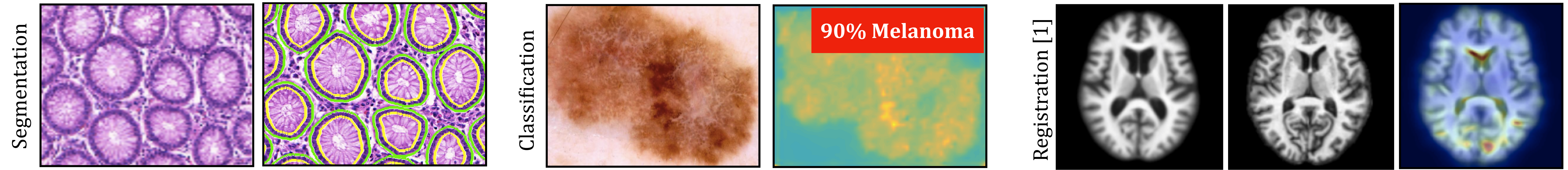
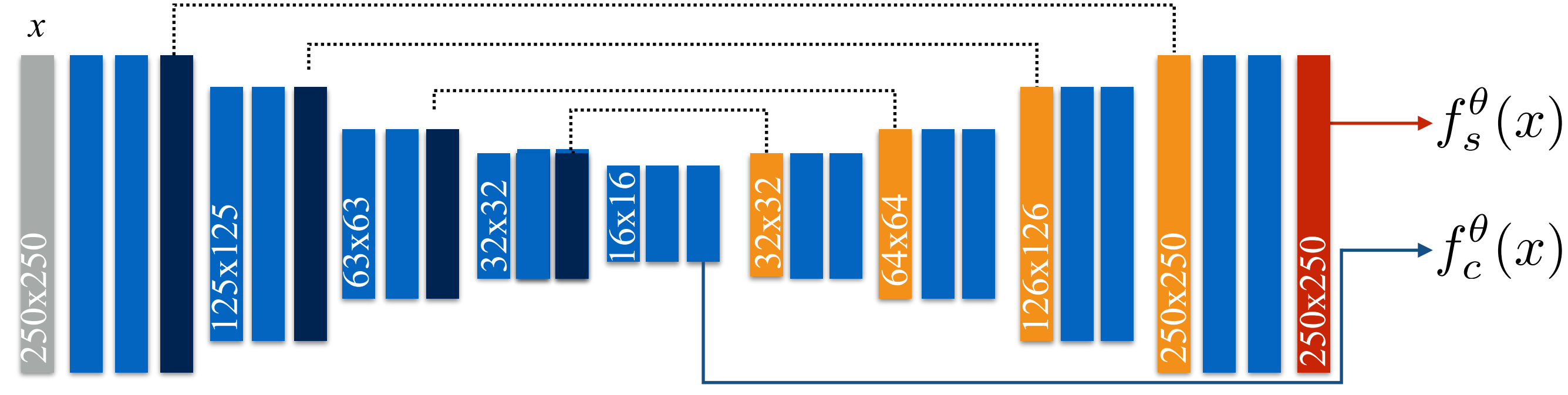


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Uncertainty In Medical Image Analysis



State of the art deep learning models



... can encode flexible priors as multi loss functions [2]

$$\mathcal{L}_{total}(x; \theta) = \sum_{i=1}^T \lambda_i \mathcal{L}_i(x; \theta)$$

Generally, set via grid search
Could be set based on model's uncertainty [3]?

$\mathcal{L}_i =$ Segmentation Loss

Uncertainty Driven Multi Loss Function

$$\mathcal{L}_{total}(x; \theta, \sigma_c, \sigma_s, \sigma_t, \sigma_g) = \mathcal{L}_c(x; \theta, \sigma_c) + \mathcal{L}_s(x; \theta, \sigma_s) + \mathcal{L}_t(x; \theta, \sigma_t) + \mathcal{L}_g(x; \theta, \sigma_g)$$

Uncertainty-Based Predictions

$$P(C_k = 1 | x, \theta, \sigma_c) = \frac{\exp(\frac{1}{\sigma_c^2} f_{c_k}^\theta(x))}{\sum_{k'=1}^K \exp(\frac{1}{\sigma_c^2} f_{c_{k'}}^\theta(x))}$$

