Worksheet 8: Prime ideals, integral domains

1. Show that if $R$ is an integral domain, then $R[x]$ is also an integral domain.
2. Cancellation works in integral domains. That is, if $R$ is an integral domain with $a, b, c \in R$, and $a c=b c$, then $a=b$. Why is this true in integral domains? Can you think of an example in a ring that's not an integral domain where cancellation doesn't work?
3. Why is any subring of an integral domain an integral domain?
