Math 5320, 4/13/18 Worksheet 32: The Main Theorem

1. Consider the Galois extension  $\mathbb{Q}(\sqrt{2},\sqrt{3})/\mathbb{Q}$ . What is its Galois group? What subgroup of the Galois group does the field  $\mathbb{Q}(\sqrt{6})$  correspond to?

2. Is  $\mathbb{Q}(\sqrt{6})/\mathbb{Q}$  Galois? What are some different methods you could use to answer this question?