Uniform $f_{c_k}^\theta(x)$ Non-Uniform $f_{c_k}^\theta(x)$

Multi-Region Interactions

A ← Excludes → B B → Contains → C

A	1	0	0
B	0	1	1
C	0	0	1
$V(S_p)$	1	1	1
S_p	A	B	C

$$P_t(S_p^r | x_p; \theta) = \frac{1}{Z} V(S_p) \prod_{r=1}^L \exp(\frac{1}{\sigma_t^2} f_{s_r}^\theta(x_p)) \times S_p^r$$

Smooth Object Boundaries

Connected neighbours with different labels. Connected neighbours sharing a label.

$$\mathcal{L}_c(x; \theta, \sigma_c) = \frac{1}{\sigma_c^2} \sum_{k=1}^K -C_k \log P(C_k = 1 | x_p; \theta) + \log \sigma_c^2$$

$$\mathcal{L}_t(x; \theta, \sigma_t) = \frac{1}{\sigma_t^2} \sum_{p \in \Omega} \sum_{r=1}^L -S_p^r \log P_t(S_p^r = 1 | x, \theta) + \log \sigma_t^2$$

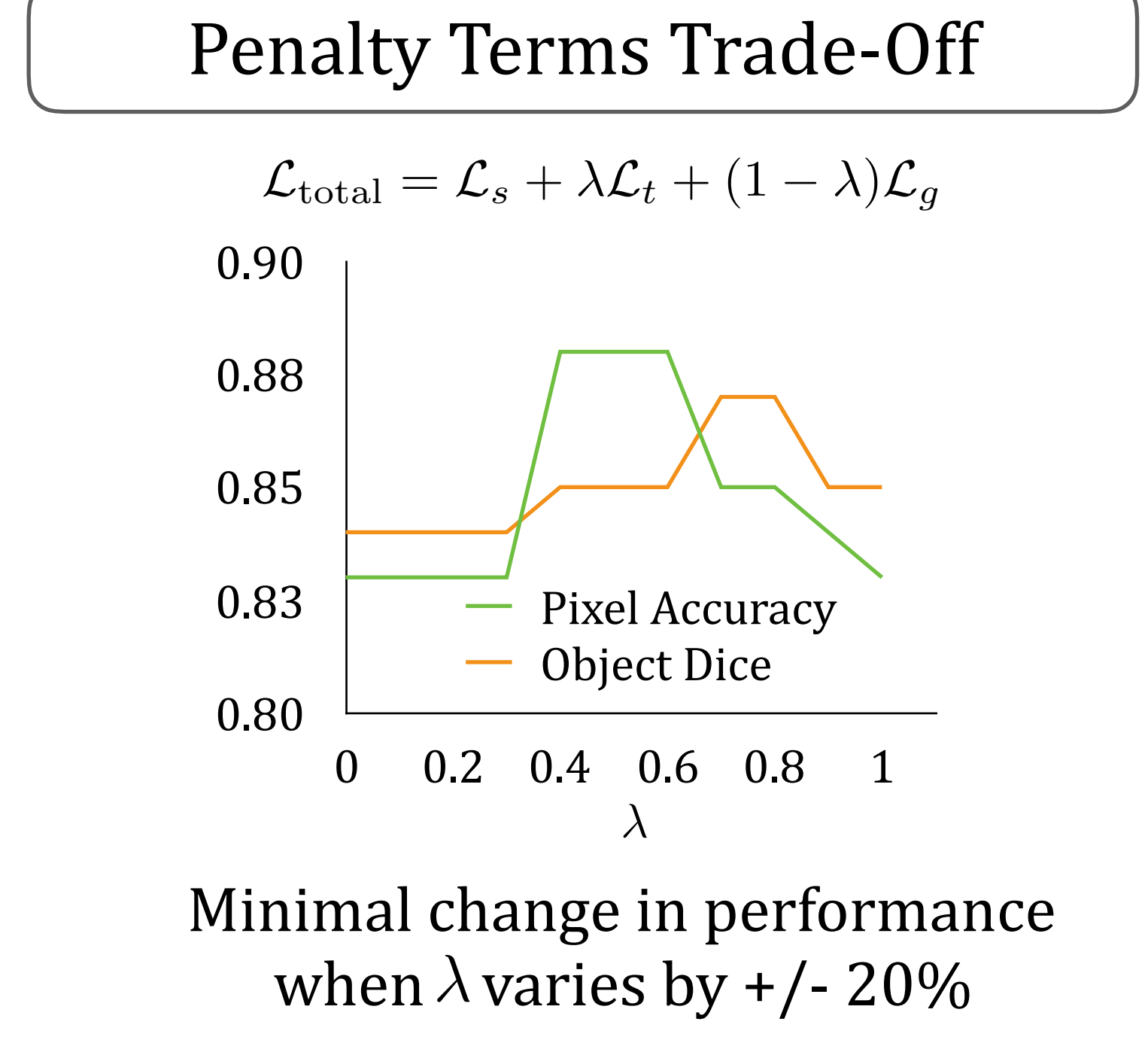
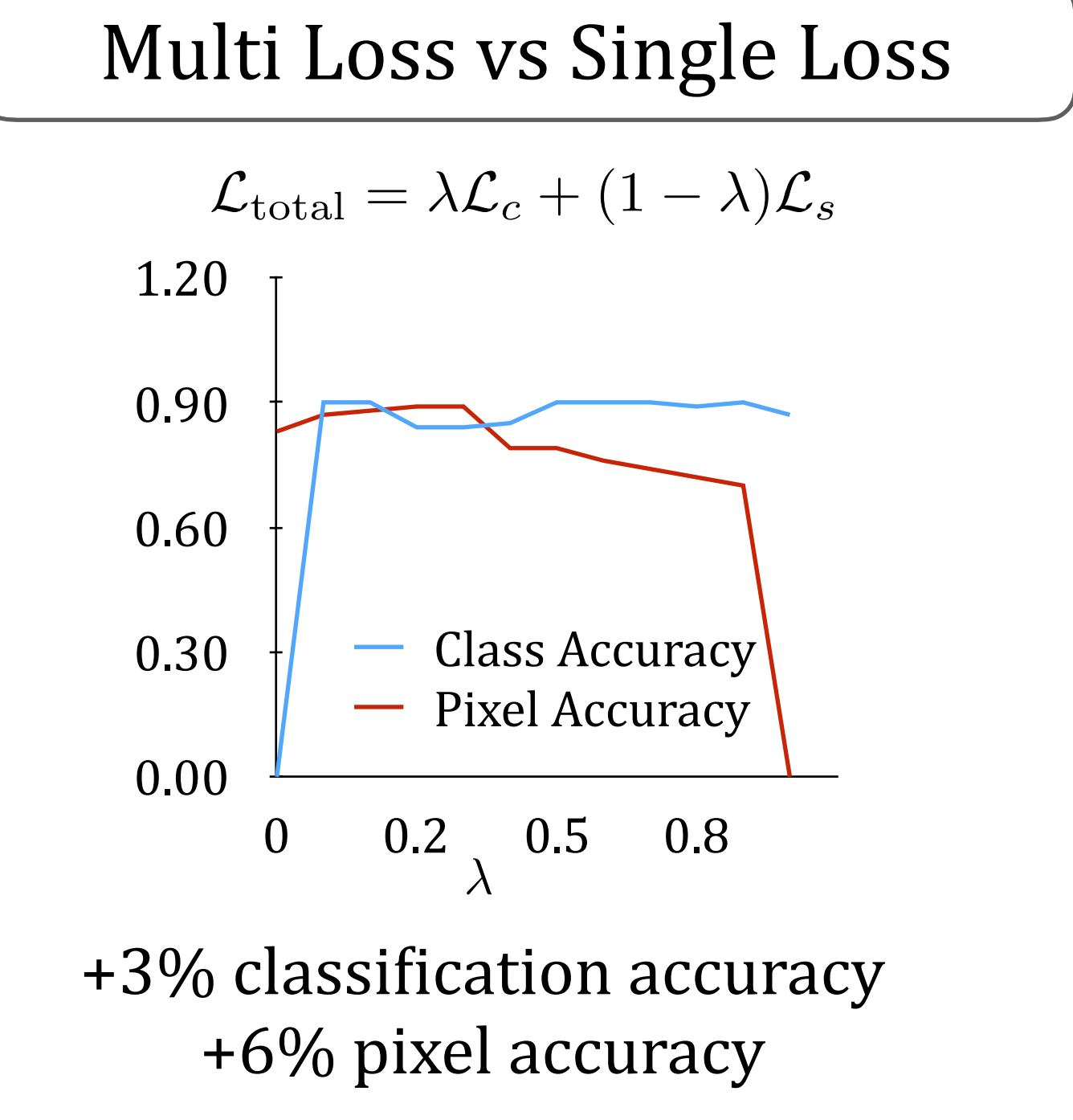
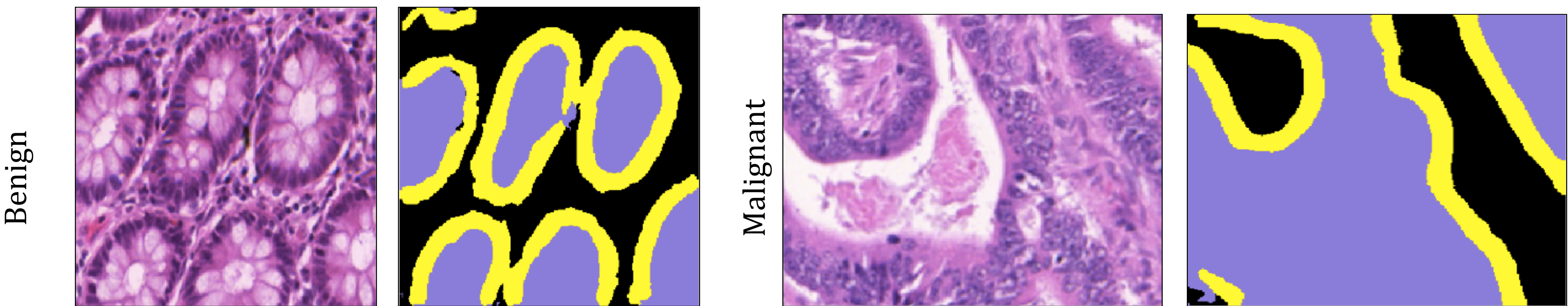
$$\mathcal{L}_s(x; \theta, \sigma_s) = \frac{1}{\sigma_s^2} \sum_{p \in \Omega} \sum_{r=1}^L -S_p^r \log P(S_p^r = 1 | x, \theta) + \log \sigma_s^2$$

