

1. Consider the polynomial  $x^2 + x + 1$ .

(a) Substitute  $y + 1$  for  $x$  and expand the result.

(b) Why is the polynomial in  $y$  you obtained in part (a) irreducible?

(c) Why does the work you have done in parts (a) and (b) show that  $x^2 + x + 1$  must also be irreducible?