

Topics for Today

1.) Current Acct. Sustainability

2.) Comparative Statics Predictions

- Temporary Output Shocks
- Permanent Output Shocks
- Anticipated Changes in Future Output
- Terms of Trade Shocks
- Changes in Risk
- World interest rate shocks.

Comparative Statics

- One of the main reasons for exploring the microfoundations of CA dynamics is that it provides a clear basis for comparative statics predictions. That is, given a change in a country's external environment or govt. policy, how will its CA change?
- The text pursues a graphical approach, with an emphasis on showing how various shocks influence the country's budget constraint. From that analysis, it's clear that virtually anything can happen after a shock, depending on the relative strength of income + substitution effects and the relative income effects on current + future consumption.
- To get clear predictions, economists often consider explicit functional forms, which place restrictions on income + substitution effects.

- We will do the same here. Let's first solve for the CA as a function of the exogenous variables, and then use this solution to make comparative statics predictions.
- Suppose preferences take the following form:

$$U(c_1, c_2) = \ln c_1 + \beta \ln c_2 \quad \beta < 1$$

For simplicity, assume $B_0^* = 0$ (no initial net foreign assets).

Optimality Condition

$$\frac{U_1}{U_2} = 1+r \implies \frac{c_2}{\beta c_1} = 1+r$$

$$\implies c_2 = \beta(1+r)c_1$$

Note that the nature of the optimal consumption plan depends on the relationship between the interest rate, r , and the country's rate of "time preference", ρ , where $\beta = \frac{1}{1+\rho}$:

1.) If $\rho > r \Rightarrow$ country is relatively impatient
 $\Rightarrow \beta(1+r) < 1$
 $\Rightarrow c_2 < c_1$
 \Rightarrow falling consumption path

2.) If $\rho < r \Rightarrow$ country is relatively patient
 $\Rightarrow \beta(1+r) > 1$
 $\Rightarrow c_2 > c_1$
 \Rightarrow rising consumption path

3.) $\rho = r \Rightarrow$ country has same patience as other countries
 $\Rightarrow \beta(1+r) = 1$
 $\Rightarrow c_2 = c_1$
 \Rightarrow consumption-smoothing

- The first 2 cases predict that a country's wealth will be either falling or rising indefinitely. It's hard to imagine real world examples of this. So let's take as our benchmark

$$\beta(1+r) = 1 \Rightarrow C_2 = C_1$$

- Substituting this into the budget constraint,

$$(1 + \frac{1}{1+r})C_1 = Q_1 + \frac{Q_2}{1+r}$$

$$\Rightarrow C_1 = \frac{1+r}{2+r} (Q_1 + \frac{Q_2}{1+r})$$

Since $B_0^* = 0$,

$$CA_1 = TB_1 = Q_1 - C_1$$

$$\Rightarrow CA_1 = \frac{1}{2+r} (Q_1 - Q_2)$$

Temporary Output Shocks

Suppose output falls temporarily.

$$\Delta Q_1 < 0 \quad \Delta Q_2 = 0$$

$$\Rightarrow \Delta CA_1 < 0 \quad (= \frac{1}{1+r} \Delta Q_1)$$

\Rightarrow Current Acct. Deficit

Interpretation: Country borrows to cushion the blow of the temporary output loss.

Permanent Output Shocks

Now suppose output falls permanently.

$$\Delta Q_1 = \Delta Q_2 < 0$$

$$\Rightarrow \Delta CA_1 = 0$$

\Rightarrow Currnt. Doesn't Change

Interpretation: No reason to borrow now, since income will be lower in the future too. Consumption just declines by the fall drop in income.

Anticipated Change in Future Income

Suppose income is expected to rise in the future $\Delta Q_1 = 0$ $\Delta Q_2 > 0$

$$\Rightarrow \Delta CA_1 < 0 \quad \left(= -\frac{1}{2+r} \Delta Q_2 \right)$$

\Rightarrow Current Acct. Deficit

Interpretation: Country borrows on the basis of its higher future income.

Punchline

Current Accts. respond to temporary shocks, but not to permanent shocks.

This result is more general than this simple model might suggest. It extends to settings with many (infinite) periods, uncertainty, and more general preference specifications.

Terms of Trade Shocks

- In the real world, there's more than one good! Typically, the goods that a country buys on world markets are different from the goods it sells.
- Changes in the price of a country's exports relative to the price of its imports are the most important real world among shocks.

• Define $TT = \frac{P_x}{P_m} = \text{Terms of Trade}$

$TT \uparrow \Rightarrow$ Terms of Trade Improvement
 \Rightarrow Get more imports for each unit of exports you give up.

Suppose international Bonds are denominated in importable goods. The budget constraints become:

$$C_1 + B_1^* - B_0^* = r_0 B_0^* + TT_1 \cdot Q_1$$

$$C_2 + B_2^* - B_1^* = r_1 B_1^* + TT_2 \cdot Q_2$$

Combining and imposing the TVC ($B_2^* = 0$),

$$C_1 + \frac{C_2}{1+r_1} = (1+r_0)B_0^* + TT_1 \cdot Q_1 + \frac{TT_2 \cdot Q_2}{1+r_1}$$

Note that Terms of Trade shocks operate just like income shocks. In particular, we have:

The Currnt. Acct. responds to temporary or expected future Terms of Trade shocks, but not to permanent Terms of Trade shocks.

Uncertainty and the Trade Balance

Consider an economy that initially has known and constant income $Q_1 = Q_2 = Q$, with preferences,

$$U(c_1, c_2) = \ln c_1 + \ln c_2$$

Suppose $B_0^* = 0$ and $r = 0$.

Now the optimality condition implies $c_2 = c_1$. Substituting into the budget constraint

$$2c_1 = Q_1 + Q_2 = 2Q$$

$$\Rightarrow c_1 = Q$$

$$\Rightarrow TB_1 = CA_1 = 0$$

Now suppose everything is the same except Q_2 becomes risky

$$Q_2 = \begin{cases} Q+a & \text{with prob. } \frac{1}{2} \\ Q-a & \text{with prob. } \frac{1}{2} \end{cases}$$

Now households must maximize expected utility

$$\ln C_1 + E \ln C_2$$

where

$$\begin{aligned} C_2 &= 2Q+a - C_1 && \text{in good state} \\ &= 2Q-a - C_1 && \text{in bad state} \end{aligned}$$

Subbing in,

$$\max_{C_1} \ln C_1 + \frac{1}{2} \ln(2Q+a-C_1) + \frac{1}{2} \ln(2Q-a-C_1)$$

First-Order Condition

$$\frac{1}{c_1} = \frac{1}{2} \left[\frac{1}{2Q+a-c_1} + \frac{1}{2Q-a-c_1} \right]$$

$$\Rightarrow c_1 < Q$$

$$\Rightarrow TB_1 > 0$$

Interpretation : Greater uncertainty leads to precautionary saving

Conjecture : Explains reserve accumulation in Asia following the 1997-98 Asian Crisis ?