

**OPMT 5751: Important Formulas and Relations from Regression**

Total Sum of Squares:  $TSS = \sum(Y_i - \bar{Y})^2$

Residual Sum of Squares:  $RSS = \sum(\hat{Y}_i - \bar{Y})^2$

Error Sum of Squares:  $RSS = \sum(Y_i - \hat{Y}_i)^2$

Where  $Y_i$  is actual Y value,  $\hat{Y}_i$  is predicted Y value, and  $\bar{Y}$  is the average of actual Y values

Note that

$$\hat{Y}_i = a + bX_i$$

and we get  $a$  (intercept) and  $b$  (coefficient) from the Regression

The R-Squared is

$$R^2 = \frac{RSS}{TSS}$$

Variance and Standard Errors:

Variance of the error term is

$$s_e^2 = \frac{ESS}{n-2} = \frac{\sum e_i}{n-2}$$

Therefore, the standard error is:

$$s_e = \sqrt{\frac{ESS}{n-2}}$$

The Variance of  $b$  is

$$s_b^2 = \frac{\frac{ESS}{n-2}}{\sum (X_i - \bar{X})^2}$$

Thus the Standard Error of  $b$  is

$$s_b = \sqrt{\frac{\frac{ESS}{n-2}}{\sum (X_i - \bar{X})^2}}$$

**NOTE:** All of these values are produced automatically from the *Regression Toolpack output*. However, they can all be calculated by hand in the Spreadsheet as long as we have the estimates for  $a$  and  $b$ .