1. In  $\mathbb{Z}[x]$ , the ideal  $(2x^2 - 4, 4x - 5)$  is not principal. However, this ideal is principal in R[x]. What is it generated by?

2. Let  $\varphi: R \to S$  be a ring homomorphism. Show that the image of  $\varphi$ , denoted by  $\varphi(R)$  is a subring of S.