$$\mathcal{L}_g(x; \theta, \sigma_g) = \frac{1}{\sigma_g^2} \sum_{p \in \Omega} \sum_{r=1}^L \sum_{q \in \mathcal{N}^p} S_p^r \left| \log \frac{P_t(S_p^r | x_p; \theta)}{P_t(S_q^r | x_q; \theta)} \right| B_{p,q} + \log \sigma_g^2$$

Validation And Performance

Dataset

- Warwick-QU Colon Adenocarcinoma Dataset [4]
- 70 Training / 15 Validation / 80 Test Images
- Image and Pixel-Level Annotation
- All models were randomly initialized



Uncertainty Driven Trade-Off

	Without uncertainty	With Uncertainty
$\mathcal{L}_c + \mathcal{L}_s$		
Accuracy	0.9	0.95
Dice	0.8	0.79
$\mathcal{L}_c + \mathcal{L}_s + \mathcal{L}_t$		
Accuracy	0.94	0.94
Dice	0.8	0.81
$\mathcal{L}_c + \mathcal{L}_s + \mathcal{L}_t + \mathcal{L}_g$		
Accuracy	0.91	0.95
Dice	0.83	0.87
Best Parameters		
Accuracy	0.95	0.95
Dice	0.85	0.87

+2% Object Dice when using uncertainty driven loss vs extensive grid search

[1] Yang et al. Fast Predictive Image Registration, LABELS 2016
[2] BenTaieb et al. Topology Aware Fully Convolutional Networks for Histology gland Segmentation, MICCAI'16
[3] Kendall et al. Multi-task learning using uncertainty to weigh losses for scene geometry and semantics, arXiv 2017
[4] Sirinukunwattana et al. Gland Segmentation in colon histology images: the GlaS contest, arXiv 2016