

More Ch 3 ... More Discrete Probability Models

Assignment: For Wed at class or tutorial.

3.1-10, 3.2-10, 3.3-4, 3.4-4, 3.5-10, 3.6-4

Note typo in first e-mail.

Recall Bernoulli trials indept sequence of bernoullis:

Binomial: Fix n , X = no of successes where $P(\text{Success}) = p$ fixed

e.g. How many winners with 1 ticket in 1000 lotteries? X

X in range $0, 1, 2, \dots, n$

Geometric: Bernoulli trials again. But number of trials is random variable

this time. How many trials til first success? $P(\text{success})=p$ fixed.

See p 111. For $X=x$, must fail $x-1$ times and then win.

$P(X=x) = p(1-p)^{(x-1)}$ $x=1, 2, 3, \dots$

e.g.1 How many lotteries til major prize?

e.g.2 $P(\text{fatal accident}) = p$ How many drives?

Hypergeometric:

Recall Binomial application to sampling a large population:

With or without replacement does not matter.

Small population, does matter

Let X be number in random sample of a particular kind, where sampling is without replacement, from a population of size N .

X is Hypergeometric. p 117

$P(X=x) = \frac{rCx \cdot (N-r)C(n-x)}{NCn}$ $x = \max(0, n-(N-r)), \dots, \min(n, r)$

example: 20 light bulbs - 3 are faulty

sample 5 of them: Let X be number faulty in sample of 5.

$P(X=x) = \frac{3Cx \cdot 17C(5-x)}{20C5}$ $x = 0, 1, 2, 3$

$$P(X=1) = \frac{3C1 \cdot 17C4}{20C5} = \frac{3 \cdot (17 \cdot 16 \cdot 15 \cdot 14 / 24)}{(20 \cdot 19 \cdot 18 \cdot 17 \cdot 16 / 120)}$$

$$= .46$$

Binomial? $n=5$, $p=.15$ table p 404 \rightarrow .39 for $P(X=1)$

Consider sample of 20, $SD = 0!$ but for Binomial $SD = \sqrt{20 \cdot .15 \cdot .85} = 1.6$

Multinomial: sample n things with replacement from pop of k kinds of things.

sample is vector:

20% Green, 50% blue, 30% red. Sample 5 things \rightarrow B,G,G,R,B

$P(2G,2B,1R) = ?$ see p 121

Relationship to Binomial. 2 kinds.

Poisson Random Variable: number of instances of something

p 125 $X =$ number of events

$$P(X=x) = \exp(-\mu) \mu^x / x!$$

example. Murders in Vancouver: 10 per year

How many in 1 month? average is $10/12 = \mu$

$$P(X=0) = \exp(-10/12) = .43$$

$$P(X=1) = \exp(-10/12) (10/12) = .36$$

$$P(X=2) = \exp(-10/12) (10/12)^2 / 2! = .43 \cdot .15$$

Relationship to Binomial: p small, n large, approaches Poisson with $\mu=np$