

ECON 331

ASSIGNMENT #4

Question 1

a)

```
> restart;
```

The demand function:

```
> Qd:= k*P^(-epsilon) ;
```

$$Qd := k P^{(-\epsilon)}$$

Price elasticity of demand, 'ed':

```
> ed:= diff(Qd,P)*P/Qd;
```

$$ed := -\epsilon$$

The supply function:

```
> Qs:= c*(P-To) ;
```

Price elasticity of supply, 'es':

```
> es:= diff(Qs,P)*P/Qs;
```

$$Qs := c (P - To)$$

$$es := \frac{P}{P - To}$$

b)

```
> F:= Qd=Qs:
```

```
> dP_dTo:=simplify(implicitdiff(F,P,To)):
```

```
> Diff(P,To) = dP_dTo;
```

$$\frac{\partial}{\partial To} P = \frac{c P}{k P^{(-\epsilon)} \epsilon + c P}$$

Note that 'P' is the **equilibrium** price here.

c)

The 'assume' command allows us to restrict the values of variables or parameters to specified intervals. The following restrictions are appropriate for the market model:

```
> assume(k>0) :
```

```
> assume(epsilon>0) :
```

```
> assume(c>0) :
```

```
> assume (P>0) :
```

These restrictions allow us to determine if $0 < \frac{\partial}{\partial T_o} P < 1$ by using the 'is' command:

```
>
```

```
>
```

0

```
> is (0<dP_dTo) ;
```

true

```
> is (dP_dTo<1) ;
```

true

d)

Since $R = T_o Q_s(P, T_o)$, where P is the **equilibrium** price and Q_s is the **equilibrium** quantity, the total derivative of R with respect to T_o can be written as $Q_s + T_o \left(\frac{\partial}{\partial T_o} Q_s \right)$. Since $Q_s = c(P - T_o)$;

$\frac{\partial}{\partial T_o} Q_s = c \left(\left(\frac{\partial}{\partial T_o} P \right) - 1 \right)$. This allows us to express the total derivative of R with respect to T_o as a

relatively simple function of the equilibrium price and the parameters of the model:

```
>
```

```
> dR_dTo:=Qs+To*c*(dP_dTo-1) ;
```

$$dR_dT_o := c \sim (P \sim - T_o) + T_o c \sim \left(\frac{c \sim P \sim}{k \sim P \sim^{(-\varepsilon \sim)} \varepsilon \sim + c \sim P \sim} - 1 \right)$$

The tildes ('~') attached to variables/parameters in the above expression is Maple's way of reminding us that we have restricted these values to certain intervals (part c).

QUESTION 2

a)

```
> restart;
```

```
> C:=1600+40*Q+(2/3)*Q^(3/2) :
```

```
> AC:=expand (C/Q) ;
```

$$AC := \frac{1600}{Q} + 40 + \frac{2}{3} \sqrt{Q}$$

```
> MC:=diff (C,Q) ;
```

$$MC := 40 + \sqrt{Q}$$

b)

```
[ > P:=100+512*Q^(-1/2) :
```

```
[ > TR:=expand(P*Q) ;
```

$$TR := 100 Q + 512 \sqrt{Q}$$

```
[ > MR:=diff(TR,Q) ;
```

$$MR := 100 + \frac{256}{\sqrt{Q}}$$

```
[ c)
```

```
[ > Q:=solve(MC=MR,Q) ;
```

$$Q := 4096$$

```
[ > pi:=evalf(TR-C) ;
```

$$\pi = 1.021653333 \cdot 10^5$$

```
[ >
```