## Chapter 12

## Pricing and Advertising

Everything is worth what its purchaser will pay for it.

Publilius Syrus (first century BC)

## Chapter 12 Outline

12.1 Why and How Firms Price Discriminate
12.2 Perfect Price Discrimination
12.3 Quantity Discrimination
12.4 Multimarket Price Discrimination
12.5 Two-Part Tariffs
12.6 Tie-In Sales
12.7 Advertising

### 12.1 Why and How Firms Price Discriminate

- Why does Disneyworld charge local residents \$369 for an annual pass and out-of-towners \$489?
- Why are airline fares less if you book in advance?
- Why are computers and software bundled and sold at a single price?
- Firms sometimes use nonuniform pricing, where prices vary across customers, to earn a higher profit.


### 12.1 Why and How Firms Price Discriminate

- A firm engages in price discrimination by charging consumers different prices for the same good based on
- individual characteristics
- belonging to an indentifiable sub-group of consumers
- the quantity purchased
- Two reasons why a firm earns a higher profit from price discrimination than uniform pricing:

1. Price-discriminating firms charge higher prices to customers who are willing to pay more than the uniform price.
2. Price-discriminating firms sell to some people who are not willing to pay as much as the uniform price.

### 12.1 Why and How Firms Price Discriminate

- Necessary conditions for successful price discrimination:

1. A firm must have market power (otherwise it can't charge a price above the competitive price).

- Examples: monopoly, oligopoly, monopolistically competitive, cartel

2. A firm must be able to identify which consumers are willing to pay relatively more and there must be variation in consumers' reservation price, the maximum amount someone is willing to pay.
3. A firm must be able to prevent or limit resale from customers who are charged a relatively low price to those who are charged a relatively high price.

### 12.1 Why and How Firms Price Discriminate

- A firm's inability to prevent resale is often the biggest obstacle to successful price discrimination.
- Resale is difficult or impossible for services and when transaction costs are high.
- Examples: haircuts, plumbing services, admission that requires showing an ID
- Not all differential pricing is price discrimination.
- It is not price discrimination if the different prices simply reflect differences in costs.
- Example: selling magazines at a newsstand for a higher price than via direct mailing


### 12.1 Types of Price Discrimination

1. First-degree

- Also known as perfect price discrimination
- Each unit sold for each customer's reservation price

2. Second-degree

- Also known as quantity discrimination
- Firm charges a different price for large quantities than for small quantities

3. Third-degree

- Also known as multimarket price discrimination
- Firm charges different groups of customers different prices, but charges any one customer the same price for all units sold


### 12.2 Perfect Price Discrimination

- Under perfect price discrimination, the firm charges each consumer a price that is exactly equal to the maximum he/she is willing to pay.
- Examples: college financial aid, auto dealerships, clairvoyants
- Thus, each consumer gets zero consumer surplus.
- Firm profit is increased by the amount of consumer surplus that would exist in a competitive market; all CS is transferred to the firm.


### 12.2 Perfect Price Discrimination

- All consumer surplus is transformed into firm profit.



### 12.2 Perfect Price Discrimination

- If $D(Q)$ is the inverse demand function for total output, $Q$, and $p=D(Q)$ is the reservation price charged of each customer, the discriminating monopoly's revenue is:

$$
R=\int_{0}^{Q} D(z) \mathrm{d} z
$$

- This is equal to the area under the demand curve up to $Q$.
- Maximizing profit by choosing output: $\max _{Q} \pi=\int_{0}^{Q} D(z) \mathrm{d} z-C(Q)$
- $F O C: \frac{\mathrm{d} \pi}{\mathrm{d} Q}=D(Q)-\frac{\mathrm{d} C(Q)}{\mathrm{d} Q}=0$
- Result: produce where $D(Q)$ equals MC.


### 12.2 Perfect Price Discrimination

- Producing where Demand = MC, all consumer surplus $(A+B+C)$ is transformed into firm profit.


