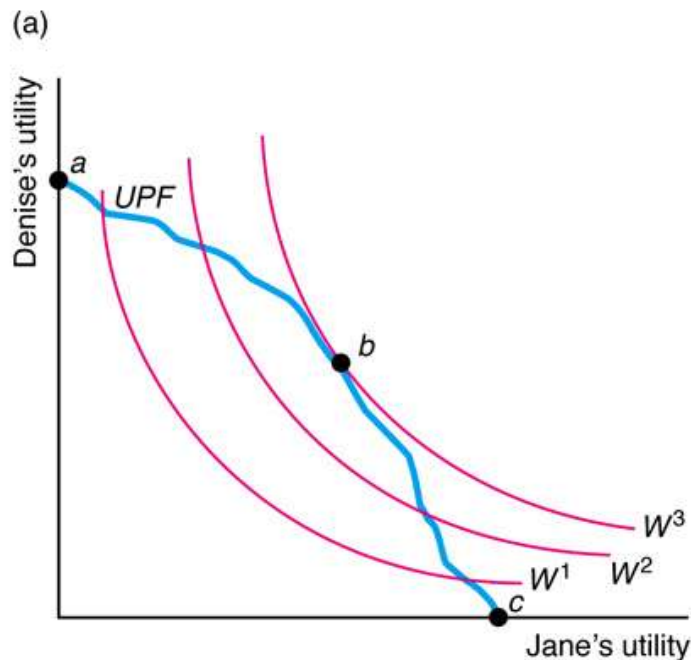
- How well various people in a society live depends on:
  - Efficiency (size of the pie)
  - Equity (how the pie is divided)
- Role of the government
  - Wealth is redistributed with every government action
  - Agricultural price support programs transfer wealth to farmers
  - Income taxes transfer income from better-off to poor
  - Proceeds from the lottery (played by mostly lower-income people) funds merit-based college scholarships in many states

# 10.5 Efficiency and Equity

- A ***social welfare function*** combines various consumers' utilities to provide a collective ranking for allocations.
  - Graphically summarized by a ***isowelfare curve***, along which social welfare is constant.
- A ***utility possibility frontier*** (UPF) is the set of utility levels corresponding to Pareto-efficient allocations along the contract curve.
- Society maximizes welfare by choosing the allocation for which the highest possible isowelfare curve touches the UPF.

# 10.5 Efficiency and Equity

- Society maximizes welfare by choosing the allocation for which the highest possible isowelfare curve touches the UPF.





# 10.5 Efficiency and Equity

- Many rules by which society might decide among various allocations have been suggested.
- These different social welfare functions yield different distributions of goods:

**1. Utilitarian:** equal weight to all people in society  
(  $W = U_1 + U_2 + \dots + U_n$  )

**2. Generalized utilitarian:** different weights assigned, perhaps to adults, hard workers, etc.  
(  $W = \alpha_1 U_1 + \alpha_2 U_2 + \dots + \alpha_n U_n$  )

**3. Rawlsian:** maximizes well-being of worst off individual (  $W = \min (U_1, U_2, \dots, U_n)$  )

# 10.5 Efficiency versus Equity

- Given a particular welfare function, society might prefer an inefficient allocation to an efficient one.
  - Example: one person has everything, which means any reallocation would make that one person worse off, but would likely be preferred by everyone else.
- Sometimes, in an attempt to achieve greater equity, efficiency is reduced.
  - Example: advocates for the poor prefer providing them with public housing (equity), but this is inefficient because the poor would be better off with a cash transfer of equal value.

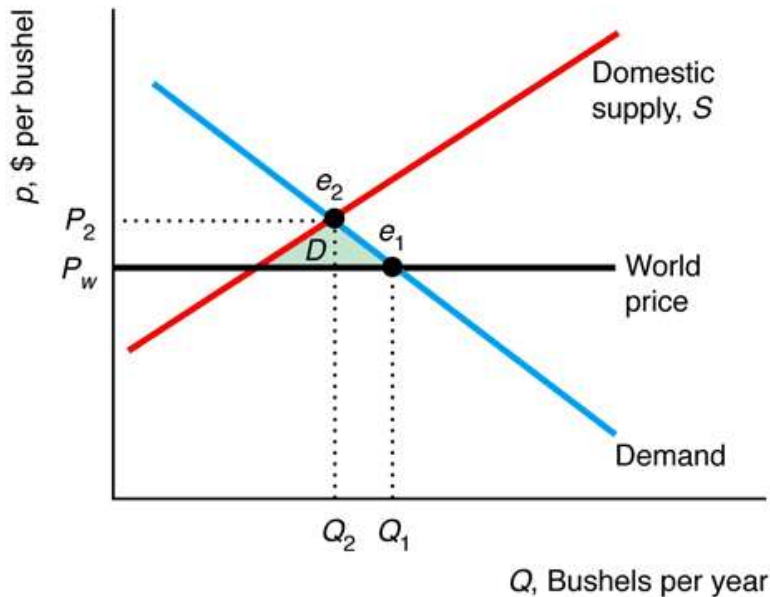
# 10.5 Efficiency versus Equity

- If competition maximizes efficiency and our usual welfare measure, shouldn't we strive to eliminate any distortion (tariff, quota, tax, etc.)?
- An economy with no distortions is a ***first-best equilibrium***
  - Any distortion will reduce efficiency
- Eliminating some distortions does not guarantee the same outcome as eliminating all of them.
- The ***Theory of the Second Best*** says that if an economy has at least two market distortions, eliminating just one may either increase or decrease welfare!

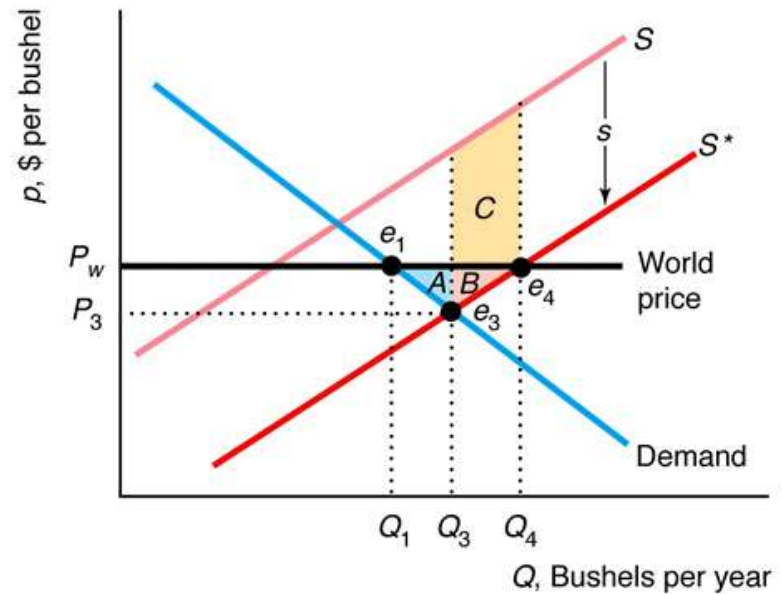
# 10.5 Efficiency and Equity

- Permitting trade may raise welfare (as in panel (a)) or may lower it (as in panel (b)) depending on existing distortions.

(a) No Distortions



(b) Subsidy



# Figure 10.4 Competitive Equilibrium

(b) Prices That Do Not Lead to a Competitive Equilibrium

