**STAT 280** 

November 26, 2001

Projects are still being marked. Return by Friday.

Today: Review of Ch 7 (7.5 on)-Ch 8 And Course Evaluations

7.5 M/M/1 Queuing Process

Can consider as composed of two parts:

- I Event times (of arrivals and service completions)
- II Transitions of queue length state



II is sometimes called the Imbedded Markov Chain

Note that transitions in the Imbedded Markov Chain can only be +1 or -1; that is  $i \rightarrow i+1$  or  $i \rightarrow i-1$ .

Conversely, a change in the queue length indicates whether it is an arrival or a service completion.

Steady State distributions for an M/M/1 queue can be found from simulations, or using the formula p 295.

r = A/S is called the arrival/service ratio.

 $_{i} = (1 - _{A}/_{S})(_{A}/_{S})^{i}$  for i = 0, 1, 2, ...

7.6-7.8 M/M/k

Balance equations:

The rate of arrivals to state j

= rate of service completions from state j+1

 $_{j}a_{j}=\ _{j+1}s_{j+1}$ 

This leads to steady state distribution of queue length (See page 308) but requires

 $1+a_0/s_1+a_0a_1/s_1s_2+a_0a_1a_2/s_1s_2s_3+\ldots$ must be finite. (\*) Note need for  $_0$  computed from sum of k terms

Consider what happens when  $k \ge 1000$ . Infinite server queue. Queue length would then be Poisson. Why? See Sec 7.8.

Ch 8: Sums of Independent Random Variables 8.1 – 8.3: CLT and basics about mean and variance. 8.4: Random Sums of RVs: Main result Thm 8.4-1 about Compound Poisson Process. Events with exponential interarrivals but count may be any RV, not just +1. Compound Poisson Process is cumulative "counts"  $\{N(t); t>0\}$ . "Counts" really just sum – not integer.

\*\*\*\*\*\*Time for Course Evaluations\*\*\*\*\*\*\*\*



Calculation Depends of Thm 2.9-1 and 2.9-2. Review later.