Monopoly
Perfect Price Discrimination

|  | Competition | Single Price | Discrimination |
| :--- | :---: | :---: | :---: |
| Consumer Surplus, $C S$ | $A+B+C$ | $A$ | 0 |
| Producer Surplus, $P S$ | $D+E$ | $B+D$ | $A+B+C+D+E$ |
| Welfare, $W=C S+P S$ | $A+B+C+D+E$ | $A+B+D$ | $A+B+C+D+E$ |
| Deadweight Loss, $D W L$ | 0 | $C+E$ | 0 |

### 12.2 Perfect Price Discrimination

- The perfect price discrimination result of producing where demand equals MC means that the competitive quantity of output gets produced.
- Although this outcome is efficient...
- it maximizes total welfare
- no deadweight loss is generated
- ... it is harmful to consumers because all welfare is producer surplus!


### 12.3 Quantity Discrimination

- Price varies only with the quantity purchased, not across different consumers buying the same quantity.
- Not all quantity discounts are price discrimination; some reflect reductions in firm costs associated with large-quantity sales.
- Additionally, quantity discrimination may involve charging consumers more per unit rather than less.
- Example: increasing-block pricing associated with electricity; per KWH charge increases the more you use.


### 12.3 Quantity Discrimination

- Consider a firm that uses declining-block prices to maximize profit.
- $\$ 70$ is charged for $1 \leq Q \leq 20$
- $\$ 50$ is charged for $Q>20$
- Thus, a consumer who buys 30 units pays $\$ 70$ • 20 $=\$ 1400$ for the first block and $\$ 50 \cdot 10=\$ 500$ for the second block, for a total of $\$ 1900$.
- By contrast, under a non-discriminating monopoly, this consumer would be charge a uniform price of $\$ 60$ and pay a total of $\$ 1800$ for 30 units.


### 12.3 Quantity Discrimination


(b) Single-Price Monopoly


Quantity

|  | Discrimination | Single Price |
| :--- | :---: | :---: |
| Consumer Surplus, $C S$ | $A+C=\$ 400$ | $E=\$ 450$ |
| Producer Surplus or Profit, $P S=\pi$ | $B=\$ 1,200$ | $F=\$ 900$ |
| Welfare, $W=C S+P S$ | $A+B+C=\$ 1,600$ | $E+F=\$ 1,350$ |
| Deadweight Loss, $D W L$ | $D=\$ 200$ | $G=\$ 450$ |

### 12.4 Multimarket Price Discrimination

- Firms divide potential customers into two or more groups (based on some easily observable characteristic) and set a different price for each group.
- Example: senior or student discounts
- The firm chooses quantities sold to each group, $Q_{1}$ and $Q_{2}$, such that $\max _{Q_{1}, Q_{2}} \pi=R_{1}\left(Q_{1}\right)+R_{2}\left(Q_{2}\right)-C\left(Q_{1}+Q_{2}\right)$
- FOCs:

$$
\frac{\partial \pi}{\partial Q_{1}}=\frac{\mathrm{d} R_{1}\left(Q_{1}\right)}{\mathrm{d} Q_{1}}-\frac{\mathrm{d} C(Q)}{\mathrm{d} Q} \frac{\partial Q}{\partial Q_{1}}=0 \quad \frac{\partial \pi}{\partial Q_{2}}=\frac{\mathrm{d} R_{2}\left(Q_{2}\right)}{\mathrm{d} Q_{2}}-\frac{\mathrm{dC}(Q)}{\mathrm{d} Q} \frac{\partial Q}{\partial Q_{2}}=0
$$

- Marginal revenue from each group should be the same and equal to marginal cost:

$$
M R^{1}=M C=M R^{2}
$$

### 12.4 Multimarket Price Discrimination

- The first-order conditions imply that marginal revenue from each group should be the same and equal to marginal cost: $\quad M R^{1}=M C=M R^{2}$
- Because marginal revenue is a function of elasticity, we can write:

$$
\begin{gathered}
-\quad M R^{A}=p_{A}\left(1+\frac{1}{\varepsilon_{A}}\right)=m=p_{B}\left(1+\frac{1}{\varepsilon_{B}}\right)=M R^{B} \\
\frac{p_{B}}{p_{A}}=\frac{1+1 / \varepsilon_{A}}{1+1 / \varepsilon_{B}}
\end{gathered}
$$

- Thus, the higher price will be charged in the less elastic market segment.


### 12.4 Multimarket Price Discrimination

- The higher price will be charged in the less elastic market segment.



### 12.4 Multimarket Price Discrimination

- Welfare under multimarket price discrimination is lower than it is under either competition or perfect price discrimination.
- Under competition, more output is produced and CS is greater
- The welfare effects relative to uniform price monopoly are indeterminate.
- Both types of monopolies set price above marginal cost, so output is lower than in competition.
- Welfare is likely to be lower with discrimination because of consumption inefficiency and time wasted shopping.


### 12.5 Two-Part Tariffs

- Another form of second-degree price discrimination, a two-part tariff is when the firm charges a consumer a lump-sum fee for the right to purchase (first tariff) and a per unit fee for each unit actually purchased (second tariff).
- Think of the first tariff as an "access fee" and the second as a "usage fee"
- Examples:
- A country club charges a membership fee and greens fees to play a round of golf
- The state fair charges an entrance fee and a per ticket fee for rides
- Cell phone service providers charge a monthly service fee and a fee per text message


### 12.5 Two-Part Tariffs

- If all consumers are identical, the firm can capture all CS by setting charging a lump-sum "access fee" equal to CS $\left(A_{1}+B_{1}+C_{1}\right)$ and a "usage fee" equal to marginal cost (m).


### 12.5 Two-Part Tariffs

- Now assume that the monopoly has two customers.
- If the firm can treat customers differently, it can still capture all consumer surplus as in the previous graph.
- If the firm has to charge all customers the same price, it maximizes profit by:
- Setting the lump-sum "access fee" equal to the potential CS of the consumer with the smaller demand and a price that is above marginal cost.


### 12.5 Two-Part Tariffs

- With different customers, firm charges lumpsum fee of $A_{1}$ and per unit fee of $\$ 20$.
(a) Consumer 1

(b) Consumer 2



### 12.6 Tie-In Sales

- Another type of nonuniform pricing is a tie-in sale, in which customers can buy one product only if they agree to purchase another product as well.
- Requirement tie-in sale: customers who buy one product from a firm are required to make all purchases of another product from that firm.
- Example: photocopying machine buyers must buy services and supplies from same company.
- Bundling: two goods are combined so that customers cannot buy either good separately.
- Example: Refrigerators are sold with shelves.


### 12.7 Advertising

- Monopoly firms don't just decide on price and quantity, they also make important decisions about how much to advertise their products.
- Advertising may positively influence consumers' preferences and thereby increase demand for the product.
- Although higher demand increases gross profit, if the cost of advertising is substantial, net profit may or may not increase.


### 12.7 The Decision Whether to Advertise

- Advertise if cost is less than additional gross profit, area $B$.



### 12.7 How Much to Advertise

- If a monopoly raises advertising expenditures by $\$ 1$, how much does its gross profit rise?
- Additional advertising pays when gross profit rises by more than $\$ 1$ following an additional dollar spent on advertising.
- Thus, the profit-maximizing amount of advertising equates the marginal benefit and marginal cost of advertising.
- Mathematically: $\max _{Q, A} \pi=R(Q, A)-C(Q)-A$
- where $R$ is revenue and is a function of output and advertising cost


### 12.7 How Much to Advertise

- Given the maximization problem:

$$
\max _{Q, A} \pi=R(Q, A)-C(Q)-A
$$

- The profit-maximizing output and advertising levels are the $Q^{*}$ and $A^{*}$ that simultaneously satisfy the FOCs:

$$
\frac{\partial \pi(Q, A)}{\partial Q}=\frac{\partial R(Q, A)}{\partial Q}-\frac{d C(Q)}{d Q}=0 \quad \frac{\partial \pi(Q, A)}{\partial A}=\frac{\partial R(Q, A)}{\partial A}-1=0
$$

- The monopoly advertises until the marginal benefit from the last unit of advertising equals $\$ 1$, the marginal cost.

